Diffuse Extragalactic Emission at Low Frequencies within the Epoch of Reionization 0-hour Field

MSc Thesis

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A thesis submitted to the Victoria University of Wellington in fulfilment of the requirements for the degree of Master of Science in Physics. Victoria University of Wellington 2017
Abstract

Low-frequency radio imaging of the southern sky has become available with the advent of the Murchison Widefield Array (MWA). The topic of this thesis is the study of extended, low-frequency radio emission, with a primary focus on the non-thermal synchrotron emission associated with the intra-cluster medium (ICM) of galaxy clusters. We do not limit the study to such emission, however, and investigate a small sample of other interesting and extended radio emission from objects in the southern sky.

A significant portion of this work is invested in detecting, and characterising, extended, diffuse radio emission from galaxy clusters within a 45 degree by 45 degree region of the southern sky centred on R.A. = 0°, decl. = −27°. This field is chosen as a deep MWA image has been made available which is sensitive to extended structures. Within the field we search for low-frequency, diffuse cluster emission, previously detected or otherwise. In doing so we find 34 diffuse radio sources, 3 of which are newly detected haloes, 1 newly detected relic with many new candidates of each. Further, we detect a new phoenix candidate as well as 2 candidate dead radio galaxies at the centre of clusters. We confirm previous observations of such emission as well, and measure properties such as their integrated flux densities, spectral indices, and sizes where possible. We compare our sample of haloes with previously detected haloes and revisit established scaling relations of the radio halo power ($P_{1.4}$) with the cluster X-ray luminosity ($L_X$) and mass ($M_{YZ,500}$). We find that both scaling relations are consistent with previous findings despite the increase in sample size, though note that the raw scatter in the data for best-fitting parameters increases with increase in sample size. In this, we demonstrate the utility of low-frequency radio telescopes like the MWA in detecting such emission, showing that the MWA is pushing into higher-redshift, lower-mass systems, though we caution that the low resolution of the MWA can work against us.

We follow-up on two galaxy clusters found to host extended emission—Abell S1136 and Abell S1063. In the case of Abell S1136 we observe the emission at its centre with the Australia Telescope Compact Array (ATCA) and determine the presence of a core, suggesting the emission to be that of an ancient episode of an active galactic nucleus in the central elliptical of the cluster, ESO 470-G020. After reducing archival ATCA data for Abell S1063 we find no evidence of a halo and consider the source to be constructed of blended point sources. We close with a description of a strong double-lobed radio source associated with a non-elliptical host ESO 472-G013, likely a spiral or irregular galaxy, that was found serendipitously whilst searching for diffuse cluster emission. We explore the host within the context of star-formation, and consider the possible origins of the AGN and lobes due to interaction with either the nearby spiral, ESO 472-G012, or a past or ongoing merger event.
Statement of Originality

I certify that this work contains no material which has been accepted for the award of any other degree or diploma in any university or other tertiary institution and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text. In addition, I certify that no part of this work will, in the future, be used in submission for any other degree or diploma in any university or other tertiary institution without the prior approval of the Victoria University of Wellington and where applicable, any partner institution responsible for the joint-award of this degree. I give consent to this copy of my thesis, when deposited in the University Library, being made available for loan and photocopying, subject to the provisions of the Copyright Act 1994. I also give permission for the digital version of my thesis to be made available on the web, via the University’s digital research repository, the library catalogue and also through web search engines, unless permission has been granted by the University to restrict access for a period of time.

In preparation of this manuscript and this work, I acknowledge Dr. Siamak Dehghan for providing optical density analyses for §ii.2.2.25 and Dr. Qian Zheng who organised, calibrated, and flagged data from the ATCA presented in §iii.2.

List of publications being prepared based on work in this thesis (titles pending):

- Duchesne, S. W., Johnston-Hollitt, M., Offringa, A. R., Pratt, G. W., Zheng, Q., and Dehghan, S., (in prep.) Diffuse galaxy cluster emission at 168 MHz within the Murchison Widefield Array Epoch of Reionization 0-hour field.

- Duchesne, S. W., Johnston-Hollitt, M., and Zheng, Q., (in prep.) The curious AGN associated with the star-forming galaxy ESO 472-G013.

List of publications being prepared, that the author has been involved in during the course of this thesis and topically related (titles pending):


List of publications that the author has been involved in during the course of this thesis, though not topically related to the work in this thesis:


Acknowledgements

First and foremost, I would like to thank my supervisor, Assoc. Prof. Melanie Johnston-Hollitt, who through the course of this work has been a wealth of knowledge and motivation; providing myriad ideas and support for the direction in which this work has progressed. I must also thank her for the funding provided, without which I would not be involved in this research.

I thank Dr. Siamak Dehghan, Dr. Qian Zheng, and Dr. Sara Shakouri, who have been more than helpful and were always willing to answer questions, ranging from “Where do I start with MIRIAD?” to “Do you know how to truncate the bibliography entries for bibtex?” I would also like to thank Susannah Keel for pointing out the diffuse emission within Abell S1099.

I would like to thank Dr. Gabriel Pratt, who provided processed X-ray data from deep XMM-Newton observations of a sample of galaxy clusters, and Dr. Philip Edwards who awarded director’s discretionary time for observations with the ATCA. I also thank Dr. Emil Lenc who provided the baseline data of the MWA, and Prof. Thomas Reiprich, who provided a look at the X-ray emission from Abell 2496 prior to its public availability. I must also thank Dr. André Offringa who provided the EoR0 field, the image upon which this work is based.

Last, but very much not least, I would like to thank my parents, Tracey and Guy Duchesne, who have supported me throughout this work, but also through all previous studies.
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§i. Introduction

§i.1. Extragalactic radio emission

When observing the sky, radio emission is found to come from within and beyond the Milky Way. Even within our own solar system radio emission is abundant; the positions of Jupiter and the Sun, for instance, need to be taken into account when observing with radio telescopes lest they interfere with observations. Beyond the solar system, but within our galaxy, radio emission may originate from stars—variable (Hewish et al., 1968) or otherwise—or their decaying husks in the form of supernova remnants (SNR, e.g. the Crab Nebula; Bolton et al., 1949), as well as the most compact objects known: the emission from the proposed black hole at the centre of the Milky Way, Sagittarius A* (Balick and Brown, 1974; Brown, 1982; Doeleman et al., 2008).

However it is radio emission of extragalactic origin that is the topic of this work. Extragalactic radio emission was first discovered by Bolton et al. (1949) when they considered the association of the radio source Centaurus A with the optical galaxy NGC 5128. After this, radio sources began to be associated with optical galaxies (e.g. Baade and Minkowski, 1954) and the study of radio galaxies and their associated emission has become an important part of astronomy. It is now known that typical radio galaxies are so-called because of the central monster within—usually an active galactic nucleus (AGN; Scheuer, 1974; Blandford and Rees, 1974) that is centrally located, associated with a black hole and likely an accretion disk. These engines emit across the electromagnetic spectrum, but classes of these object show comparatively strong radio emission. It is not only AGN that will produce radio emission from a galaxy. Star formation—especially in blue, dusty spiral galaxies—will leave a distinctive radio tracer (see e.g. Condon, 1992). These star-forming galaxies do not tend to have radio-loud AGN. Instead, their radio emission is generated by the ionized hydrogen (H\text{II}) regions which themselves plot potential star-formation sites. There is a final class of extragalactic radio emission that needs to be considered, especially at low radio frequencies: non-thermal, diffuse radio emission associated with galaxy clusters. This emission, associated with the intra-cluster medium (ICM) rather than any particular galaxy, is found in only a small selection of clusters and the main purpose of this research has been the search for this emission.

§i.1.1. Synchrotron emission

To understand extragalactic radio emission, we must first consider the radiation mechanism responsible for most extragalactic emission. This is synchrotron emission from charged electrons travelling along helical paths adjacent to magnetic field
lines. The following is adapted from Rybicki and Lightman (2004). We begin with a discussion of relativistic electromagnetic potentials: the vector potential $A(r, t)$ and scalar potential $\phi(r, t)$. Within the context radiation from charged electrons, we consider the Liénard-Wiechart potentials described by the following

\begin{equation}
A(r, t) = \frac{\mu_0}{4\pi} \frac{q v(t')}{(1 - R \cdot v(t'/c) / R)}, \tag{i.1}
\end{equation}

\begin{equation}
\phi(r, t) = \frac{1}{4\pi \varepsilon_0} \frac{q}{(1 - R \cdot v(t'/c) / R)}, \tag{i.2}
\end{equation}

where $v(t')$ is the particle’s measured velocity, $R = r(t) - r_0(t')$, $R = |r(t) - r_0(t')|$, and $t'$ is the retarded time, defined as

\begin{equation}
t' = t - \frac{|r(t) - r_0(t')|}{c}, \tag{i.3}
\end{equation}

for a particle at position $r$ measured at $r_0$. This represents the finite speed of light and transmission of information in general. An important result of these potentials arises due to the retarded time—this is the result that charged particles acting within these potentials radiate electric and magnetic fields. From Maxwell’s equations, Eq. i.1 and i.2 are used to give the electric and magnetic radiation fields, $E_{\text{rad}}(r, t)$ and $B_{\text{rad}}(r, t)$ as

\begin{equation}
E_{\text{rad}}(r, t) = \frac{q}{4\pi \varepsilon_0} \left\{ \frac{(\hat{R} - \beta)}{(1 - \hat{R} \cdot \beta)} \frac{1}{R^2} + \frac{\hat{R}}{(1 - \hat{R} \cdot \beta)} \right\} \frac{1}{R} \left[ \left( \hat{R} - \beta \right) \times \dot{\beta} \right], \tag{i.4}
\end{equation}

\begin{equation}
B_{\text{rad}}(r, t) = \frac{1}{c} \hat{R} \times E_{\text{rad}}(r, t), \tag{i.5}
\end{equation}

with $\beta = v(t')/c$. A further implication of the retarded time is the beaming effect which is more apparent as $v$ approaches the speed of light. Radiation directly in front of the particle’s trajectory will be strongest. These results can be used to show that the power radiated from a moving particle is

\begin{equation}
P' = \frac{2q^2}{3c^3} |a'|^2, \tag{i.6}
\end{equation}

which, in the instantaneous rest-frame of the particle, with $a_0' = 0$ can be written as

\begin{equation}
P = \frac{2q^2}{3c^3} \gamma^4 \left( a_\perp^2 + \gamma^2 a_\parallel^2 \right), \tag{i.7}
\end{equation}

since $dW = \gamma dW'$ and $dt = \gamma dt'$ imply that $P' = P$. With this framework, we can now consider synchrotron radiation from a charged particle under the influence of a magnetic field, $\mathbf{B}$ and electric field, $\mathbf{E}$. The four-vector of acceleration for a particle with four-velocity $U^\nu$, mass $m_0$, charge $e$, and the electromagnetic field tensor $F^\mu{}_{\nu}$, is

\begin{equation}
a^\nu = \frac{q}{mc} F^\mu{}_{\nu} U^\nu. \tag{i.8}
\end{equation}
This result can be used to show that the equations of motion for a particle acted on by electric and magnetic fields are

\[ \frac{d}{dt} (\gamma m v) = \frac{q}{c} v \times B, \]  
\[ (i.9) \]

\[ \frac{d}{dt} (\gamma mc^2) = q v \cdot E. \]  
\[ (i.10) \]

Eq. \( i.10 \) is simply 0 as we are considering the case of no (or negligible) electric field. The implication of this is that \( |v| = \) constant, and from that we can see that \( v_\parallel = \) constant and \( |v_\perp| = \) constant which means we have circular motion about the magnetic field in a plane with normal vector in the direction of \( B \). Thus, for a particle moving parallel to the magnetic field the overall motion will be the combination of this circular motion and its inherent linear motion, creating a helical path. We can calculate the frequency of this motion (the gyration frequency, \( \omega_B \)) as

\[ \omega_B = \frac{qB}{\gamma mc}. \]  
\[ (i.11) \]

The perpendicular component of the acceleration is related to this gyration frequency by \( a_\perp = \omega_B v_\perp \), and with no parallel acceleration component we can use the relativistic Larmor formula, Eq. \( i.7 \), to show that the power radiated by a given particle in the simplest case of parallel motion to the magnetic field is

\[ P = \frac{2q^2}{3c^3} \frac{q^2B^2}{\gamma^2m^2} \beta_\perp^2. \]  
\[ (i.12) \]

This result is more useful if we integrate over all possible pitch angles, \( \theta \), which is the angle between the field and the direction of velocity of the electron. Thus \( \langle \beta_\perp^2 \rangle = 2\beta^2 / 3 \) and

\[ P = \left( \frac{2}{3} \right)^2 \frac{q^2B^2}{c^2m^2} \beta^2. \]  
\[ (i.13) \]

However this is the power radiated from a single electron. To determine the total power radiated per unit frequency for a population of electrons, \( P_{\text{tot}}(\nu) \), we must integrate over the entire population including their corresponding energies. If we assume the electron population can be described by a powerlaw with index \( p \), we have \( N(E)dE \propto E^{-p}dE \). Thus the total power per unit frequency is

\[ P_{\text{tot}}(\nu) \propto \int_{E_1}^{E_2} P(\nu)E^{-p}dE, \]  
\[ (i.14) \]

where \( E_1 < E < E_2 \). We define here a critical frequency, \( \nu_c \), such that

\[ \nu_c = \frac{3}{2\omega_B}\gamma^3 \sin \theta, \]  
\[ (i.15) \]

which allows the definition of a dimensionless, constant function \( F(\nu/\nu_c) \) proportional to the radiated power of a single electron. Hence Eq. \( i.14 \) can be written

\[ P_{\text{tot}}(\nu) \propto \int_{E_1}^{E_2} F\left( \frac{\nu}{\nu_c} \right) E^{-p}dE. \]  
\[ (i.16) \]
\section*{Example spectral energy distributions.} \textit{Left:} The spectral energy distribution of the radio galaxy, Centaurus A (Alvarez et al., 2000, and references therein). Note that the index is shallower than that calculated by Alvarez et al. as the 4.7 MHz measurement is included here. \textit{Right:} The same for the radio halo within the Bullet Cluster, 1E 0657-56 (Srinivasan, 2015, and references therein). Note that the index is shallower than that calculated by Srinivasan as all data are included here. Both distributions are shown for illustrative purposes.

With an introduction of a change-of-variable, \( x = \nu/\nu_c \), and integrating with sufficiently large limits allows the integral to be treated as approximately constant. The resultant expression for \( P_{\text{tot}}(\nu) \) is then

\[ P_{\text{tot}}(\nu) \propto \nu^{-(p-1)/2}, \]  

from which we define the spectral index, \( \alpha = -(p - 1)/2 \). In the literature the spectral index is sometimes defined with the opposite sign and for this work we use the convention \( S_\nu \propto \nu^\alpha \), where \( S_\nu \) is the flux density per unit frequency. Fig. i.1 shows two example spectral energy distributions (SEDs) with associated spectral indices.

For a more complete derivation, see the aforementioned Rybicki and Lightman (2004) or e.g. Pacholczyk (1970), Jackson (1975), and Longair (1994). An important observed property of synchrotron radiation is the high-frequency intensity fall-off. This occurs due to higher energy—hence emitting at higher frequency—electrons losing energy more quickly than those at lower frequencies (see e.g. Scheuer and Williams, 1968). This is known as spectral ageing. It is this phenomenon that gives low-frequency telescopes an advantage in detecting radio emission. For most radio telescopes this comes at the cost of resolution or sensitivity.
Figure i.2: Examples of radio emission from galaxies. *Left:* The inner lobes of Centaurus A. The background image is a three-colour image using the Digitized Sky Survey (DSS2) bands, with 150 MHz radio contours from the TFIR GMRT \(^1\) Sky Survey Alternate Data Release 1 (TGSS ADR1; Intema et al., 2016) overlaid. *Right:* The star-forming spiral galaxy Messier 83. The background image is as in the left panel, however the radio contours here are at 1.4 GHz from the NRAO VLA \(^2\) Sky Survey (NVSS; Condon et al., 1998). Figures in this section use survey data that will be expanded upon in §i.2.2.

§i.1.2. Radio galaxies

When looking at radio images, distant radio galaxies make up the vast majority of sources seen. This is true whether the source is extended or if it is simply a point the size of the synthesized beam of the radio telescope used. A radio galaxy is typically an elliptical galaxy with an AGN. This AGN is hiding a monster within—usually a super-massive black hole (SMBH) that is the primary cause of the radio emission seen. The emission from the SMBH is likely from accreting matter falling into the black hole, with a transfer of gravitational potential energy to radiation of electromagnetic waves. Spiral and lenticular galaxies do not typically show such AGN with emission beyond a few pc, and particularly loud AGN-hosting disk galaxies are seen in only a handful of examples (Centaurus A, the left panel of Fig. i.2 is one such example of a lenticular galaxy hosting a radio-loud AGN). Perpendicular to the rotation axis of the SMBH, a magnetic field is often found, and along these magnetic fields electrons travel at relativistic velocities. This results in synchrotron radiation, as the electron is accelerated in a helical path along the magnetic field lines. In a radio image of such a galaxy seen perpendicular to these magnetic fields, collimated jets of synchrotron emission can be seen as in the left panel of Fig. i.2. These jets can extended up and beyond 1 Mpc, though the larger

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\(^1\)Tata Institute of Fundamental Research Giant Metrewave Radio Telescope

\(^2\)National Radio Astronomy Observatory Very Large Array
sized jets are typically only seen in under-dense locations and thus will be found either on their own or with a partner or small group, but only rarely seen in large groups or clusters (see e.g. Saripalli et al., 2005). Hotspots of new, fresh electrons (and relatively young or flat spectra) are often seen at the ends of radio lobes, and lobe structures may also feature smaller, inner lobes such as those pictures in the left panel of Fig. i.2 of Centaurus A.

However, radio galaxies with jets are a common occurrence within dense media (e.g. within clusters) and the medium and their motion through it can have a significant effect on their morphology. Miley et al. (1972) describe a class of radio galaxies called head-tail (HT) radio galaxies and suggest that their bent lobes are due to their motion through some medium. There has been work to explore the relationship between the morphology of radio lobes and the environment they find themselves in (see e.g. Gunn and Gott, 1972; Mao et al., 2009; Pratley et al., 2013; Dehghan et al., 2014), and to see whether such objects might act as tracers of dense media such as that within galaxy clusters.

§i.1.3. Clusters of galaxies

Galaxy clusters are the largest virialized structures in the Universe; thought to be formed hierarchically through mergers of galaxies, groups, and sub-clusters of varying sizes (Peebles, 1980), galaxy clusters are an important tool in understanding how the Universe behaves on the largest scales. The galaxy clusters themselves are primarily dark matter, diffuse gas that makes up the ICM, and the galaxies for which they are named. Clusters are found to host magnetic fields on the order 0.1–1 µG (Clarke et al., 2001; Johnston-Hollitt, 2003; Bonafede et al., 2010). The Milky Way is within the Virgo Super Cluster—a conglomeration of galaxy groups.

Figure i.3: The Coma Cluster with corresponding three-colour image. The medium-purple contours are at 1.4 GHz from the NVSS and the white are smoothed archival *Chandra* data (Obs. ID 13994, PI Sanders). The linear scale is at the redshift of the cluster.
and clusters including the Local Group (of which the Milky Way is a member), and the closest proper cluster to us, the Virgo Cluster. Fig. i.3 shows the Coma Cluster, hosting X-ray-emitting plasma and various radio galaxies. Redshift is a measure of wavelength attenuation due to cosmological expansion and peculiar motion of the astronomical object. At cosmological distances, the peculiar motion becomes negligible and redshift becomes an indicator of distance. A discussion of cosmological distance measures can be found in the summary by Hogg (1999).

Galaxy clusters host a wealth of interesting astronomical objects, including the aforementioned HT galaxies. However the purpose of this work is to investigate emission that is not associated with individual galaxies, rather that which is associated with the ICM itself. This type of emission is extended, diffuse, and is thought to be mostly synchrotron in origin. The emission is typically cluster-wide, though ranges in scale from \( \sim 100 \) kpc up to \( \sim 2 \) Mpc. The emission in question comes in two main types: radio relics, and radio haloes. They differ in a number of key ways, though have similarities that suggest the same synchrotron emission processes along with similar origins for synchrotron emitting electrons.

\[ \text{i.1.3.1. Relics} \]

Radio relics themselves come in two main types: kpc-scale *phoenices* and Mpc-scale *cluster relics*. For the remainder of this thesis, these will be referred to as phoenices and relics. Fig. i.4 demonstrates two such examples.

Phoenices trace relic synchrotron emission from ancient lobes of long-dead AGN (Komissarov and Gubanov, 1994). After the central engine of a double-lobed galaxy dies, the electrons that once radiated as they spiralled along the magnetic fields running parallel to the black hole rotation axis now radiate along the magnetic field of whatever galaxy cluster they find themselves in. Fundamentally, the synchrotron emission is no different, except that the spectra of phoenices tend to be much steeper than their radio galaxy counterpart (\( \alpha < -1.5 \); Kempner et al., 2004). This apparent steepening of the spectral index is thought to be due to turbulent re-acceleration and the compression of magnetic fields from the same turbulence in the ICM (Enßlin and Brüggen, 2002). The morphology of phoenices is typically elongated, but still roundish. This apparent shape is unsurprising given their origins as double-lobed radio sources, where the emission might look like a slightly smeared radio galaxy, representing the slow diffusion of the old lobes into the surrounding ICM. Phoenices are often found towards the centre of clusters, and it is likely these objects are the husks of centrally located ellipticals, which often host large-scale radio lobe structures. The typical scale of phoenices ranges from \( \sim 100–400 \) kpc, and beyond this size the emission can be considered as proper cluster relic emission. Beyond 400 kpc, the turbulent re-acceleration required for the steep SEDs seen is required to be on the cluster-wide scale rather than localised.

Mpc-scale relics are usually more elongated than phoenices, and are found fur-
Figure i.4: Example relics. *Left:* A radio phoenix at the centre of Abell 4038, first reported by Slee and Reynolds (1984). The background is a three-colour image from the DSS2 with 1.4 GHz radio contours from the NVSS. *Right:* The double relic system associated with Abell 3667, (see e.g. Schilizzi and McAdam, 1975; Röttgering et al., 1997; Johnston-Hollitt, 2003). The background is a three-colour image from the DSS2, with contours at 200 MHz from the GaLactic and Extragalactic All-sky MWA $^3$ survey (GLEAM; Wayth et al., 2015) overlaid. The two relics sit on opposite sides of the cluster, a little over 1 Mpc from the cluster’s centre. The linear scales in each panel are at the redshifts of the respective clusters.

These objects are thought to trace large-scale shocks through the ICM during and after massive merger events. These relics are often found to coincide with the major-merger axis, and can come in adjacent pairs known as double relics (e.g. Abell 3667; Johnston-Hollitt 2003, Abell 3376; Bagchi et al. 2006, PSZ1 G108.18-11.53; de Gasperin et al. 2015). These double relics are good observational evidence for shock–re-acceleration as the generation mechanism for the steep SEDs as the double relics are always found on opposing sides of a cluster. Both relics and phoenices exhibit strong fractional polarization which, at the largest scales, can exceed 30 per cent (see e.g Johnston-Hollitt, 2003). Due to projection effects, this can be a good way to distinguish between an intervening relic and a cluster halo, described in the next section.

§i.1.3.2. Haloes

The large-scale, centrally located, diffuse synchrotron emission found in galaxy clusters is called a halo.

Cluster haloes are centrally located within the cluster, morphologically regular, and are often found to coincide with the X-ray–emitting plasma of the ICM. Two example haloes are shown in Fig. i.5. The X-ray luminosities of clusters with known haloes range from $0.63 - 35.5 \times 10^{44}$ erg s$^{-1}$ in the 0.1–2.4 keV band,
with an average luminosity of $6.7 \times 10^{44} \text{ erg s}^{-1}$. The emission mechanism for the X-ray–emitting plasma is thermal Bremsstrahlung, where electrons experience an acceleration due to their interaction with ions in the plasma. Haloes do not normally show any significant fractional polarisation however this is likely a limitation of the resolution of current-generation radio interferometers (Govoni et al., 2013). The mechanism that generates these radio haloes is still under investigation. The primary, re-acceleration model of halo generation suggests the synchrotron emission occurs after electrons are re-accelerated through merger-driven turbulence in the magnetised ICM (see e.g. Brunetti et al., 2001; Buote, 2001; Petrosian, 2001; Petrosian and East, 2008; Cassano et al., 2012). An alternate model is that of secondary, hadronic origin (see e.g. Dennison, 1980; Dolag and Enßlin, 2000). In this secondary model, electrons are generated as secondary products of collisions between cosmic ray protons and ICM protons. Pions, a product in these proton-proton collisions, produce electrons as well as $\gamma$-rays. The electrons are subsequently accelerated by magnetic fields and emit synchrotron radiation. This model not only requires $\gamma$-ray emission from clusters, but also that all galaxy clusters host radio haloes albeit at low levels. The synchrotron emission from electrons produced through these proton-proton collisions will be significantly weaker than that seen through re-acceleration via turbulence (Blasi and Colafrancesco, 1999). So far only upper limits for $\gamma$-ray emission have been presented (Prokhorov and Churazov, 2014), and with current generation radio telescopes, the necessary sensitivity to detect haloes generated solely through the secondary model has not been reached. The primary and secondary models...
are not mutually exclusive, and there has been work to combine the two models (e.g. Brunetti and Blasi, 2005; Brunetti and Lazarian, 2011, 2016). The primary model is observationally supported by the fact that only clusters with strong X-ray emitting cores are known to have radio haloes. However radio halo detection had been biased toward those clusters hosting highly X-ray luminous plasma as these are the clusters often targeted (e.g. Giovannini et al., 1999; Venturi et al., 2007, 2008; Kale et al., 2013, 2015). Only recently have surveys been conducted to search for diffuse cluster emission without preselecting clusters based solely on their X-ray luminosities. For example, Bernardi et al. (2016) select clusters based on mass, and Shakouri et al. (2016) survey clusters over a wide range of X-ray luminosities.

§i.1.3.3. Mini-haloes

As well as cluster radio haloes, there also exists a class of diffuse emission called mini-haloes. Mini-haloes show similar properties to cluster haloes, with steep spectral indices, extended structure, and central location within clusters. However they differ observationally in two key ways: mini-haloes are always found coincident with a BCG with significant radio emission, though they are not necessarily associated with this embedded galaxy. The second differences is their observed association with dynamically relaxed clusters, indicating a lack of dynamical requirement suggested for cluster halo formation (for a recent review see Bravi et al., 2016).

§i.1.3.4. Re-acceleration mechanisms for diffuse emission

Whether haloes or relics, it is likely the mechanism responsible for the observed steep spectra and general properties is that of electron re-acceleration. Due to spectral ageing, for such steep spectra to occur there is a requirement that the electrons responsible for the emission be of great age, at least in comparison to electron populations one might find in normal radio galaxies. As these electrons are part of old populations, they must have energy injected in situ, which can be explained by re-acceleration, either through violent merger events causing large-scale shocks through the ICM or through some local ICM turbulence. Jaffe (1977) originally considered a number of possibilities for the observed steep spectrum in the Coma cluster halo. One such possibility includes electrons leaking from one or more cluster radio galaxies, though this is hindered by the long diffusion times and large scales of the cluster halo. However, it is Fermi acceleration that is likely responsible for the properties of both cluster haloes and relics.

Fermi acceleration is of two forms: first order (Fermi-I) and second order (Fermi-II); so-called due to increase in particle energies being proportional to $\beta$ and $\beta^2$ respectively (see Protheroe, 1999, and references therein). In the case of Fermi-I, we can consider the scenario of a shock front passed through the magnetised ICM which cleaves the region in two; an upstream component corresponding
to the pre-shocked ICM and a downstream component corresponding to region that the shock has passed through. Electrons are accelerated by magnetic fields in the upstream region, allowing them to pass through the shock front an into the downstream region. This produces an increase in energy proportional to the velocity of the shock. Within the downstream region, they may be accelerated again by the magnetic fields and may cross back over the shock into the upstream region, increasing the energy further. For \( k \) crossings, the energy can be shown to be

\[
E = E_0 \left(1 + \frac{\Delta E}{E}\right)^k,
\]

for \( E_0 \) the initial energy and \( \Delta E \) the energy change due to crossing the shock. Fermi-II acceleration occurs when electrons are accelerated by magnetic clouds of compressed ICM after or during turbulent events. The energy gain is small as energy gain is almost equal to energy loss—electrons colliding with magnetised clouds with velocities in the same directions lose energy whereas those that collide head-on gain energy. The overall energy gain is proportional to \( \beta^2 \), and since \( \beta < 1 \) energy is always less than in Fermi-I acceleration. Fermi acceleration of both orders have been shown via simulations (see Miniati et al., 2001) to be consistent with observations.

Whilst Fermi acceleration (of both types) does well to explain the emission and spectra seen in haloes and relics, radio phoenices may be explained by a different mechanism—adiabatic compression of the magnetic field resulting in the boost to the energy of the ageing electron populations (Enßlin and Gopal-Krishna, 2001). This process revives radio plasma once associated with a long-dead AGN, where the central engine has shut off, and the lobes—now a radio plasma of electrons and magnetic fields—have diffused into the surrounding ICM, eventually having settled to a point where the diffuse pressure balances the pressure exerted by ICM. The radio plasma comprises of magnetic fields and electrons which, in the presence of a shock or turbulence within the ICM, can be compressed adiabatically.

### §i.2. Radio instruments and surveys at multiple wavelengths

#### §i.2.1. Australian radio telescopes

This work makes heavy use of radio data from two prominent Australian telescopes: the Murchison Widefield Array (MWA; Tingay et al., 2013; Bowman et al., 2013) and the Australia Telescope Compact Array (ATCA; Frater et al., 1992). The following section briefly describes these two instruments.
§ii.2.1.1. The Murchison Widefield Array

The MWA is an array consisting of 128 individual aperture arrays called tiles. The MWA is situated within the Murchison Radio-astronomy Observatory (MRO), which is operated by CSIRO\textsuperscript{4}. The MRO lies in an isolated region of Western Australia and has very little radio frequency interference (RFI); other Australian telescopes such as the Australia Square Kilometre Array Pathfinder (ASKAP) also make use of this site for the same reason. In this work, we make use of a deep, $45^\circ \times 45^\circ$ image created for use in the study of the Epoch of Reionization (EoR0). This image will be briefly described in §ii.1.1 and is described in detail in Offringa et al. (2016).

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure_i6.png}
\caption{Number of baselines greater than a given baseline length for the MWA. Inset: As before but for baselines $\leq 60$ m (see Lenc et al., 2016).}
\end{figure}

The 128 tiles of the MWA perform radio imaging at frequency ranges from 72–300 MHz. The tiles are arranged in groups of 8, with a receiver connected to each group. The tiles are spaced to attempt to provide smooth $uv$ coverage, which is provided by an $r^{-2}$ radial distribution for the central region, with extra tiles being placed at larger distances. The minimum baseline, or separation of tiles, is 7.7 m, and the maximum is $\sim$3 km. This minimum baseline, as well as number of smaller baselines, provides good sensitivity to extended, diffuse structures. Fig. i.6 shows the number of baselines available greater than a given baseline length with an inset showing the baselines less than 60 m. The largest baseline provides a limit on the angular resolution, as well as the sensitivity to compact structures.

\textsuperscript{4}Commonwealth Scientific and Industrial Research Organisation
§i.2.1.2. The Australia Telescope Compact Array

The ATCA is a six-antenna Earth rotation aperture synthesis array operated as part of the Australia Telescope National Facility (ATNF) and is located near Narrabri, ∼550 km from Sydney, at the Paul Wild Observatory. The six antennas are 22 m in diameter each, and have a maximum spacing of 6 km and minimum spacing of 31 m. These spacings allow sensitivity to radio sources that have both extended and reasonably compact structures. The telescope can operate at various frequency bands, between 1.1–105 GHz.

Five of the six antenna stations move along tracks, which allows for variability in the baselines used for observing. The sixth antenna sits on fixed station 3 km from the fifth, which gives the maximum baseline of the ATCA. Radio images are formed from visibilities, which are correlated signals between pairs of elements of an antenna. To get good sky coverage and sensitivity on the maximum number of spatial scales, the telescope must be allowed to observe for a full 12-hour rotation of the Earth and over a number of the available antenna configurations. Data-reduction and observing strategies for the 1.1–3.1 GHz band are presented in §iii.1.3, and this band is used for a follow-up observation of a peculiar radio source found during the work of §ii.

§i.2.2. Survey science

Beyond the two radio telescopes described in §i.2.1, survey data has been utilised in this work. In this section, we briefly detail the various sky-surveys, at various wavelengths, that have been used as part of this research.

§i.2.2.1. Radio surveys

At radio wavelengths, there are four main sky surveys that are used in this work. Firstly, the NVSS (Condon et al., 1998) at 1.4 GHz which covers the entire northern sky down to declinations of −40 degrees. The NVSS has a resolution of 45 arcsec by 45 arcsec and has an average rms noise of approximately 0.45 mJy beam$^{-1}$. Recently the TGSS (ADR1; Intema et al., 2016) at 147.5 MHz was released as a low-frequency counterpart to the NVSS. The TGSS covers the northern sky and continues its coverage down to declinations of approximately −53 degrees. The TGSS has an average rms of approximately 3.5 mJy beam$^{-1}$ though is not so sensitive to some diffuse emission as the higher resolution of approximately 25 arcsec by 25 arcsec resolves out flux from extended emission. The southern counterpart to the NVSS is the Sydney University Molonglo Sky Survey (SUMSS; Bock et al., 1999; Mauch et al., 2003) at 843 MHz and covers the southern sky up to a declination of −30 degrees. The resolution is equivalent to the NVSS, and its rms is approximately 2–4 mJy beam$^{-1}$ depending on the particular field and if there are any particularly bright and confusing sources nearby. Finally, there is the VLA Low-frequency Sky Survey redux (VLSSr; Lane et al., 2014) at 74 MHz which is
another northern survey, extending down to −30 degrees. When comparing to
the 6C (Hales et al., 1991) and 8C (Rees, 1990) surveys Lane et al. find that
the VLSSr has up to a 30 per cent discrepancy in its flux scale for sources below 1 Jy,
and so is only used in this work when that is not the case. The average rms for
the VLSSr is approximately 100 mJy beam$^{-1}$ and its resolution is 75 arcsec by 75
arcsec.

Those four surveys present the majority of the auxiliary data used in this work.
During the course of this research, the GLEAM survey (Wayth et al., 2015) was
released which covers the frequency range 72–231 MHz. This range is broken up
into twenty 7.5 MHz sub-bands, as well as a single 60 MHz band centred on 200
MHz and three 30 MHz bands centred on 88, 118, and 154 MHz. The coverage
of GLEAM is from approximately +25 degrees and includes the entire southern
sky. The rms varies between the sub-bands, but ranges from approximately 12–
70 mJy beam$^{-1}$ for the highest and lowest bands respectively. GLEAM is a useful
counterpart to the aforementioned surveys, though is not used for research detailed
in §ii as there is a larger study of diffuse cluster emission detected with GLEAM
being prepared by Johnston-Hollitt et al. The GLEAM survey is used in §iii for
follow-up work.

§i.2.2.2. Other surveys and archival data

The research makes heavy use, however qualitatively, of the Digitized Sky Survey
(DSS2) images. The DSS2 is an all-sky survey in the red, blue, and near-infrared
bands of the Oschin Schmidt Telescope on Palomar Mountain and the UK Schmidt
Telescope at the Anglo-Australian Observatory. Each telescope covers the northern
and southern portions of the survey respectively. For the purpose of this work, the
DSS2 is used to optically identify potential host galaxies and to visually confirm
the centres of clusters. The RÖentgen SATellite (ROSAT; Trümper, 1984) All-Sky
Survey (RASS; Voges et al., 1999) is also used as a quick method of checking for
significant soft-band X-ray emission near clusters, though no results from RASS
are presented in this work. Archival Chandra data with the Advanced CCD Imaging
Spectrometer (ACIS) instrument and XMM-Newton data with the European
Photon Imaging Camera (EPIC) instrument are used where available for similar
reasons, and in a select few clusters we utilise deep (> 30 ks exposure) X-ray im-
ages from the Representative XMM-Newton Cluster Structure Survey (REXCESS;
Böhringer et al., 2007; Pratt et al., 2009) which have been reduced by Dr. Gabriel
Pratt. Additionally, Dr. Gabriel Pratt has reduced archival XMM-Newton which
is used in §ii. Finally, we make use of AllWISE results of the Widefield Infrared
Survey Explorer (WISE; Wright et al., 2010; Mainzer et al., 2011) which covers
the sky in mid-infrared with bands at 3.4, 4.6, 12, and 22 µm. These data are used
in §iii within the context of star-formation from a curious galaxy.
§ii. Diffuse cluster emission within the EoR0 field

The primary goal of this work has been the search for diffuse cluster emission—relics and haloes. These objects are of interest as they trace cluster merger events. These events are important in understanding the way in which the Universe evolves through large-scale structure formation. Due to the steep spectral indices of such diffuse emission, low-frequency radio observations are more likely to be successful in detection, and in particular the MWA provides a useful tool to commence such a search. We are able to detect new haloes, relics, phoenices, and further re-observe previously detected emission and provide new measurements of these sources. Finally, we are able to explore cluster haloes within the context of scaling relations between halo properties and cluster properties.

§ii.1. The search for diffuse cluster emission

§ii.1.1. The Epoch of Reionization 0-hour field

The cosmological Epoch of Reionization (EoR) is thought to be traced by the redshifted neutral hydrogen (H\textsubscript{i}) 21-cm line occurring somewhere in the vicinity of 50–200 MHz. A method used to attempt to detect this signal is using an interferometric telescope, such as the GMRT EoR experiment (Paciga et al., 2013), the LOFAR \textsuperscript{1} EoR project (Yatawatta et al., 2013), the MWA EoR project (Bowman et al., 2013; Offringa et al., 2016), and PAPER \textsuperscript{2} (Ali et al., 2015).

As part of the MWA EoR project Offringa et al. present a 45°× 45° image centred on (α\textsubscript{2000}, δ\textsubscript{2000}) = (00.00°, −27.00°), at a frequency of 168 MHz called the EoR0 field. This field is shown in Fig. ii.1. The image is obtained from 45 hours of integration and has a resolution of ∼2.3 arcmin. The EoR0 field is the deepest, confusion limited image made with the MWA. As mentioned in §i.2.1.1, the large number of short (≤ 60 m) baselines makes the MWA a powerful tool to investigate extended, diffuse emission, as the shorter baselines of an interferometric telescope provide sensitivity to large-scale structure. Data collection, reduction, and imaging for the field used here is explained in detail in Offringa et al. Whilst the primary purpose of the EoR0 field is the study of EoR, the image itself is incredibly sensitive, reaching near the centre of the image down to ∼2.3 mJy beam\textsuperscript{−1} and increasing out towards the edges and in particular corners up to ∼100 mJy beam\textsuperscript{−1}. This surface brightness sensitivity makes the EoR0 field useful in the search for steep spectrum cluster haloes and relics. The R.A. and decl. range used here is

\textsuperscript{1}Low-Frequency Array

\textsuperscript{2}Precision Array for Probing the Epoch of Reionization
Figure ii.1: The central $\sim42^\circ$ of the Epoch of Reionization 0-hour field. Overlaid are the positions of galaxy clusters from the Abell catalogues (Abell et al., 1989), Meta-Catalogue of X-ray detected Clusters of galaxies (MCXC; Piffaretti et al., 2011), and the *Planck* catalogue of Sunyaev–Zel’dovich sources (PSZ1; Planck Collaboration et al., 2015a). We cut the sample of clusters to attempt to avoid the edges of the image where the noise is highest. The filled circles are coloured according to their redshift, and unfilled circles are those without a measured redshift. The sample of clusters is described in §ii.1.2. Note the side-lobe structure of the primary beam appearing in the corners of the image. The colourmap of the redshift distribution is an implementation of *cubehelix* (Green, 2011). This colourmap is used in various places throughout this work.
as follows: $(337.48^\circ \leq \alpha_{\text{J2000}} \leq 22.49^\circ)$ and $(-44.69^\circ \leq \delta_{\text{J2000}} \leq -0.61^\circ)$, which is chosen to cut out the most significant noise in the corners and edges of the image.

§ii.1.2. Catalogues of galaxy clusters

Within the EoR0 field we searched for diffuse emission within a $\sim 2$ Mpc radius around clusters within the following catalogues: Abell revised North, South, and Supplementary (Abell et al., 1989, hereafter ACO) catalogues with 5250 clusters; the Meta-Catalogue of X-ray detected Clusters of galaxies (Piffaretti et al., 2011, hereafter MCXC), with 1743 clusters; the Planck catalogue of Sunyaev–Zel’dovich sources (Planck Collaboration et al., 2015a, hereafter PSZ1) with 1227 clusters. The three catalogues differ in how clusters were detected. For the ACO catalogue, clusters were detected by eye from optical plates. For the MCXC, Piffaretti et al. (2011) compiled and homogenised a collection of X-ray detected clusters from a number of individual catalogues. One of the main purposes of this collection was to remove duplicate entries for the same clusters, but also to actually distinguish between cluster X-ray sources and other extragalactic X-ray sources. The resulting catalogue is therefore not only accurate in its definition of a cluster, but also has accompanying cluster properties, such as redshift and X-ray luminosity. PSZ1 is a catalogue of clusters created from Sunyaev–Zel’dovich (SZ; Sunyaev and Zeldovich, 1970) measurements, where SZ is the effect of the ICM on CMB photons which provide a tell-tale sign of large mass concentrations, hence clusters. Between the three catalogues there is significant overlap, but within the region encompassed by the EoR0 field, and excluding those clusters that lie too far to the edge of the image, this constitutes 668 unique clusters, 505 unique to ACO, 70 unique to MCXC, and 19 unique to PSZ1, with 24 clusters present in all three catalogues.

All clusters are checked systematically for diffuse cluster emission except 217 clusters in the ACO catalogue without a redshift. For clusters without a redshift we are unable to determine the projected linear distance from the cluster centre, which makes determining if emission is part of the cluster difficult if not at the centre. Whilst this does not pose much problem for haloes, we also consider that ACO clusters without a redshift are unlikely to have auxiliary data in the form of cluster mass, X-ray luminosities, or information on cluster members. We do note, however, that a subset of the PSZ1 cluster do not have a measured redshift though they are searched regardless as they have auxiliary measured properties. Further, cluster emission serendipitously found in clusters not part of the aforementioned catalogues is investigated when noticed.
§ii.1.3. Source detection and measurement

§ii.1.3.1. Manual source-finding: eyeballing galaxy clusters

While source-finding algorithms exist and are put to good use to produce point-source catalogues, automated source-finding can miss the extended, low surface brightness haloes and relics within clusters. Therefore the EoR0 field is searched by eye for diffuse emission. We use auxiliary data in the form of sky surveys, which are described in §i.2.2, however we do not use the GLEAM survey here as the results of a GLEAM diffuse emission search will be published elsewhere. Table ii.1 summarises the surveys used, comparing properties to the EoR0 field.

To determine the nature of detected emission, we look for the following:

(i.) high-frequency counterparts (1.4 GHz and 843 MHz),
(ii.) low-frequency counterparts (147.5 and 74 MHz),
(iii.) optical identifications, and
(iv.) X-ray emission coincident with centrally located radio emission.

(i) and (ii) are used as an easy method of checking if we are looking at blended point sources. (i) gives a quick insight into the spectral index of the source. With significant high frequency emission, at least comparably to 168 MHz, a flat spectral index is present which is very uncharacteristic of diffuse cluster emission. (iii) is important as cluster haloes and relics are not associated with an optically visible galaxy, though in the case of cluster haloes there is expected to be a concentration of optically visible galaxies as the halo should be centrally located. If an optically visible galaxy is found at the peak of the diffuse emission or between two lobes, then the likelihood is that of extended, disturbed, or otherwise normal lobes of a radio galaxy. (iv) allows us to confidently classify centrally located diffuse emission as a cluster halo or relic. In particular, Chandra or XMM-Newton observations are detailed enough to provide the position and any elongation of the X-ray emission relative to any centrally located diffuse radio emission. With these points forming the foundations of our search, we eyeballed the subset of clusters described in §ii.1.2 and noted emission that would fall into the category of either halo or relic. Once these objects are found, we wish to look at their spectral properties, including their integrated flux densities over the entire surface of the emission and the associated

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**Table ii.1:** Existing sky surveys used as auxiliary data to the EoR0 field.

<table>
<thead>
<tr>
<th>Survey</th>
<th>Frequency (MHz)</th>
<th>Declination (J2000, °)</th>
<th>Resolution (″×″)</th>
<th>$\sigma_{\text{rms}}$ (mJy beam$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>EoR0</td>
<td>168</td>
<td>$-44.69 \leq \delta \leq -08.61$</td>
<td>$138 \times 138$</td>
<td>$\gtrsim 2.3$</td>
</tr>
<tr>
<td>NVSS</td>
<td>1400</td>
<td>$\geq -40$</td>
<td>$45 \times 45$</td>
<td>$\sim 0.45$</td>
</tr>
<tr>
<td>SUMSS</td>
<td>843</td>
<td>$\leq -30$</td>
<td>$45 \times 45/\sin(\delta)$</td>
<td>$\gtrsim 2$</td>
</tr>
<tr>
<td>TGSS</td>
<td>147.5</td>
<td>$\gtrsim -53$</td>
<td>$25 \times 25/\cos(\delta - 19)$</td>
<td>$\sim 3.5$</td>
</tr>
<tr>
<td>VLSSr</td>
<td>74</td>
<td>$\geq -30$</td>
<td>$75 \times 75$</td>
<td>$\gtrsim 100$</td>
</tr>
</tbody>
</table>

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spectral energy distributions (SED) and spectral indices.

§ii.1.3.2. Noise and flux densities

The EoR0 field is a large image that has greatly varying rms noise throughout. The corners of the image feature heavy noise due to the primary beam null. Offringa et al. (2016) use BANE\(^3\), a tool that is packaged with the source-finding software, AEGEAN (Hancock et al., 2012), to estimate noise throughout the EoR0 field. The mean noise level is calculated to be \(3.2 \pm 0.6\) mJy beam\(^{-1}\) for the central 10° of the image. Large-scale diffuse structure of Galactic origin is seen streaking the image which leads to higher rms noise, however in regions with no Galactic emission the rms can be seen to be as low as \(~2\) mJy beam\(^{-1}\).

It is also vital to carefully estimate local noise in any ancillary data used at the position of any emission as we are looking at objects that often have emission at or barely above the \(3\sigma_{\text{rms}}\) level at 168 MHz. Table ii.1 gives the lower estimate of the rms for each of the surveys, however this varies significantly over the EoR0 field. For the NVSS and TGSS surveys, to obtain local rms values we simply consult the catalogues (Condon et al., 1998; Intema et al., 2016, respectively) and use the local rms noise of the nearest catalogue source. In the case of SUMSS, since no local rms is given in its catalogue (Murphy et al., 2007), we inspect each image and give an estimate of the rms which is usually on the order of \(2–4\) mJy beam\(^{-1}\), depending quite strongly on whether there is a bright source in the field creating significant imaging artefacts. For the VLSSr images, we use \(100–500\) mJy beam\(^{-1}\), again depending on the individual images.

The EoR0 field does not have a well-defined synthesized beam, which means that integrated flux densities across the field will be inconsistent with other radio data, and we find that the integrated flux density measurements of the EoR0 field differed by a systematic factor of approximately 30 per cent when compared to the nearly equivalent 162–170 MHz band in the recently released GLEAM survey. Fig. ii.2 shows this discrepancy. Sources are measured with AEGEAN on both the EoR0 field and the 162-170 MHz band, within a 5 degree region at the centre of the EoR0 field. Only sources that fit the following criteria are compared:

(i.) \(0.1 \leq S_\nu \leq 10\) Jy,
(ii.) \((ab)/(B_{\text{maj}}B_{\text{min}}) < 1.5\),
(iii.) sources in each image are within 5 arcsec of each other,

where \(a\) and \(b\) are the semi-major and semi-minor axes of the fitted ellipses, and \(B_{\text{maj}}, B_{\text{min}}\) are the FWHM of the synthesized beam. Uncertainties are only applied to the flux densities in the 162–170 MHz GLEAM band, and are the quadrature sum of all uncertainties applicable—i.e. the uncertainty in the fitting by AEGEAN and the flux density scale uncertainties inherent to GLEAM and the EoR0 field. The fitting is a weighted least-squares fit, with resulting equation, however we do not use this scale for calibration.

\(^3\text{https://github.com/PaulHancock/Aegean/wiki/BANE}\)
Flux density differences for sources between 0.1 and 10 Jy in a 5 degree region of the EoR0 field, comparing with the 162–170 MHz band of GLEAM. The dashed line is a weighted least-squares fit to the data, and the solid line is the expected 1:1 fit. Note that uncertainties in the y direction are the quadrature sum of all applicable uncertainties in the data. Note that the selection criteria included sources up to 10 Jy but no sources were found above 3.5 Jy in this central region.

To scale the integrated flux densities in the EoR0 field we choose six reasonably bright (2–6 Jy) unresolved sources, exhibiting no side-lobe structure and no blending with nearby sources. All six sources show no deviation from a simple power law between 72–231 MHz. Fig. ii.3 shows the six calibrators with predicted 168 MHz flux density against measured flux density. From the resultant fit we find a factor 0.690 ± 0.051 to be used for calibration of measured integrated flux densities, and this calibration is used through the remainder of this paper.

Flux densities of sources are either calculated by purpose-built PYTHON code\footnote{See Appendix A for details.} or simply using AEIGEAN if sources are blended, as the aforementioned PYTHON code does not fit sources, and assumes each source is discrete. We do not use AEIGEAN for all sources as AEIGEAN is intended as a point-source–finder, and will give the best results measuring such sources. Each flux measurement has an uncertainty, $\sigma_{S_{\nu}}$, calculated as

$$\sigma_{S_{\nu}} = \sqrt{(0.05 \times S_{\nu})^2 + (0.051 \times S_{\nu})^2 + \left(\sigma_{\text{rms}} \sqrt{N_{\text{beam}}}\right)^2} \ [\text{Jy}],$$

where $N_{\text{beam}}$ is the number of beams crossing the extended source. The first term in Eq. ii.1 is an additional uncertainty added due to flux density scaling in the

\[\text{GLEAM flux density, } S_{162-170} \text{ [Jy]} = 0.66(\pm 0.011) \times S_{168} - 0.001(\pm 0.006)\]
Figure ii.3: Flux densities as measured within the original EoR0 field for the six calibrators, along with their predicted 168 MHz flux density after calculating a spectral index across the GLEAM bands. The dashed line is a weighted least-squares fit to the data, and uncertainties are as in Fig. ii.2.

EoR0 field as described in §4.1 of Offringa et al. (2016), the second term is the additional uncertainty in rescaling the integrated flux density measurements, and the third term is a standard error given to flux density measurements of extended sources.

§ii.1.3.3. Spectral indices and source sizes

Spectral indices of sources are calculated in one of two ways, depending on the number of available measurements. The first method involves approximating a straight line between two flux density measurements at different frequencies, e.g. 168 and 1400 MHz, which gives an estimation of the spectral characteristics in that frequency range. A more robust method requires measurements at more than two frequencies. In these cases the spectral index is estimated by weighted least squares fitting to the flux and frequency data in logarithm space, hence fitting a power law to the spectra. We follow fitting recipes present in Hogg et al. (2010), and extend these to be unbiased in estimating the uncertainty in the fitting parameters (see Wolberg, 2006, pp. 50–51 and references therein). While the spectral energy distribution of many astronomical sources (see e.g. Jaffe and Perola 1973, Tribble 1993, Callingham et al. 2017) are not typically well described by a simple power law, over the frequency range here (74–1400 MHz) haloes and relics tend not to show any turnovers or breaks typically do not deviate from the assumed power law.
except in rare instances (e.g. the relic in Abell 2443 which has a break near 325 MHz reported by Cohen and Clarke, 2011).

In parts of this work we estimate limits to flux densities where no flux, above the rms noise, is seen in an image. In particular, we use this for estimating 1.4 GHz and 147.5 MHz limits when 168 MHz emission has no counterpart in the NVSS or TGSS survey images, respectively. These are used then to impose limits on the spectral indices. For such sources, we estimate the source area at 168 MHz, which is a function of the MWA beam at $B_{\text{maj}} \approx 2.3$ arcmin, and attempt to correct for the difference in beam sizes between the VLA (NVSS), GMRT (TGSS), and MWA (EoR0) by naively taking the ratios of $B_{\text{maj}}$ and correcting the area based on this ratio. The limit is then

$$S_{\text{limit}} = \sigma_{\text{rms}} f A_{168} \times \frac{4\ln 2}{\pi B_{\text{maj}} B_{\text{min}}} \text{ [Jy]},$$

(ii.2)

where $f = B_{\text{maj}}/B_{\text{maj,168}}$ and $A_{168}$ is the source area measured at 168 MHz.

The in-house PYTHON code used also calculates the largest angular scale (LAS) of a source by comparing the angular separation between boundary pixels of a source. This is only possible for sources that are discrete and show no blending. For such sources, we estimate an angular size by making an assumption on how far the diffuse source blends into any nearby point sources. The size characterisation is important to determine if the detection is truly extended. For a non-blended source to be considered extended in this work it must have an LAS that is greater than $1.5B_{\text{maj}}$, where $B_{\text{maj}} \approx 2.3$ arcmin, which is approximately the expected $B_{\text{maj}}$ of the EoR0 field.
§ii.2. Results from the EoR0 field

§ii.2.1. Diffuse cluster emission at 168 MHz

Here we present the diffuse emission detected in the EoR0 field from the ACO, PSZ1 and MCXC catalogues. We detect 34 objects of interest, of which 29 are likely relics, phoenices, or haloes associated with 25 clusters. We find clusters lie within the mass range $1 \times 10^{14} \, M_{\odot} < M_{500} < 12 \times 10^{14} \, M_{\odot}$ for those with measured masses, though those without measured masses may lie below this range, but not likely above it. The detection rate for such emission within the EoR0 field is $\sim 6.4$ per cent, which on average is lower than previous surveys, (e.g. $\sim 32$ per cent: Venturi et al. 2007, 2008, $\sim 17$ per cent: Bernardi et al. 2016, $\sim 12$ per cent: Shakouri et al. 2016), however as mentioned, previous surveys target the most massive, and X-ray luminous clusters. Included are previously detected relics in Abell 0013, Abell 0085, and Abell 2744 (Slee and Reynolds, 1984; Slee et al., 2001; Govoni et al., 2001), phoenices in Abell 0133 and Abell 4038 (Slee and Reynolds, 1984; Slee and Roy, 1998; Slee et al., 2001), haloes in Abell 2744 and MACS J2243.3-0935 (Govoni et al., 2001; Cantwell et al., 2016), as well as the large, ambiguous emission seen in Abell 0133 (Randall et al., 2010). Included are also 5 radio galaxies on first pass thought to be possible relic, phoenix, or halo candidates. For the purpose of distinguishing between relics and phoenices, we place a limit of 400 kpc as a maximum size of phoenix. Where emission scale approaches this size we look at the spectral index and location, where a linear size approaching 400 kpc with ultra-steep spectral indices ($\alpha < -1.5$, Kempner et al. 2004) and a location closer to the cluster’s centre would be suggestive of phoenices rather than relics. Table ii.2 summarises the results of the diffuse emission search. Following this, §ii.2.2 describes each cluster along with the diffuse emission detected within it. Images featuring optical backgrounds are three-colour images with red, green, and blue corresponding to infrared, red, and blue respectively, using data from the DSS2, unless otherwise stated in the corresponding caption. For this section, a flat $\Lambda$CDM cosmology is adopted with $H_0 = 68 \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_{\Lambda} = 0.7$, used to convert angular scales to linear with a given redshift. Note that for all radio, X-ray, and optical images in this work: north is up and east is left unless otherwise stated.
<table>
<thead>
<tr>
<th>Cluster</th>
<th>Redshift</th>
<th>Type</th>
<th>R.A. decl.</th>
<th>S168</th>
<th>$\alpha$</th>
<th>LAS</th>
<th>LLS</th>
<th>Det. threshold</th>
</tr>
</thead>
<tbody>
<tr>
<td>Abell 0013</td>
<td>0.094</td>
<td>R</td>
<td>003.37</td>
<td>-19.50</td>
<td>1850 ± 132</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Abell 0022</td>
<td>0.142</td>
<td>cH or cR</td>
<td>005.16</td>
<td>-25.66</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Abell 0033</td>
<td>0.234</td>
<td>RG or R</td>
<td>006.89</td>
<td>-19.54</td>
<td>25.5 ± 4.6</td>
<td>-8.1(±1.4) ≤ $\alpha_{168}^{1.4}$ ≤ -0.44(0.09)</td>
<td>6.7</td>
<td>1570 b</td>
</tr>
<tr>
<td>Abell 0085</td>
<td>0.055</td>
<td>R</td>
<td>010.38</td>
<td>-09.37</td>
<td>9385 ± 957</td>
<td>$\alpha_{100}^{147.5}$ = -1.85 ± 0.03</td>
<td>7.1</td>
<td>470</td>
</tr>
<tr>
<td>Abell 0122</td>
<td>0.114</td>
<td>RG</td>
<td>014.35</td>
<td>-26.29</td>
<td>329 ± 25</td>
<td>$\alpha_{168}^{1.4}$ ≤ -1.52 ± 0.04</td>
<td>4.9</td>
<td>620</td>
</tr>
<tr>
<td>Abell 0133</td>
<td>0.057</td>
<td>P</td>
<td>015.67</td>
<td>-21.87</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Abell 0141</td>
<td>0.161</td>
<td>H</td>
<td>016.39</td>
<td>-24.64</td>
<td>110 ± 11</td>
<td>$\alpha_{168}^{1.4}$ ≤ -0.98 ± 0.05</td>
<td>5.51</td>
<td>1250</td>
</tr>
<tr>
<td>Abell 2496</td>
<td>0.122</td>
<td>U</td>
<td>342.72</td>
<td>-16.45</td>
<td>561 ± 42</td>
<td>$\alpha_{14}^{1.4}$ - 1.26 ± 0.02</td>
<td>~4.8</td>
<td>~650</td>
</tr>
<tr>
<td>Abell 2556</td>
<td>0.087</td>
<td>cP</td>
<td>348.30</td>
<td>-21.47</td>
<td>29.3 ± 5.5</td>
<td>$\alpha_{168}^{1.4}$ - 1.22 ± 0.14</td>
<td>3.33</td>
<td>336</td>
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<td>Abell 2680</td>
<td>0.177</td>
<td>cH</td>
<td>059.13</td>
<td>-21.04</td>
<td>23 ± 8</td>
<td>$\alpha_{168}^{1.4}$ ≤ -1.2 ± 0.2</td>
<td>~3.2</td>
<td>~600</td>
</tr>
<tr>
<td>Abell 2693</td>
<td>0.175</td>
<td>cH</td>
<td>000.56</td>
<td>-19.55</td>
<td>49.6 ± 6.0</td>
<td>$\alpha_{168}^{1.4}$ ≤ -0.88 ± 0.06</td>
<td>3.75</td>
<td>681</td>
</tr>
<tr>
<td>Abell 2721</td>
<td>0.114</td>
<td>cR</td>
<td>001.56</td>
<td>-34.73</td>
<td>53.5 ± 13.6</td>
<td>$\alpha_{168}^{1.4}$ ≤ -0.96 ± 0.12</td>
<td>-</td>
<td>460</td>
</tr>
<tr>
<td>Abell 2744</td>
<td>0.307</td>
<td>R</td>
<td>003.66</td>
<td>-30.39</td>
<td>550 ± 51</td>
<td>$\alpha_{168}^{1.4}$ = -1.11 ± 0.04</td>
<td>-</td>
<td>~2140</td>
</tr>
<tr>
<td>Abell 2751</td>
<td>0.107</td>
<td>R</td>
<td>004.23</td>
<td>-31.39</td>
<td>324.9 ± 61.4</td>
<td>-</td>
<td>-</td>
<td>-</td>
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<tr>
<td>APMCC 039</td>
<td>0.082</td>
<td>RG</td>
<td>004.46</td>
<td>-31.31</td>
<td>60.3 ± 7.7</td>
<td>-1.28(±0.09) ≤ $\alpha_{147.5}^{1.4}$ ≤ -0.43(±0.06)</td>
<td>8.816</td>
<td>840.8</td>
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<tr>
<td>Abell 2798</td>
<td>0.105</td>
<td>cR</td>
<td>009.41</td>
<td>-28.51</td>
<td>110.3 ± 9.4</td>
<td>$\alpha_{168}^{1.4}$ = -1.18 ± 0.08</td>
<td>4.84</td>
<td>575</td>
</tr>
<tr>
<td>Abell 2811</td>
<td>0.108</td>
<td>H</td>
<td>010.54</td>
<td>-28.53</td>
<td>80.7 ± 16.5</td>
<td>$\alpha_{168}^{1.4}$ ≤ -1.5 ± 0.1</td>
<td>~4.13</td>
<td>~502</td>
</tr>
<tr>
<td>Abell 3964</td>
<td>0.133</td>
<td>RG</td>
<td>346.17</td>
<td>-19.84</td>
<td>16.6 ± 4.3</td>
<td>-</td>
<td>2.84</td>
<td>413</td>
</tr>
<tr>
<td>Abell 4038</td>
<td>0.0282</td>
<td>P</td>
<td>356.92</td>
<td>-28.15</td>
<td>4875 ± 249</td>
<td>-</td>
<td>-</td>
<td>-</td>
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Table ii.2: *continued*

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<tr>
<th>Cluster</th>
<th>Redshift</th>
<th>Type</th>
<th>$\alpha_{J2000}$</th>
<th>Decl.$_{J2000}$</th>
<th>$S_{168}$ (mJy)</th>
<th>$\alpha_{168}$</th>
<th>LAS (arcmin)</th>
<th>LLS (kpc)</th>
<th>Det. threshold (mJy beam$^{-1}$)</th>
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</thead>
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<tr>
<td>Abell S0084</td>
<td>0.108</td>
<td>cH</td>
<td>012.33</td>
<td>$-29.51$</td>
<td>$32.3 \pm 4.5$</td>
<td>$\alpha_{168}^{cH}$ $\leq -1.3 \pm 0.1$</td>
<td>4.19</td>
<td>511</td>
<td>7</td>
</tr>
<tr>
<td>Abell S1063</td>
<td>0.348</td>
<td>RG</td>
<td>342.19</td>
<td>$-44.51$</td>
<td>$265 \pm 38$</td>
<td>$\alpha_{168}^{cR}$ $= -1.36 \pm 0.11$</td>
<td>$\sim 5.5$</td>
<td>$\sim 1670$</td>
<td>50</td>
</tr>
<tr>
<td>Abell S1099</td>
<td>0.110</td>
<td>U</td>
<td>348.27</td>
<td>$-23.14$</td>
<td>$184 \pm 20$</td>
<td>$\alpha_{168}^{cH}$ $= -1.00 \pm 0.015$</td>
<td>-</td>
<td>-</td>
<td>15</td>
</tr>
<tr>
<td>Abell S1121</td>
<td>0.358</td>
<td>H</td>
<td>351.31</td>
<td>$-41.21$</td>
<td>$154 \pm 48$</td>
<td>-</td>
<td>$\sim 4.3$</td>
<td>$\sim 1300$</td>
<td>15</td>
</tr>
<tr>
<td>Abell S1136</td>
<td>0.063</td>
<td>U</td>
<td>354.08</td>
<td>$-31.61$</td>
<td>$586 \pm 46$</td>
<td>-</td>
<td>$\sim 7.2$</td>
<td>$\sim 530$</td>
<td>10</td>
</tr>
<tr>
<td>LCRS B004346.8-393051 (core)</td>
<td>0.156</td>
<td>RG</td>
<td>359.51</td>
<td>$-22.57$</td>
<td>$34.4 \pm 16.2$</td>
<td>$\alpha_{168}^{cR}$ $= -0.696 \pm 0.218$</td>
<td>-</td>
<td>-</td>
<td>15</td>
</tr>
<tr>
<td>LCRS B004346.8-393051 (tail)</td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RXC J2351.0-1954</td>
<td></td>
<td>cH</td>
<td>357.76</td>
<td>$-19.94$</td>
<td>$87 \pm 17$</td>
<td>$\alpha_{168}^{cH}$ $\leq -1.4 \pm 0.1$</td>
<td>$\sim 2.8$</td>
<td>$\sim 670$</td>
<td>10</td>
</tr>
<tr>
<td>RXC J2351.0-1954 (A)</td>
<td>0.248</td>
<td>cR</td>
<td>357.87</td>
<td>$-19.99$</td>
<td>$56.9 \pm 8.6$</td>
<td>$\alpha_{168}^{cR}$ $\leq -1.23 \pm 0.07$</td>
<td>6.25</td>
<td>1500</td>
<td>10</td>
</tr>
<tr>
<td>RXC J2351.0-1954 (B)</td>
<td></td>
<td>cR</td>
<td>357.59</td>
<td>$-19.81$</td>
<td>$147 \pm 13$</td>
<td>$\alpha_{168}^{cH}$ $\leq -1.68 \pm 0.04$</td>
<td>5.87</td>
<td>1410</td>
<td>10</td>
</tr>
<tr>
<td>MACS J2243.3-0935 $^d$</td>
<td>0.447</td>
<td>H</td>
<td>340.86</td>
<td>$-09.59$</td>
<td>$83 \pm 36$</td>
<td>$\alpha_{168}^{cR}$ $= -1.6 \pm 0.4$</td>
<td>$\sim 2.8$</td>
<td>$\sim 1000$</td>
<td>60</td>
</tr>
<tr>
<td>WHL J235151.0-085929</td>
<td>0.394</td>
<td>cH</td>
<td>357.91</td>
<td>$-08.98$</td>
<td>$128 \pm 20$</td>
<td>$\alpha_{168}^{cH}$ $= -1.62 \pm 0.10$</td>
<td>-</td>
<td>-</td>
<td>10</td>
</tr>
</tbody>
</table>


$^b$ Assuming a redshift of $z = 0.2395$.

$^c$ Reported by Govoni et al. (2001).

$^d$ Reported by Cantwell et al. (2016).
§ii.2.2. Individual galaxy clusters

§ii.2.2.1. Abell 0013

The galaxy cluster Abell 0013 (MCXC J0013.6-1930; PSZ1 G072.48-78.46) has mass $M_{500} = 2.79^{+0.36}_{-0.38} \times 10^{14} M_\odot$ (PSZ1), a redshift of $z = 0.0940$, and X-ray luminosity $L_{500} = 1.236332 \times 10^{47}$ W (MCXC). Slee and Reynolds (1984) report the detection of a steep-spectrum radio relic after 1.465 GHz and 4.885 GHz VLA imaging. Slee et al. (2001) provide further VLA observations at 1.425 GHz and show filamentary structure in the emission. The top panel of Fig. ii.4 shows an RGB image with MWA, NVSS, and TGSS contours overlaid. The steep spectrum relic is recovered in the MWA image, labelled “A” in the figure, and extends beyond what is expected due to the difference in resolution. The flux density at 168 MHz is measured to be $S_{168} = 1.850 \pm 0.132$ Jy, with an LAS of 6.7 arcmin and largest linear scale (LLS) at the cluster’s redshift of 750 kpc. Within the NVSS catalogue the source is split into two components: NVSS J001332-193023 and NVSS J001326-192950. These sources are reported to have flux densities of $10.7 \pm 2.1$ mJy and $18.0 \pm 2.0$ mJy respectively (Condon et al., 1998). With comparison to Fig. 2 of Slee et al. (2001) we conclude that both of these NVSS sources are a single source and so add them to arrive at a flux density of $S_{1.4} = 28.7 \pm 4.1$ mJy for the emission. We calculate a spectral index between the 1.4 GHz and 168 MHz measurements as $\alpha_{1.4} = -1.96 \pm 0.08$. Such a steep spectral index, along with apparent proximity to the cluster’s core is suggestive of a radio phoenix, however at the projected size of 750 kpc this becomes too large for small-scale turbulence to re-accelerate electrons. This size is indicative of a radio relic. It is entirely possible the relic is further on the periphery, only appearing close to the centre due to projection effects. Slee et al. (2001) report the spectral index between 1.465 GHz and 1.385 GHz to be $\alpha_{1.465} = -4.4 \pm 0.4$. Due to the resolution of the these observations, it is likely the relic has not been detected in its entirety, resulting in flux being resolved out of the VLA images and resulting in an overly steep spectral index. Slee et al. provide high resolution 1.4 GHz analyses of the relic, showing the structure that is traced by the TGSS and NVSS emission as in the top panel of Fig. ii.4. They consider the possibility of the diffuse emission being old lobes of one of the optically visible cluster members near the core. They identify the most probable host as the brightest cluster galaxies (BCG) 2MASX J00133401-1929017 and 2MASX J00133853-1930007 with redshifts $z = 0.099272 \pm 0.000217$ and $z = 0.090529 \pm 0.000157$ (Quintana and Ramirez, 1995) respectively.

The bottom panel of Fig. ii.4 shows exposure corrected, smoothed XMM-Newton data (Obs. ID 0200270101, PI Ehle). The bulk of the central radio emission is offset from the main component of the X-ray plasma as well as the optical concentration of galaxies. The offset from the X-ray and optical cores suggests that the emission is not a cluster halo. In addition to the relic “A”, there is extended emission seen (marked “B” in Fig. ii.4) that has no 1.4 Hz or 147.5 MHz counterpart. The extension may be related to the nearby point-source, NVSS J001408-193218.
Figure ii.4: Abell 0013. **Top:** RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 13.2 mJy beam$^{-1}$ also increasing by a factor of 2. A factor of 2 is chosen here so that optical galaxies remain unobscured by radio contours. The dashed circle is centred on Abell 0013 with a radius of 1 Mpc. **Bottom:** *XMM-Newton* X-ray background with EoR0 field contours alongside X-ray contours.
(2MASX J00140813-1932176) with clear optical ID. However, we the extension seems to trace the optically visible subgroup and may be emission associated with it. This emission may be an example of diffuse emission tracing the accretion shock of an in-falling galaxy group. Shakouri et al. (2016) consider emission associated with the clusters RXC J0225.1-2918 and Abell S0258 as a possible example of this, though even with their polarimetry and higher resolution they are unable to confirm this and we are unable to do so here as well.

This radio relic (and cluster in general) is a good example of the power of the MWA for finding steep-spectrum sources and using higher resolution imaging to properly ascertain their nature. Without auxiliary data we run into issues of classification with the MWA alone, where we know steep-spectrum diffuse cluster emission exists but are unable to definitively classify the emission as either a halo, relic, or otherwise, without further data. Conversely, with only the high-resolution data diffuse flux is resolved out. In the case of Abell 0013, one might argue it shows characteristics of a radio phoenix in its steep spectral index and location near the centre of the cluster (unless its location is being projected onto the central region).

However, its newly detected linear size goes against this classification due to the shock and turbulence requirements now becoming cluster-wide rather than local to the emission.

§ii.2.2.2. Abell 0022

The cluster Abell 0022 (MCXC J0020.7-2542; PSZ1 G042.77-82.97) has a redshift of $z = 0.142352 \pm 0.000327$ (Pimbblet et al., 2006), mass $M_{\text{YZ},500} = 4.56^{+0.42}_{-0.44} \times 10^{14} M_{\odot}$ (PSZ1), and X-ray luminosity $L_{500} = 2.872451 \times 10^{37}$ W (MCXC). The cluster features extremely diffuse, faint emission that appears to permeate the cluster. Fig. ii.5 shows the emission extending from the centre of the cluster northward. Although we see from the NVSS and TGSS data that the MWA emission is coincident with three point sources: NVSS J002042-254239, associated with a member of the intervening galaxy triple DUKST 473-042; NVSS J002048-254437; and NVSS J002058-253957, emission associated with the cluster member 2MASX J00205811-2539516. The MWA data extends considerably further north reminiscent of the cluster halo in Abell 3888 (Shakouri et al., 2016). We do not obtain a flux density measurement for the extended emission as it blends into the emission from 2MASX J00205811-2539516, which has a flux density contribution that we are unable to subtract as there is neither significant emission seen at 1.4 GHz in the NVSS image, nor in the 147.5 MHz emission in the TGSS image.

$XMM-Newton$ data is shown in the bottom panel of Fig. ii.5 (Obs. ID 0201900301, PI Böhringer), which were taken and reduced as part of the REXCESS survey (Böhringer et al., 2007; Pratt et al., 2009). The 168 MHz radio emission extends far beyond the X-ray emission, however it is likely the bulk of the halo sits coincident with the X-ray peak, but is blending with DUKST 473-042, which has a spectroscopic redshift of $z = 0.063821 \pm 0.000500$ (Ratcliffe et al., 1998) and is seen in the centre of the field. We cannot unambiguously classify the extended emission
Figure ii.5: Faint candidate halo in Abell 0022. Top: RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 21 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster with a radius of 1 Mpc. Bottom: X-ray image from the REXCESS survey with EoR0 contours overlaid as in the top panel along with X-ray contours increasing with a factor of 2 in black.
as either a candidate halo, relic, or both. We suggest follow-up observations at a higher resolution to disentangle the point sources from the diffuse radio emission.

§ii.2.2.3. Abell 0033

![Figure ii.6: Candidate relic on the periphery of Abell 0033. The background is an RGB image with contours overlaid as follows: EoR0, white, 3σ_{rms} beginning at 6.9 mJy beam^{-1} increasing by a factor of $\sqrt{2}$ and grey, dashed, 2σ_{rms} at 4.6 mJy beam^{-1}; NVSS, red, beginning at 1.5 mJy beam^{-1} increasing by a factor of 2. No TGSS emission is seen above the 3σ_{rms} level of 25.8 mJy beam^{-1}. The dashed circle is centre on the position of Abell 0033 and the dotted circled is centred on WHL J002712.5-193045, both with radii Mpc at the reported redshifts. They are suspected to be the same cluster (see main text). The boxes indicate possible optical IDs for the diffuse emission.](image)

Fig. ii.6 shows curious emission on the periphery of both Abell 0033 ($z = 0.28$, photometric; Leir and van den Bergh 1977) and WHL J002712.5-193045 ($z = 0.2395$, spectroscopic; Wen and Han 2013). The white circles in Fig. ii.6 have 1 Mpc radii about the cluster centres. The two clusters are separated by an angular distance of $\sim 80$ arcsec, and given the clear concentration of optical galaxies seen in the DSS2 images, they are likely the same cluster and we hereafter consider there to be only Abell 0033 at the redshift of $z = 0.2395$. The grey, dashed contour in Fig. ii.6 is at the 2σ_{rms} level to indicate the possibility of the two objects, Obj. A and B, being a single piece of extended emission on the cluster periphery. If this is the case, the entire structure has a flux density of $S_{168} = 25.5 \pm 4.6$ mJy, and an LAS is 6.72 arcmin which translates to an LLS of 1570 kpc at $z = 0.2395$. 
Both the NVSS and TGSS surveys do not show significant emission within the area of the 168 MHz emission. From this we provide upper limits on the 1.4 GHz and 147.5 MHz flux densities of $S_{1.4} \leq 10 \text{ mJy}$ and $S_{147.5} \leq 73 \text{ mJy}$. This gives a limit on the spectral index between 147.5 MHz and 1.4 GHz of $-8.1(\pm 1.4) \leq \alpha \leq -0.44(\pm 0.09)$, assuming a simple power law to the SED. This range of spectral indices is consistent with either typical radio galaxies of $\alpha = -0.8$ (Condon, 1992), the steep spectrum cluster relics (e.g. de Gasperin et al., 2014), or the dying radio galaxies often found within clusters (e.g. Murgia et al., 2011). However the lower-limit covers a range that is unrealistic for known astronomical sources so is not definitive for classification purposes or useful in any way.

Upon inspection of the optical data, two possible optical IDs are found and highlighted with boxes in Fig. ii.6. There is an optically visible source reported in the USNO-A2.0 catalogue, USNO-A2.0 0675-00178746, sitting between A and B. The RGB image of Fig. ii.6 shows significant reddening of this optical source, consistent with a high redshift. The shape of the emission is then reminiscent of the lobes of a radio galaxy and the overall morphology is similar to the dead radio galaxy associated with the lenticular galaxy NGC 1534—recently discovered using the MWA (Hurley-Walker et al., 2015)—with faint lobes and steep spectral indices as ancient remnants of old episodes of AGN activity. However, Obj. A has an optically visible galaxy, GALEXASC J002737.37-192909.3, near its centre and so could be associated with it. In this case, Obj. B is unlikely to be associated with Obj. A and may be a cluster radio relic. We offer these possibilities as the origins of this emission, but cannot classify the emission definitively. Note that the LLS presented in Table ii.2 assumes Obj. A and B are a single source and associated with the cluster with a redshift of $z = 0.2395$.

§ii.2.2.4. Abell 0085

Abell 0085 (MCXC J0041.8-0918; PSZ1 G115.20-72.07) is a nearby cluster with a redshift of $z = 0.055061 \pm 0.000340$ (Oegerle and Hill, 2001), mass $M_{YZ,500} = 4.90^{+0.21}_{-0.22} \times 10^{14} \text{ M}_\odot$ (PSZ1) and X-ray luminosity $L_{500} = 5.100085 \times 10^{37} \text{ W}$ (MCXC). Slee and Reynolds (1984) report the detection of a phoenix offset from the cluster centre, and Giovannini and Feretti (2000) provide follow-up 300 MHz imaging with the VLA and ascertain an LLS for the radio phoenix of 386 kpc (corrected for this cosmology). 168 MHz emission coincides with the previously detected phoenix (labelled “A” in Fig. ii.7), and has an approximate LLS of 470 kpc. The in-house PYTHON script does not deal with blended emission. To obtain the flux density of the steep spectrum emission in Abell 0085 we use AEGET with an rms noise of 24 mJy beam$^{-1}$, seedclip of 3, and floodclip of 2. The flux density is measured to be $S_{168} = 9.385 \pm 0.957 \text{ Jy}$. 1.4 GHz emission from the NVSS traces the relic as described by Slee et al. The TGSS shows 147.5 MHz emission beyond that of the NVSS despite similar resolutions with an extended structure to the southeast, tracing the emission at 300 MHz shown by Giovannini and Feretti. This extension is also encompassed by the 168 MHz emission. We do not use
Figure ii.7: Abell 0085. Top: The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 49.7 mJy beam$^{-1}$ increasing by a factor of increasing by $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 9.6 mJy beam$^{-1}$ also increasing by factor of 2. Bottom: XMM-Newton image with EoR0 contours overlaid as in the top panel. Both panels show the linear scale at the cluster’s redshift.
the 1.4 GHz flux density from the NVSS as a large portion of the relic is undetected. Rather, we use the 147.5 MHz TGSS image and measure a flux density of $S_{147.5} = 10.21 \pm 0.07$ Jy. We use the 300 MHz measurement of $S_{300} = 2.739$ Jy (Giovannini and Feretti, 2000) though include a 10 per cent uncertainty as no uncertainty is quoted by Giovannini and Feretti. Thus, we calculate a spectral index of $\alpha_{147.5}^{300} = -1.85 \pm 0.03$, though note that the TGSS image is likely missing flux due to resolution and missing baselines, which suggests the relic may have an even steeper spectral index.

The radio source to the southeast of the relic (labelled “B” in Fig. ii.7) has extended 168 MHz emission beyond the source seen in the NVSS which is likely associated with the galaxy SDSS J004150.17-092547.4. The TGSS 147.5 MHz data shows two distinct sources within this extended, steep-spectrum emission. The bottom panel of Fig. ii.7 shows a zoomed-in view of Obj. B, with MWA contours overlaid on exposure corrected, smoothed XMM-Newton data (Obs. ID 0723802101, PI de Plaa). Obj. B features an extension to the bulk of the X-ray emitting plasma at the cluster’s core. Kempner et al. (2002) suggest that this extension of X-ray emission, along with the complex of radio sources Obj. B, is representative of subcluster asymmetrically merging with the main cluster of Abell 0085.

§ii.2.2.5. Abell 0122

Abell 0122 (MCXC J0057.4-2616), with a redshift of $z = 0.113478$ (Zaritsky et al., 2006), mass $M_{X,500} = 1.7267 \times 10^{14} M_\odot$, and X-ray luminosity $L_{500} = 0.861163 \times 10^{37}$ W (MCXC), features a strong diffuse source at its centre. This diffuse emission has a flux density of $S_{168} = 329 \pm 25$ mJy with an LAS of 4.9 arcmin. At the redshift of the cluster the emission has a projected LLS of 620 kpc. There is no significant 1.4 GHz emission seen with the NVSS survey, though the 147.5 MHz TGSS data shows extended emission. The TGSS ADR1 catalogue splits this into two distinct sources with its higher $7\sigma_{\text{rms}}$ cutoff for source detections, compared to Fig ii.8 which has TGSS contours at the $3\sigma_{\text{rms}}$ level typically necessary for faint diffuse emission detections. We provide a 1.4 GHz flux limit of $S_{1.4} \leq 13$ mJy and a corresponding spectral index of $\alpha_{168}^{1.4} \leq -1.52 \pm 0.04$.

The bottom panel of Fig: ii.8 shows exposure corrected, smoothed XMM-Newton data (Obs. ID 0504160101, PI Sivanandam). The 168 MHz radio emission fills the X-ray plasma as is typical of cluster radio haloes and the location, steep spectral index, and X-ray emission are suggestive of an ultra-steep spectrum radio halo (USSRH; see e.g. Cassano et al., 2006). However the 147.5 MHz morphology appears to suggest a tailed radio galaxy, or other radio galaxy-related origin. The tailed radio galaxy origin is somewhat hampered by the lack of optical ID coincident with the peak of the 147.5 MHz emission. The BCG, 2MASX J00572288-2616528, lies offset from the peak by approximately 10 arcsec. Given the morphology, steep spectral index, and displacement of an optical host, there exists the possibility that the emission is that of an old, dead radio galaxy, likely associated
Figure ii.8: Steep-spectrum emission at the centre of Abell 0122. Top: The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 12 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy and increasing by a factor of 2; TGSS, medium purple, beginning at 13.5 mJy also increasing by a factor of 2. The linear scale is at the cluster’s redshift. Bottom: The background image is archival XMM-Newton data with EoR0 contours as in the top panel. The dashed circle is centred on Abell 0122, and has a radius of 1 Mpc.
with the BCG. Abell 0122 shows no evidence in the either X-ray emission or the optical density that would suggest the cluster is undergoing, or had undergone, a merger event. If the turbulent re-acceleration model is correct, a halo in this cluster of this power would be unusual. Given the morphology of the source in the TGSS image, we have classified this emission as a radio galaxy, though note that there is the possibility the emission represents a mini-halo due to the morphologically relaxed nature of the X-ray plasma.

§ii. 2.2.6. Abell 0133

![Figure ii.9](image) The centre of Abell 0133. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 15 mJy beam\(^{-1}\) increasing with a factor of \(\sqrt{2}\); NVSS, red, beginning at 1.5 mJy beam\(^{-1}\) and increasing with a factor of 2; TGSS, medium purple, 13.2 mJy beam\(^{-1}\) also increasing with a factor of 2. The linear scale is at the redshift of the cluster, and Obj. A is the diffuse emission of interest.

Abell 0133 (MCXC J0102.7-2152; PSZ1 G149.55-84.16) has a redshift of \(z = 0.0562\) (Way et al., 1997), X-ray luminosity \(L_{X,500} = 1.460216 \times 10^{37} \text{ W (MCXC)}\), and mass \(M_{YZ,500} = 3.08^{+0.23}_{-0.24} \times 10^{14} \text{ M}_\odot \text{ (PSZ1)}\). The cluster has been studied extensively in X-ray (e.g. Reichert et al., 1981; Fujita et al., 2002, 2004) along with the multi-wavelength study by Randall et al. (2010) which all point towards the disturbed, dynamic nature of the the cluster. Further, steep-spectrum radio emission in the form of a radio phoenix was detected by Slee and Reynolds (1984) \(\sim 30\) arcsec from the cD, ESO 541-G013. Further high-resolution follow-up observations by Slee et al. (2001) showed filamentary structure to this phoenix. An important
result of the X-ray studies show that the X-ray–emitting gas is disturbed, with the possibility of a weak shock (Fujita et al., 2004) creating a tongue-like feature pointing to the northwest. This feature coincides with the phoenix reported by Slee and Reynolds (1984).

Fig. ii.9 shows the cluster centre with the emission of interest, with Obj. A a large, possible lobe, Obj. B the radio phoenix, and the orange square indicating the possible ID for double-lobe-like structure, along with Obj. C, an interesting knot. Randall et al. (2010) discuss the possibility of the entire structure representing a giant, background radio galaxy, with the core and host marked in Fig. ii.9. As part of this interpretation, the phoenix is thought to be a separate entity, most likely associated with the cluster. We consider an alternative explanation not covered by Randall et al. (2010) where the southern lobe A is in fact a relic. This explanation draws on deep radio observations of 1E 0657-56 (the Bullet Cluster; Liang et al., 2000, 2001; Shimwell et al., 2014, 2015; Srinivasan, 2015). Liang et al. (2000) show low resolution radio imaging of the Bullet Cluster, and further X-ray observations provide high resolution imaging to show the directionality of the shock (Markevitch, 2006) with clear diffuse emission located to the east of the west-ward X-ray shock. This piece of diffuse emission is considered a relic, created through back-shock of the massive, merging system (Shimwell et al., 2014). We consider the possibility that the extended filament between the northern B and southern A lobes in Abell 0133 is in fact of similar origin. This scenario would suggest that the southern lobe is a relic similar to the bulb portion of the relic in the Bullet Cluster. The locational difference between the possible relic in Abell 0133 and relic in the Bullet Cluster could be simple projection effects. Obj. C in Fig. ii.9 marks a knot in the filament, clear in the medium purple TGSS contours, and seen in Figure 5(d) of Randall et al. (2010). This has no optical ID so is not necessarily an unassociated point source. In the case of structure being that of a background giant radio galaxy (GRG), there is a requirement that extreme twisting of the core relative to the southern lobe must have occurred, or is in the process of occurring. Whilst such disjoint motion is seen in lobed radio galaxies (e.g. NGC 326: Fanti et al., 1977; Murgia et al., 2001), these galaxies with disturbed lobes typically reside within clusters, where the ICM plays a crucial role in shaping the jets through ram pressure as the galaxy core travels through or precesses within the medium. It may be that the structure is a GRG in a background cluster. The supposed optical host has a redshift of $z = 0.2930$ (2MASX J01024529-2154137: Owen et al., 1995; Slee et al., 2001; Randall et al., 2010), however there are no other available redshifts near 2MASX J01024529-2154137. We find that the 147.5 MHz TGSS contours in Fig. ii.9 show that the peak of this emission near the core of the GRG does not align with the proposed optical ID, marked with an orange square, though the 1.4 GHz NVSS contours do align well with 2MASX J01024529-2154137. GRGs are found independent of clusters, but the ICM is required for jets to be bent from the axis of the GRG which may be the case here.
We estimate the extent of the diffuse emission within both the relic and radio galaxy interpretations. If the emission is that of a radio galaxy, we find LAS to be 10.4 arcmin, which at $z = 0.2930$ corresponds to an LLS of 2.82 Mpc and at $z = 0.0562$ an LLS of 701 kpc. In the relic scenario, we consider the southern lobe to be a relic, and measure the east-west dimensions. The LAS is found to be 6.0 arcmin, which corresponds to an LLS of 405 kpc at the cluster’s redshift. As mentioned, the filament between the core and southern lobe would likely be part of this relic in this scenario, the size of which is difficult to estimate given any additional emission from the cD, the phoenix, as well as the intruding emission likely associated with 2MASX J01024529-2154137. We do not provide any further certainty on the nature of the emission, merely offer the alternate explanation of radio relic akin to that in the Bullet Cluster. In Table ii.2 we list the phoenix, as well as the ambiguous emission as both a relic and a radio galaxy.

§ii.2.2.7. Abell 0141

Abell 0141 (MCXC J0105.5-2439) is a distant cluster with a redshift of $z = 0.230$ (Struble and Rood, 1999). We present a hitherto undetected radio halo at its centre coinciding with the optical mass concentration. The mass and X-ray luminosity are $M_{X,500} = 4.7167 \times 10^{14} M_\odot$ and $L_{500} = 5.160525 \times 10^{37} \text{ W} \ (\text{MCXC})$. The top panel of Fig. ii.10 shows the cluster with an RGB image as a background with the 168 MHz contours overlaid to illustrate the radio halo’s location relative to the cluster.

Previous searches for diffuse radio emission in this cluster includes a search by Venturi et al. (2007) as part of the GMRT Radio Halo Survey (GRHS), in which their 610 MHz images with $1\sigma = 90 \ \mu\text{Jy beam}^{-1}$ did not detect anything resembling the emission seen at 168 MHz. The cluster had been a curiosity due to the lack of a halo as the cluster is undergoing a merger. The bottom panel of Fig. ii.10 shows the dynamic nature clearly in the bi-modality of the X-ray plasma. Further, the optical concentration of galaxies trace the two X-ray peaks and the elongation of the X-ray emission and 168 MHz radio emission. Dahle et al. (2002) comment on the ill-defined optical centre, noting that the two optical density peaks occur $\sim 2$ arcmin apart, with elongation along the north–south axis as seen in the X-ray and radio emission. Thus this new, unambiguous detection of a radio halo in Abell 0141 supports the previous findings in the literature of the association of radio haloes in merging clusters.

The radio halo is measured to have a flux density of $S_{168} = 110 \pm 11 \ \text{mJy}$ and an LAS of 5.51 arcmin, which translates to an LLS of 1.250 Mpc. This LLS puts the radio halo within the class of giant radio haloes (GRH) defined to be greater than 1000 kpc in extent. An upper limit to the 1.4 GHz flux density is estimated to be $S_{1.4} \leq 13.7 \ \text{mJy}$ which places an upper limit on the spectral index as $\alpha_{168}^{1.4} \leq -0.98 \pm 0.05$. A similar limit from the 147.5 MHz TGSS survey would suggest a spectral index $\alpha_{147.5}^{168} \geq -5.6 \pm 0.3$, though this lower limit is not useful for classification purposes.
Figure ii.10: Radio halo at the centre of Abell 0141. Top: The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam\(^{-1}\) and increasing by a factor of \(\sqrt{2}\); NVSS, red, beginning at 1.5 mJy beam\(^{-1}\) and increasing by a factor of 2; TGSS, medium purple, beginning at 13.8 mJy beam\(^{-1}\) also increasing by a factor of 2. Bottom: Exposure corrected, smoothed XMM-Newton data (Obs. ID 0693010501, PI Zhang) with EoR0 contours overlaid. In both panels the dashed circle is centred on the cluster with a 1 Mpc radius.
§ii. 2.2.8. Abell 2496

Abell 2496 (MCXC J2251.0-1624; PSZ1 G047.75-60.16) has a redshift of $z = 0.1221$, an X-ray luminosity of $L_{500} = 2.030655 \times 10^{37}$ W (MCXC), and mass $M_{YZ,500} = 2.98^{+0.41}_{-0.44} \times 10^{14} M_{\odot}$ (PSZ1). Fig. ii.11 shows the centre of the cluster with diffuse emission with an irregular morphology. Assuming that this emission is a single source and that any embedded galaxies do not show significant radio emission, the 168 MHz flux density is measured to be $S_{168} = 561 \pm 42$ mJy, with an estimated LAS of $\sim 4.8$ arcmin translating to an LLS at the cluster’s redshift of $\sim 650$ kpc. The radio source is part of the NVSS catalogue as NVSS J225055-162721 from which we obtain the 1.4 GHz flux density of $S_{1.4} = 37.7 \pm 2.0$ mJy (Condon et al., 1998). We obtain flux densities from the TGSS and VLSSr catalogues for sources at the position of the halo of $S_{147.5} = 659.4 \pm 67.0$ mJy (Intema et al., 2016) and $S_{74} = 1.34 \pm 0.25$ Jy (Lane et al.). With these and our 168 MHz measurement we obtain a spectral index across the frequency range 74–1400 MHz of $\alpha = -1.26 \pm 0.02$. This is consistent with typical cluster halo spectral indices (Feretti et al., 2012), however it is clear the 168 MHz flux density is being measured over a larger area, as well as including more sources, than the 147.5 MHz TGSS and 1.4 GHz NVSS measurements. This is clearly seen in Fig. ii.11 where there is much more emission to the north of the source, which may be unassociated and is not incorporated in the TGSS and NVSS catalogue values. The emission, while seen in the TGSS and NVSS contours at 3$\sigma_{\text{rms}}$, is not measured for the respective catalogues. Further, due to the higher resolution of the TGSS images, 147.5 MHz flux density measurements of extended emission may be under-estimated due to resolving out flux on larger spacial scales. This has less of an affect in the NVSS images. We note that the TGSS ADR1 has flux density discrepancies, where variations of more than ten per cent are seen within certain parts of the survey $^5$. This does not affect all regions within the survey, and in the case of Abell 2496 the flux density in this region does not vary by more than five per cent from the equivalent 151 MHz flux density obtained from the GLEAM survey, present in GLEAM extragalactic catalogue (GLEAM EGC; Hurley-Walker et al., 2017), so we consider the TGSS measurement as accurate on the spacial scales it samples. The bulk of the radio emission is offset from the X-ray emission seen with XMM-Newton data in the bottom panel of Fig. ii.11 (Obs. ID 0765030801, PI Reiprich). The emission does extend towards the X-ray peak, however given the offset the emission is more likely that of a relic. The slight extension of the 168 MHz emission along with the patchy 1.4 GHz NVSS and 147.5 MHz TGSS at the peak of the X-ray may suggest a particularly faint or small halo at the centre of the cluster, perhaps a mini-halo.
Figure ii.11: Diffuse emission within Abell 2496. Top: The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 15 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2. TGSS, medium purple, 12 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed, white circle is centred on the MCXC coordinates with radius of 1 Mpc. Bottom: Exposure corrected, smoothed XMM-Newton data overlaid with MWA contours as in the top panel.
Figure ii.12: Diffuse emission, Obj. A, in Abell 2556. The background image is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 13.4 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on Abell 2556 and the dotted circle on Abell 2554, each with radii of 1 Mpc.

§ii.2.2.9. Abell 2556 and Abell 2554

Fig. ii.12 shows the two clusters Abell 2556 (MCXC J2313.0-2137) and Abell 2554 (MCXC J2312.3-2130; PSZ1 G041.51-66.77) which have centres within 13 arcmin of each other, but have redshifts of $z = 0.0871$ and $z = 0.1108$ (Caretta et al., 2002) respectively. Their respective masses are $M_{X,500} = 2.4758 \times 10^{14} M_\odot$ (MCXC) and $M_{YZ,500} = 3.05^{+0.37}_{-0.39} \times 10^{14} M_\odot$ (PSZ1). Abell 2556 has an X-ray luminosity of $L_{500} = 1.509152 \times 10^{37}$ W (MCXC). To the north of Abell 2556, 1 Mpc from its centre (east of Abell 2554, over 1 Mpc) an elongated diffuse source is seen, labelled “A” in Fig. ii.12, with flux densities $S_{168} = 29.3 \pm 5.5$ mJy (this work) and $S_{14} = 2.2 \pm 0.5$ mJy (Condon et al., 1998). From these we obtain a steep spectral index of $\alpha_{168} = -1.22 \pm 0.14$. The LAS of the source is 3.33 arcmin which suggests an LLS of 336 kpc at $z = 0.0871$ or 416 kpc at $z = 0.1108$. The size of the emission does not suggest a radio relic. With no visible optical galaxy at the centre of the emission, lack of significant elongation, size, and steep spectral index suggest a radio phoenix. However, we note that radio phoenices are more often found towards cluster centres but this would be consistent with the spectral index, where phoenices closer to the centre become much steeper.

§ii.2.2.9. Abell 2556 and Abell 2554

Fig. ii.12 shows the two clusters Abell 2556 (MCXC J2313.0-2137) and Abell 2554 (MCXC J2312.3-2130; PSZ1 G041.51-66.77) which have centres within 13 arcmin of each other, but have redshifts of $z = 0.0871$ and $z = 0.1108$ (Caretta et al., 2002) respectively. Their respective masses are $M_{X,500} = 2.4758 \times 10^{14} M_\odot$ (MCXC) and $M_{YZ,500} = 3.05^{+0.37}_{-0.39} \times 10^{14} M_\odot$ (PSZ1). Abell 2556 has an X-ray luminosity of $L_{500} = 1.509152 \times 10^{37}$ W (MCXC). To the north of Abell 2556, 1 Mpc from its centre (east of Abell 2554, over 1 Mpc) an elongated diffuse source is seen, labelled “A” in Fig. ii.12, with flux densities $S_{168} = 29.3 \pm 5.5$ mJy (this work) and $S_{14} = 2.2 \pm 0.5$ mJy (Condon et al., 1998). From these we obtain a steep spectral index of $\alpha_{168} = -1.22 \pm 0.14$. The LAS of the source is 3.33 arcmin which suggests an LLS of 336 kpc at $z = 0.0871$ or 416 kpc at $z = 0.1108$. The size of the emission does not suggest a radio relic. With no visible optical galaxy at the centre of the emission, lack of significant elongation, size, and steep spectral index suggest a radio phoenix. However, we note that radio phoenices are more often found towards cluster centres but this would be consistent with the spectral index, where phoenices closer to the centre become much steeper.

5http://tgssadr.strw.leidenuniv.nl/doku.php?id=knownproblems
§ii.2.2.10. Abell 2680

Figure ii.13: Abell 2680. The background image is an RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 11.1 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle represents a 1 Mpc radius about the cluster centre.

Abell 2680 has a photometric redshift of $z = 0.1771$ (Wen and Han, 2013). Fig. ii.13 shows a patch of steep-spectrum emission at the centre of the cluster, where both the TGSS and NVSS surveys show no counterparts (Obj. A). The emission may be slightly elongated east-west, though this apparent elongation may just be the result of blending with the eastern sources. The steep-spectrum emission blends with the eastern NVSS sources: NVSS J235647-210352 and NVSS J235656-210326. The eastern-most source, NVSS J235656-210326, has a counterpart in the TGSS however the other source does not and so no spectral index can be calculated thus we do not predict a 168 MHz flux density for the source. We make an approximate measurement of the flux density yielding $S_{168} = 22.8 \pm 8.0$ mJy, where the uncertainty is given by Eq. ii.1 with an additional contribution to account for the slight blending to the east. We estimate a 1.4 GHz upper limit of 1.8 mJy to provide an upper limit to the spectral index between 168–1400 MHz, $\alpha_{168}^{1.4} \leq -1.2 \pm 0.2$. The LAS is estimated to be $\sim$3.2 arcmin, which at $z = 0.1771$ suggests a projected LLS of 600 kpc. The physical extent of the source and coincidence with the cluster centre core suggests a cluster halo. This particular case requires observations at different resolutions to determine if the source is actually extended.
§ii.2.2.11. Abell 2693

![Figure ii.14: Candidate radio halo A and steep-spectrum source B within and nearby Abell 2693. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 12 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster and has a 1 Mpc radius.](image)

Abell 2693 has a photometric redshift of $z = 0.173453$ (Coziol et al., 2009) and hosts a candidate radio halo at its centre. The candidate halo, marked A in Fig. ii.14, has an LAS of 3.75 arcmin and an LLS at the cluster’s redshift of 681 kpc. The location of the halo traces the optical galaxies. We measure the 168 MHz flux density to be $S_{168} = 49.6 \pm 6.0$ mJy. From the lack of 1.4 GHz emission in the NVSS, we estimate an upper limit to the 1.4 GHz flux density to be $S_{1.4} \leq 7.7$ mJy which imposes an upper limit on the spectral index of $\alpha_{168}^{1.4} \leq -0.88 \pm 0.06$. This limit on the spectral index is in no way conclusive of the classification of radio halo. However, the location, and size suggest that it may be a halo, and we classify this emission as a candidate halo.

To the west of the cluster there is an elongated steep-spectrum source marked B in Fig. ii.14. If the entirety of Obj. B is a single object, then there is a spectral gradient across the source, with a steeper spectral index towards the northeast. It is unlikely this is a cluster relic associated with Abell 2693 as it sits at $\sim 2.5$ Mpc from the cluster centre and has the morphology of a head-tail (HT) radio galaxy (Miley et al., 1972).
Table ii.3: 168 MHz flux densities and spectral indices calculated for blended sources near the centre of Abell 2721.

<table>
<thead>
<tr>
<th>Source</th>
<th>$S_{168}$ (mJy)</th>
<th>$\alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prediction using spectral index</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NVSS J000553-344434</td>
<td>183.5 ± 6.2</td>
<td>-0.88 ± 0.04</td>
</tr>
<tr>
<td>NVSS J000614-344730</td>
<td>292 ± 16</td>
<td>-1.15 ± 0.07</td>
</tr>
<tr>
<td>Diffuse emission</td>
<td>34 ± 33</td>
<td>$\leq -0.74$ ± 0.04</td>
</tr>
<tr>
<td>Measured with AEGEAN</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NVSS J000553-344434</td>
<td>234 ± 23</td>
<td>-</td>
</tr>
<tr>
<td>NVSS J000614-344730</td>
<td>276 ± 27</td>
<td>-</td>
</tr>
<tr>
<td>Diffuse emission</td>
<td>54 ± 14</td>
<td>$\leq -0.96$ ± 0.12</td>
</tr>
</tbody>
</table>

§ii.2.2.12. Abell 2721

Fig. ii.15 shows Abell 2721 (MCXC J0006.0-3443; PSZ1 G352.35-77.66) which has a redshift of $z = 0.114412 ± 0.000334$ (Zaritsky et al. 2006) with mass $M_{YZ,500} = 3.77^{+0.35}_{-0.37} \times 10^{14} M_{\odot}$ (PSZ1) and X-ray luminosity $L_{500} = 1.809494 \times 10^{37}$ W (MCXC). Diffuse radio emission is seen at 168 MHz offset to the east of the cluster centre (Obj. A in Fig. ii.15). No emission is detected at 1.4 GHz in NVSS, 843 MHz in SUMSS, or 147.5 MHz in TGSS above their respective $\sim 3\sigma_{rms}$ levels. The lack of emission seen in NVSS or SUMSS suggests a steep spectral index, however the lack of emission in TGSS is likely due to lack of sensitivity to extended, low surface brightness emission.

As part of the ATCA REXCESS Diffuse Emission Survey (ARDES), deep 1.4 and 2.1 GHz imaging of the cluster was obtained with the ATCA, finding no evidence of diffuse emission (Shakouri et al., 2016). Given that Abell 2721 was one of the more disturbed clusters in the ARDES sample, the lack of radio halo in the ATCA imaging was previously noted and a upper limit to the 1.4 GHz flux density is provided by Shakouri et al. (in prep.). This limit is $S_{1.4} \leq 7$ mJy. We estimate the LLS of the diffuse emission to be $\sim 460$ kpc. In an attempt to get a flux estimate for the diffuse emission at 168 MHz, we first calculate the spectral indices of the western and southern point sources, NVSS J000553-344434 and NVSS J000614-344730 respectively, such that we might predict the flux density contribution from these sources to the region and subtract them. For NVSS J000553-344434 we obtain catalogue flux densities of $S_{1.4} = 29.3 ± 1.3$ mJy (Condon et al., 1998), $S_{843} = 42.4 ± 1.7$ mJy (Mauch et al.), and $S_{147.5} = 218.5 ± 22.4$ mJy (Intema et al., 2016). These yield a spectral index of $\alpha = -0.88 ± 0.04$, giving a 168 MHz flux density of $S_{168} = 183.5 ± 6.2$ The uncertainty in the predicted flux density is obtained through standard unbiased prediction uncertainty (see Wolberg, 2006, pp. 54–57). Similarly, for NVSS J000614-344730 we obtain catalogue flux densities of $S_{1.4} = 24.5 ± 0.9$ mJy (Condon et al., 1998), $S_{843} = 49.7 ± 2.1$ mJy (Mauch et al., 2003), and $S_{147.5} = 305.4 ± 30.9$ mJy (Intema et al., 2016), yielding the spectral
Figure ii.15: Diffuse emission within Abell 2721. Top: The background is an RGB image formed using the DSS2 red, IR, and blue bands, with contours overlaid as follows: EoR0, white, beginning at $10 \, \text{mJy beam}^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at $1.5 \, \text{mJy beam}^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at $8.1 \, \text{mJy beam}^{-1}$ also increasing by a factor of 2. Bottom: X-ray image from the REXCESS survey with EoR0 contours overlaid as in the top panel along with X-ray contours increasing with a factor of 2 in black. The dashed circle is centred on the cluster with a radius of 1 Mpc.
index $\alpha = -1.15 \pm 0.07$ giving $S_{168} = 292 \pm 16$. The entire structure (diffuse emission, NVSS J000553-344434 and NVSS J000614-344730) is measured to have a flux density of $S_{168}^{\text{tot}} = 509 \pm 28$ mJy. Subtracting the point sources gives $S_{168} = 34 \pm 33$ mJy. The large uncertainty in this estimation is the result of combining predicted 168 MHz measurements. This estimate along with the ATCA 1.4 GHz limit provides a spectral index limit of $\alpha_{168}^{1.4} \leq -0.74 \pm 0.04$. We compare these results to those obtained by AEIGEAN, which is able to separate out the three components of the structure. This approach is successful, and yields a flux density of $S_{168} = 54 \pm 14$ for the diffuse emission, which is consistent with the method of summing the flux density contributions of each pixel within a box roughly surrounding the diffuse emission. The likely cause of the discrepancy are the SED’s between 147.5 and 1400 MHz, and using those to predict a 168 MHz flux density. We use AEIGEAN again to measure the flux densities of NVSS J000553-344434 and NVSS J000614-344730, arriving at $S_{168} = 236 \pm 23$ mJy and $S_{168} = 276 \pm 27$ mJy respectively. The total flux of the structure of three sources is then $S_{168}^{\text{tot}} = 565 \pm 38$ mJy, which disagrees with the previously measured value using the in-house code, though they agree within their uncertainties. Table ii.3 summarises the 168 MHz flux densities and spectral indices of the blended sources. The extra flux density likely originates from setting a floodclip value in AEIGEAN of $2\sigma_{\text{rms}}$, which is less than the hard $3\sigma_{\text{rms}}$ cutoff used with the in-house code. The difference in total flux of the structure is not large enough to be a significant cause of the discrepancy between individual source calculations. Predicting flux densities by way of spectral modelling can fail dramatically if the spectrum is not sampled finely enough to catch the true nature of the SED. We assume that both NVSS sources can be fit with simple power laws. This may not be the case, and without finer sampling in the vicinity of 168 MHz it is difficult to tell whether the power law fits are accurate. Despite this, the AEIGEAN result and predicted value of the diffuse emission are consistent to within their uncertainties, though they are large.

The bottom panel of Fig. ii.15 shows the REXCESS X-ray data overlaid with MWA contours. We see that the X-ray emission sits at the centre of the cluster, whereas the diffuse emission seen only at 168 MHz is offset towards the east. While there is the possibility that this is a cluster halo, elongated along the E-W direction and partially obscured by the emission from NVSS J000553-344434, it is more likely that this is a radio relic akin to the relics seen in Abell 0013 or Abell 0085. This candidate relic may be projected onto the centre of the cluster, and its reasonably flat spectral index compared to other relics would be consistent with a peripheral relic. Hence because of its offset and size, and in the absence of any available polarimetry, we classify this new diffuse emission as a candidate radio relic.

§ii.2.2.13. Abell 2744

Abell 2744 (MCXC J0014.3-3022; PSZ1 G009.02-81.22) is a distant massive X-ray luminous cluster ($M_{YZ,500} = 7.3614 \times 10^{14}$ $M_\odot$ (PSZ1), $z = 0.3066$, and $L_{500} =$
Figure ii.16: Abell 2744 with giant radio halo and relic. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 12.9 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster with a radius of 1 Mpc.

Abell 2744 with giant radio halo and relic. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 12.9 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster with a radius of 1 Mpc.

11.818114 $\times 10^{37}$ W (MCXC) and is a Hubble Frontier Fields cluster (Lotz et al., 2014) due to its mass and redshift, showing gravitational lensing of the high-redshift background galaxies (see Castellano et al., 2016, for a catalogue of lensed galaxies with redshift and magnification data). Fig. ii.16 shows Abell 2744 with both a centrally located giant radio halo (GRH, defined to have an LLS > 1 Mpc) and a mega-parsec scale radio relic on its northeast periphery (Govoni et al., 2001). Both of these objects are seen in the EoR0 field at 168 MHz, as is expected with such steep-spectrum sources, blending together along that northeast edge of the cluster. As seen in Fig. ii.16, the giant radio halo fills the the entire cluster out to 1 Mpc having an approximate LLS of 2.14 Mpc and the relic with an LLS on the order 1.49 Mpc.

We use AEGEAN to measure the integrated flux densities of the halo and relic. AEGEAN detects the two as a single source and fits two components—one for each the halo and relic—which give integrated fluxes of $S_{168}^{\text{halo}} = 550 \pm 51$ mJy and $S_{168}^{\text{relic}} = 237 \pm 24$ mJy. Venturi et al. (2013) obtain 325 MHz measurements using the GMRT, and use those along with re-reduced 1.4 GHz data from the VLA to estimate spectral indices of $\alpha_{\text{halo}} = -1.19^{+0.08}_{-0.11}$ and $\alpha_{\text{relic}} = -1.24 \pm 0.10$ for the halo and relic respectively. We use the 168 MHz flux density measurements along with those present in Venturi et al. to obtain spectral indices of $\alpha_{\text{halo}} = -1.11 \pm 0.04$ and
\[ \alpha_{\text{relic}} = \pm 1.19 \pm 0.05 \] for the halo and relic. There is little deviation and spectral indices calculated here agree to within the associated uncertainties, however the measurements by Venturi et al. (2013) exclude the bridge emission as well as at least one embedded point source, which are not excluded in these measurements.
Figure ii.17: A candidate relic and a faint radio galaxy, near Abell 2751 and APMCC 039, marked as A and B. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at 13.5 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on Abell 2751 and the dotted on APMCC 039, each with radii of 1 Mpc.
§ii.2.2.14. Abell 2751 and APMCC 039

Abell 2751 (MCXC J0016.3-3121, \(L_{500} = 4.95174 \times 10^{37}\) W from MCXC) and APMCC 039 have an angular separation of 17.7 arcmin and redshifts of \(z = 0.107\) (Struble and Rood, 1999) and \(z = 0.082\) (Dalton et al., 1997) respectively. However we note that the redshift for APMCC 039 is photometric, and so we compare the redshifts of the surrounding galaxies to check for the possibility that the two clusters may be interacting. Fig. ii.17 shows the two clusters, with the dashed and dotted circles indicating 1 Mpc radii about the cluster centres at their reported redshifts. The small orange squares indicate galaxies with redshifts in the range 0.1–0.114, which is \(cz \approx 2000\) km s\(^{-1}\) around the redshift of Abell 2751. There are no galaxies in the vicinity at the reported redshift of APMCC 039. It is clear from Fig. ii.17 that the two clusters host galaxies of similar redshifts and due to their angular separation are likely interacting.

We detect a new candidate relic to the east of Abell 2751 (Obj. A in Fig. ii.17), blending with the point source NVSS J001648-312223. As the relic sits \(\sim 1\) Mpc from both Abell 2751 and APMCC039, it may be associated with either cluster. In the case where the clusters are interacting, the relic sits at the intersection point between them. The relic itself is part of the NVSS catalogue as NVSS J001655-312258. The 168 MHz emission appears to simply be an extended radio tail extending from NVSS J001648-312223, however the 147.5 MHz TGSS emission is resolved enough to show that the relic emission is not associated with the point source. Fig. ii.17 shows the emission around these clusters with an RGB image which does not show an obvious optical ID associated with the relic emission. The combined total flux density of the point source and relic is measured to be \(S_{168}^{\text{tot}} = 843.1 \pm 60.7\) mJy. We obtain the following flux densities for NVSS J001648-312223 from catalogues: \(S_{1.4} = 55.0 \pm 2.1\) mJy (Condon et al., 1998), \(S_{843} = 91.4 \pm 3.2\) mJy (Murphy et al., 2007), \(S_{147.5} = 365.3 \pm 37.3\) mJy (Intema et al., 2016), and \(S_{74} = 1360 \pm 270\) mJy (Lane et al., 2014). Due to uncertainty in the TGSS ADR1 flux density scale in certain regions of the sky, we do not use the 147.5 MHz flux density for sources in this region. We assume a standard power law and fit these measurements to obtain a spectral index \(\alpha = -1.07 \pm 0.02\) which we use to predict the 168 MHz flux density as \(S_{168} = 518.2 \pm 9.4\) mJy. The flux density of the relic is then estimated to be \(S_{168}^{\text{rel}} = 324.9 \pm 61.4\) mJy.

To the north of APMCC 039 is the radio source NVSS J001804-311824 (Obj. B in Fig. ii.17), which at 1.4 GHz in the NVSS appears as a discrete point source with a flux density of \(S_{1.4} = 4.0 \pm 0.6\) mJy (Condon et al., 1998). The EoR0 field however shows emission extended far beyond this source, appearing as a faint tail to this possible radio galaxy. The entire emission is measured to have a 168 MHz flux density of \(S_{168} = 60.3 \pm 7.7\) mJy and an LAS of 8.816 arcmin which at the reported redshift of APMCC 039 translates to an LLS of 840.8 kpc, or 1066 kpc at the redshift of Abell 2751. If we take the catalogue 1.4 GHz flux density to be a lower limit to the flux, we can estimate an upper limit to the flux density across the entire source to be \(S_{1.4} \leq 24.0 \pm 0.6\) mJy. We determine limits to the spectral
Figure ii.18: Candidate radio relic within Abell 2798. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 13.8 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster with a radius of 1 Mpc.

index to be $-1.28(\pm0.09) \leq \alpha_{168} \leq -0.43(\pm0.06)$. This range covers normal radio galaxies, flat-spectrum sources, and most steep-spectrum sources so is not useful for classification. The emission lacks a clear optical ID, which may suggest that it is in fact a radio relic associated with APMCC 039. In the case of interacting clusters this is a distinct possibility. However with the morphology and range of spectral indices, we suggest that the emission is from likely a radio galaxy with a potential core described by the source NVSS J001804-311824.

§ii.2.2.15. Abell 2798

Abell 2798 (MCXC J0037.4-2831) has a redshift of $z = 0.105$ (Struble and Rood, 1999) with mass $M_{500} = 1.3146 \times 10^{14} \text{M}_\odot$ and X-ray luminosity $L_{500} = 0.545534 \times 10^{47} \text{W (MCXC)}$. Fig. ii.18 shows the cluster centre hosting a steep-spectrum radio source, slightly offset from centre. This radio source has a flux density of $S_{168} = 110.3 \pm 9.4 \text{ mJy}$ and LAS of 4.84 arcmin, which at the cluster’s redshift translates to an LLS of 575 kpc. Both the TGSS and NVSS surveys show extended emission offset slightly from the centroid of the 168 MHz emission. However there are no optical IDs for this emission. The NVSS source is NVSS J003738-283008 and has a flux density of $S_{1.4} = 9.0 \pm 1.3 \text{ mJy}$ (Condon et al., 1998). This yields a spectral index for the source of $\alpha_{168} = -1.18 \pm 0.08$. The RASS broad band (0.1–
2.4 keV) count image shows no significant X-ray emission within the cluster which is consistent with the low cluster mass. We classify this emission similarly to that in Abell 0013: a candidate radio relic either near the cluster centre or projected onto it. Further high-resolution imaging will be necessary to fully determine the nature of this emission.

§ii.2.2.16. Abell 2811

The cluster Abell 2811 (MCXC J0042.1-2832; PSZ1 G357.94-87.52) has a redshift of $z = 0.107908 \pm 0.000500$ (Zaritsky et al., 2006), an X-ray luminosity $L_{500} = 2.734146 \times 10^{37}$ W (MCXC), and mass $M_\text{YZ,500} = 3.67^{+0.35}_{-0.37} \times 10^{14}$ M$_\odot$ (PSZ1). Fig. ii.19 shows the cluster and RGB image overlaid with MWA, NVSS, and TGSS contours. At the centre of the cluster we make a new detection of a faint radio halo (Obj. A in Fig. ii.19). The cluster has been studied previously within the context of galactic haloes and the enrichment of the ICM (e.g. Sivanandam et al., 2009) with particular focus on the BCG, 2MASX J00420892-2832087. Further, as part of the XMM-Newton survey of the soft X-ray background Henley and Shelton (2013) consider this emission a galactic halo. However, Sivanandam et al. note that the surrounding X-ray emission is offset from the BCG by 27 arcsec ($\sim 55$ kpc), which suggests that the clusters is in a dynamic, merging state and that the low-frequency
Figure ii.20: Abell 3964. The background is an RGB image with overlaid contours overlaid as follows: EoR0, white, beginning at $10 \text{ mJy beam}^{-1}$ and increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at $1.4 \text{ mJy beam}^{-1}$ and increasing by a factor of 2; TGSS, medium purple, beginning at $10.8 \text{ mJy beam}^{-1}$ also increasing by a factor of 2. The dashed circle is centred on Abell 3964 and has a radius of 1 Mpc.

radio emission seen in Fig. ii.19 is a cluster halo and not emission associated with the BCG. This radio halo is on the order of 4.13 armin, which translates to $\sim 502$ kpc at the cluster’s redshift, however the surrounding sources make it difficult to properly ascertain its true size. We measure a flux density of the halo region with AEGERAN, which fits a Gaussian component to the halo, separating it out from the nearby sources it blends with, obtaining $S_{168} = 80.7 \pm 16.5$ mJy. Considering the lack of detection in the NVSS image, we estimate an upper limit to the 1.4 GHz flux density of 3.1 mJy which yields an upper limit to the spectral index of $\alpha_{168}^{1.4} \leq -1.5 \pm 0.1$. This would place the emission within the realm of the ultra-steep spectrum haloes.

§ii.2.2.17. Abell 3964

The cluster Abell 3964 has a faint, possibly steep-spectrum source on its North-Eastern periphery, about 1 Mpc from the cluster centre. The cluster has a redshift of $z = 0.1325$ (Caretta et al., 2002), and with an LAS of 2.84 arcmin this implies the emission has a projected LLS of 413 kpc. The emission has a flux density of $S_{168} = 16.6 \pm 4.1$. Despite how faint the emission is at 168 MHz, at the $3\sigma_{\text{rms}}$ level both the NVSS and TGSS surveys show emission as well. There is a faint source visible in the DSS2 red band image at the centre of the image which is likely
the host galaxy. There is no source in the NASA/IPAC Extragalactic Database (NED) at this position, however upon searching the VizieR service we find the source belongs to the USNO-B1.0 catalogue as USNO-B1.0 0701-0830366. We conclude that this is simply a faint, high-redshift radio galaxy coincidentally on the periphery of Abell 3964. This is left in as an example of such objects that were eventually rejected as, in particular, relic candidates.

§ii.2.2.18. Abell 4038

Abell 4038 (MCXC J2347.7-2808) is a nearby cluster with a redshift of $z = 0.028190 \pm 0.000550$ (Sanders et al., 2011), mass $M_{X,500} = 2.0383 \times 10^{14} \, M_\odot$ (MCXC), and X-ray luminosity $L_{500} = 1.029501 \times 10^{37} \, W$ (MCXC). A steep-spectrum source (Obj. B and C in Fig. ii.21) is reported by Slee and Reynolds (1984) near the cluster centre without an optically visible host galaxy. Slee and Roy (1998) and Slee et al. (2001) then provide follow-up analyses of this steep-spectrum source and consider it a radio relic (defined as a radio phoenix here). As with Abell 0085 the 168 MHz emission extends beyond the emission seen with the NVSS and TGSS. The emission of the phoenix blends with the radio emission from IC 5358 and 2MASX J23474209-2807335 (Obj. A in Fig. ii.21). Kale and Dwarakanath (2012) present a multi-frequency study of the phoenix with the GMRT, combining

Figure ii.21: The centre of Abell 4038. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 20 mJy beam$^{-1}$ and increasing with a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing with a factor of 2; TGSS, medium purple, beginning at 20 mJy beam$^{-1}$ also increasing with a factor of 2. Marked objects are described in the text.
literature data with their 150, 240, 606, and 1288 MHz data to subtract the interloping sources. We use results from their observations, as well as additional data from the NVSS at 1.4 GHz (Condon et al., 1998) and at 29.9 MHz from Slee et al. (2001; but see also Finlay and Jones 1973), to estimate the 168 MHz contributions from IC 5358 and 2MASX J23474209-2807335 as 80.6 ± 1.0 and 12.4 ± 0.4 mJy, respectively. We measure the combined total flux to be 4.875±0.249 Jy and arrive at $S_{168} = 4.782 ± 0.249$ Jy for the phoenix.

§ii.2.2.19. Abell S0084

Abell S0084 (MCXC J0049.4-2931) is a cluster added to the Abell catalogue as part of the supplementary catalogue. The cluster has a redshift of $z = 0.108041 ± 0.000400$ (Zaritsky et al., 2006) and X-ray luminosity $L_{500} = 1.438047 \times 10^{37}$ W (MCXC). We detect diffuse radio emission at the cluster centre (Fig. ii.22). The cluster was part of the ARDES sample of Shakouri et al. (2016) though no diffuse emission was detected at the centre of the cluster. From ATCA imaging at 1.4 GHz, Shakouri et al. obtain an rms noise of 313 µJy beam$^{-1}$ from which we estimate an upper limit to the 1.4 GHz flux density to be $S_{1.4} \leq 2.2$ mJy (Shakouri et al. in prep.). The centroid of the emission is offset from the cluster centre by 63 arcsec and has an LAS of 4.19 arcmin, which at the cluster’s redshift is an LLS of 511 kpc. The flux density is measured to be $S_{168} = 32.3±4.5$ mJy. The 147.5 MHz emission is not suggestive of a point source and the lack of detection by Shakouri et al. (2016) suggests a steep spectral index. With the 1.4 GHz upper limit, we estimate an upper limit on the spectral index, $\alpha_{1400}^{168} \leq -1.3 ± 0.1$. The right panel of Fig. ii.22 shows the REXCESS X-ray data with MWA contours overlaid. There is no cavity present in the X-ray data to suggest that the emission could be the lobes of an AGN and thus likely associated with the cluster itself. Further, Abell S0084 is not a cool core cluster (Pratt et al., 2009) and so we do not suspect this emission is a mini-halo. However the X-ray plasma appears undisturbed and the radio emission is offset from the X-ray peak by $\sim 100$ kpc so we only tentatively classify this emission as that of a candidate cluster halo, though note that the emission may be representative of an old or dead radio galaxy near the centre.

§ii.2.2.20. Abell S1063

Abell S1063 (MCXC J2248.7-4431; PSZ1 G349.46-59.90) is a Hubble Frontier Fields cluster and features heavy gravitational lensing of the distant background optical galaxies (see e.g. Diego et al., 2016). The cluster has a redshift of $z = 0.3475$ (Böhringer et al., 2004) with mass $M_{YZ,500} = 11.41^{+0.43}_{-0.44} \times 10^{14}$ M$_\odot$ (PSZ1) and X-ray luminosity $L_{500} = 27.166569 \times 10^{37}$ W (MCXC). The cluster is near the southern edge of the EoR0 field and so is more affected by noise. Despite this, above a 50 mJy beam$^{-1}$ level, an elongated piece of emission is unambiguously seen within the cluster. XMM-Newton archival data (Obs. ID 0504630101, PI Andersson, 52.734 ks, 0.1–12 keV), smoothed and exposure corrected, shows...
Figure ii.22: The centre of Abell S0084. Top: The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 7 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 12 mJy beam$^{-1}$ also increasing by a factor of 2. Bottom: X-ray image from the REXCESS survey with EoR0 contours overlaid as in the top panel along with X-ray contours.
Figure ii.23: Abell S1063. **Top:** The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 50 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; SUMSS, red, beginning at 5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 7.8 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster (with coordinates from Piffaretti et al. 2011—see text) and has a radius of 1 Mpc. The white box indicates the BCG of the cluster. **Bottom:** The background image is the XMM-Newton data with EoR0 contours overlaid is in the top panel.
strong X-ray emission coinciding with the 168 MHz radio emission though their respective peaks lie offset to one another, with the X-ray peak situated at the position of the BCG (see Fig. ii.23). The X-ray emission can be seen to extend further northeast with the peak of the 168 MHz emission occurring in this same direction. The BCG, LCRS B224549.3-444744 (with $z = 0.347110 \pm 0.000250$; Guzzo et al. 2009) is marked with a square in Fig. ii.23. Note that the MCXC, PSZ1, and ACO catalogues all report different coordinates for the cluster centre, and it is the MCXC coordinates that coincide with the central BCG, hence the MCXC coordinates are taken as the cluster centre (e.g. in Fig. ii.23).

The emission at 168 MHz has counterparts in the TGSS and SUMSS surveys. The morphology in the TGSS and SUMSS surveys is suggestive of a tailed radio galaxy, with the tail pointing into the cluster centre, however the peak of these TGSS and SUMSS emission does not show an optical ID for such a galaxy. The TGSS catalogue reports a source here with flux density $S_{147.5} = 155.5 \pm 16.5$ mJy and the SUMSS catalogue has a source with $S_{843} = 29.4 \pm 3.0$ mJy. However, the source lies in a region where the TGSS ADR1 flux densities are systematically low, and so we do not consider the 147.5 MHz flux density here. With the EoR0 field, a flux density (with a cut-off threshold of 50 mJy) of $S_{168} = 265 \pm 38$ is measured. We also obtain an LAS of $\sim 5.5$ arcmin and an LLS of $\sim 1670$ kpc. Taking the ratios of the logarithms of the 843 and 168 MHz flux densities yields a spectral index for the source of $\alpha_{843}^{168} = -1.36 \pm 0.11$. Due to the difference in resolution, it is likely this is an upper limit, where a not insignificant percentage of the 843 MHz integrated flux density may be resolved out. This will likely be the case with the TGSS measurement of the source also, though it is hard to be certain with the inherent flux density discrepancy that exists already with the TGSS ADR1 data. We provide reduced, archival ATCA data and describe this cluster further in §iii.2.

§ii.2.2.21. Abell S1099

Abell S1099 is reported to have a redshift of $z = 0.110400$ (Caretta et al., 2002). Fig. ii.24 shows the RGB image with MWA, NVSS, and TGSS contours overlaid. The cluster hosts extended, diffuse emission with steep spectral index, perhaps associated with one of the BCGs, 2MASX J23130574-2308369 ($z = 0.108575$; Caretta et al. 2004), which coincides with the peak of the emission at 168 MHz. We measure the 168 MHz to be $S_{168} = 184 \pm 20$ mJy, where the uncertainty includes a term to account for the slight blending towards the northwestern source, NVSS J231317-230513. Further, Obj. A in Fig. ii.24 appears to be an embedded point source, catalogued as NVSS J231255-230959 (Condon et al., 1998), which is not accounted for. We see that the 1.4 GHz emission is patchy and use the MIRIAD (Sault et al., 1995) task CONVOL to convolve the NVSS image to the 108.87 arcsec $\times$ 108.87 arcsec of the EoR0 field to measure the emission. This yields $S_{1.4} = 22.3 \pm 6.4$ mJy, where the uncertainty incorporates the embedded source and the blending with NVSS J231317-230513. We calculate a spectral index of $\alpha_{1.4}^{168} = -1.00 \pm 0.15$ which does not suggest a centrally located cluster.
Figure ii.24: Diffuse emission in Abell S1099. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing with a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 11.1 mJy beam$^{-1}$ also increasing with a factor of 2. The linear scale is at the redshift of Abell S1099. “A” marks a likely embedded source.

relic, though is consistent with the flatter-spectrum haloes or peripheral relics. It is not clear where the cluster centre lies, and with no auxiliary X-ray data beyond RASS we are unable to determine if the emission is that of a cluster halo. The morphology, and apparent steep spectral index are suggestive of a halo, but the BCG at the centre of the emission and the lack of clear cluster centre casts doubt towards this classification.

§ii.2.2.22. Abell S1121

Abell S1121 (PSZ1 G348.92-67.38) is reported by Coziol et al. (2009) to have a redshift of $z = 0.190431$ though Liu et al. (2015) report a redshift of $z = 0.3580$ for this system. Assuming $z = 0.3580$ as used by PSZ1 the cluster has a mass of $M_{YZ,500} = 7.05^{+0.61}_{-0.60} \times 10^{14} M_{\odot}$ (PSZ1). The cluster hosts a radio halo, with extended 168 MHz emission located at the cluster centre, with little-to-no SUMSS or TGSS counterparts at 843 and 147.5 MHz. There is a bright source to the north of the cluster that in SUMSS is creating artefacts streaking across the SUMSS image for this region. However, it is also important to note that Abell S1121 lies near the edge of the EoR0 field and is in an area of the image with higher noise, hence the 15 mJy beam$^{-1}$ contours in Fig. ii.25. The top panel of Fig. ii.25
Figure ii.25: Candidate radio halo within Abell S1121. Top: The background is an RGB image with contours overlaid as follows: EoR0, 15 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$ and TGSS, red, beginning at 13.8 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed and dotted circles are centred on the cluster with 1 Mpc radii at each of the reported redshifts. The orange boxes and circles indicate galaxies with available redshifts within 2000 km s$^{-1}$ at the two reported redshifts (see text) Bottom: Archival Chandra data smoothed to $\sim$15 arcsec resolution with EoR0 contours as in the top panel along with X-ray contours.
shows galaxies with available redshifts in the range \(cz \approx 2000 \text{ km s}^{-1}\) around the reported redshifts, with the orange circles associated with \(z = 0.190431\) and the orange boxes associated with \(z = 0.3580\). Given the location and numbers of each distribution, we consider the emission (and the cluster) to be at the redshift reported by Liu et al. (2015), \(z = 0.3580\). There is likely a separate, intervening system along the line-of-sight that Coziol et al. (2009) are measuring.

The bottom panel of Fig. ii.25 shows archival Chandra data (Obs. ID 13405, PI Garmire, exposure time 8.94 ks, 0.1–13.1 keV). This X-ray emitting plasma is situated in the core of the cluster, however it has directionality, with morphology like a cone similar to the Bullet Cluster discussed along with Abell 0133. This type of morphology suggests cluster dynamics often coincident with radio haloes. The main component of the diffuse 168 MHz emission coincides with this X-ray core. There are two point sources blended with the diffuse emission: SUMSS J232506-411339 and SUMSS J232457-411542. For SUMSS J232506-411339 we use the SUMSS catalogue measurement of \(S_{843} = 24.3 \pm 3.0 \text{ mJy}\) (Murphy et al., 2007) and assume a spectral index of \(\alpha = -0.8 \pm 0.2\), to predict \(S_{168} = 88 \pm 31 \text{ mJy}\). Similarly, for SUMSS J232457-411542 we use the catalogue measurement of \(S_{843} = 11.6 \pm 2.1 \text{ mJy}\) (Murphy et al., 2007), also assuming a spectral index of \(\alpha = -0.8 \pm 0.2\), to predict \(S_{168} = 42 \pm 16 \text{ mJy}\). The total flux of the emission is measured to be \(S_{168}^{\text{tot}} = 284 \pm 32 \text{ mJy}\). From this we estimate the flux density of the diffuse component to be \(S_{168} = 154 \pm 48 \text{ mJy}\). However, we have previously seen that extrapolating from poorly sampled SEDs—let alone using an assumed spectral index—does not always produce good results.

We estimate the LAS of the diffuse region of the emission to be \(\sim 4.3\) arcmin which translates to an LLS of \(\sim 1300\) kpc at \(z = 0.3580\). Given the location, size, coincidence with X-ray emission, approximate 168 MHz flux density, and the fact that Abell S1121 is a reasonably massive cluster, we classify the newly detected emission as a giant radio halo.

\section*{§ii.2.2.23. Abell S1136}

Abell S1136 (MCXC J2336.2-3136) has a redshift of \(z = 0.0625\) (Schwope et al., 2000), X-ray luminosity \(L_{500} = 0.504007 \times 10^{37} \text{ W}\), and mass \(M_{X,500} = 1.2886 \times 10^{14} \text{ M}_\odot\) (MCXC). Fig. ii.26 shows the centre of the cluster with an elongated piece of diffuse radio emission appearing strongly at 168 MHz, with a patchy counterpart in the TGSS survey at 147.5 MHz. There is no corresponding 1.4 GHz or 843 MHz emission seen in the NVSS or SUMSS surveys. This implies a steep spectral index. The source to the west of the diffuse emission is a double source, catalogued as NVSS J233603-313431. We use AEGEAN once again, and see the diffuse source split into two distinct components. The total flux density of the diffuse source is then measured to be \(S_{168} = 586 \pm 46 \text{ mJy}\).

The RASS broad-band 0.1–2.4 keV image does not show particularly strong X-ray emission at the centre, and the RGB image (Fig. ii.26) shows the optical concentration of galaxies at the centre is offset towards the west of the bulk of the
Figure ii.26: Diffuse emission within Abell S1136. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 14.4 mJy beam$^{-1}$ also increasing by a factor of 2.

168 MHz emission. The elongation is north-south, with an almost bent double-lobed structure, and has an LAS of $\sim$7.2 arcmin which translates to an LLS of $\sim$530 kpc. While the emission could be classified as a cluster halo, alternate explanations are those of cluster relic intervening along the line-of-sight towards the cluster, or a dead radio galaxy likely having a previous association with the BCG, ESO 470-G020. Without polarisation data and higher resolution imaging we do not classify this emission here. A follow-up observation of the cluster with the ATCA is described in §iii.1.

§ii.2.2.24. PSZ1 G307.55-77.87

PSZ1 G307.55-77.87 is a distant cluster with a photometric redshift of $z = 0.4530$ (Planck Collaboration et al., 2014) and mass of $M_{\text{YZ,500}} = 5.69^{+0.80}_{-0.88} \times 10^{14} \, M_\odot$ (PSZ1). Fig. ii.27 shows diffuse emission towards the cluster periphery. The nearby point source is LCRS B004346.8-393051 which has a redshift of $z = 0.155664 \pm 0.000450$ (Shectman et al., 1996) and is not associated with the cluster, though it may be the source of the diffuse emission within the context of a tail or lobe of a radio galaxy.

In the case that the emission is a cluster relic, we estimate the 168 MHz flux density by estimating the 168 MHz flux density of the LCRS source. The LCRS
source has 1.4 GHz flux density of $S_{1.4}^{\text{LCRS}} = 7.8 \pm 0.5 \text{ mJy}$ (Condon et al., 1998) and 843 MHz flux density of $S_{843}^{\text{LCRS}} = 11.1 \pm 1.0 \text{ mJy}$ (Murphy et al., 2007) which give a spectral index for the LCRS source of $\alpha_{843}^{1.4} = -0.696 \pm 0.218$. Extrapolating from this and $S_{1.4}^{\text{LCRS}}$ yields $S_{168}^{\text{LCRS}} = 34.4 \pm 16.2 \text{ mJy}$. The total emission of the possible relic and the LCRS source is measured to be $S_{168}^{\text{tot}} = 52.7 \pm 12.7 \text{ mJy}$. This implies a flux density of $S_{168} = 18 \pm 21 \text{ mJy}$ for the relic. Given the uncertainty there is not anything further we can say about the SED of the emission. However, the likely explanation is that of a radio galaxy and lobe or tail, not associated with the cluster but with LCRS B004346.8-393051.

§ii.2.2.25. RXC J2351.0-1954

RXC J2351.0-1954 (PSZ1 G057.09-74.45) has a redshift of $z = 0.247700 \pm 0.000190$, a mass $M_{YZ,500} = 5.66_{-0.62}^{+0.59} \times 10^{14} \text{ M}_\odot$ (PSZ1), and X-ray luminosity $L_X = (4.33 \pm 0.84) \times 10^{37} \text{ W}$ (Chon and Böhringer, 2012). The top panel of Fig. ii.28 shows the cluster and surrounding field, and the bottom panel shows the central region of the cluster. The dashed circle is at 1 Mpc radius and centred on $(\alpha_{J2000}, \delta_{J2000}) = (357.7703, -19.9132)$. In the top panel of Fig. ii.28 two steep-spectrum, diffuse sources are located to the southeast (Obj. A) and northwest (Obj. B). The bottom panel of the same figure shows a zoomed-in view of the cluster centre.
Figure ii.28: RXC J2351.0-1954. Top: RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ and increasing with a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ and increasing with a factor of 2; TGSS, medium purple, beginning at 13.8 mJy beam$^{-1}$ also increasing with a factor of 2. The dashed circle is centred on the cluster coordinates with a radius of 1 Mpc. Bottom: A smaller field of view of the top panel using the DSS2 red band only, with a small orange circle to denote the cluster’s coordinates given by Chon and Böhringer (2012) and orange squares to show galaxies with spectroscopic redshifts in the region.
Table ii.4: 168 MHz flux densities and spectral indices calculated for blended sources near RXC J2351.0-1954.

<table>
<thead>
<tr>
<th>Source</th>
<th>$S_{168}$ (mJy)</th>
<th>$\alpha_{147.5}^{1.4}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>APMUKS(BJ) B234816.36-201016.8 (D)</td>
<td>78.6 ± 10.7</td>
<td>−0.50 ± 0.06</td>
</tr>
<tr>
<td>NVSS J235053-195715 (E)</td>
<td>56.5 ± 7.9</td>
<td>−0.59 ± 0.06</td>
</tr>
<tr>
<td>Central diffuse emission (C)</td>
<td>87 ± 17</td>
<td>−</td>
</tr>
</tbody>
</table>

Figure ii.29: Optical density map of the area surrounding RXC J2351.0-1954. The asterisk marks the coordinates of the cluster given by Chon and Böhringer (2012). This map was generated by Dr. Siamak Dehghan.

Obj. A and B have similarities with double relics on the periphery of merging clusters. Obj. A is ∼8.35 arcmin (∼2 Mpc) from the cluster centre and Obj. B is ∼11.8 arcmin (∼2.8 Mpc). Neither A nor B have an obvious ID visible in the blue, red, or IR bands from the DSS2. The flux densities of the sources are measured to be $S_{168}^A = 56.9 ± 8.6$ mJy and $S_{168}^B = 147 ± 13$ mJy. Neither source appears in the NVSS data at 1.4 GHz so we place upper limits on the 1.4 GHz flux densities of $S_{14}^A \leq 4.22$ and $S_{14}^B \leq 4.7$ mJy places upper limits on the spectral indices of $\alpha_{168}^{1.4A} \leq -1.23 ± 0.07$ and $\alpha_{168}^{1.4B} \leq -1.68 ± 0.04$. Obj. B shows 147.5 MHz emission in the TGSS image above $3\sigma_{rms}$ but is not part of the TGSS ADR1 catalogue as it is not detected above $7\sigma_{rms}$. Further, emission from Obj. B is likely resolved out of the TGSS image due to its higher resolution than the MWA. Obj. A shows the elongated, bent shape that is typical of cluster relics. Obj. B shows a more regular morphology at 168 MHz in the EoR0, though shows elongation similar to a radio galaxy in the TGSS data.

The bottom panel of Fig. ii.28 shows the cluster centre, with the small, or-
...ange circle indicating the central coordinates provided by Chon and Böhringer (2012). Coordinates provided by Planck Collaboration et al. (2015a) lie to the southeast. The red-band DSS2 image shows an optical concentration of galaxies coinciding with 168 MHz radio emission extending from the point source NVSS J235053-195715. The orange squares indicate the positions of galaxies with spectroscopic redshifts, at the approximate redshift of the cluster and reported by Chon and Böhringer (2012). We assume that the centre of the cluster as traced by the optically visible galaxies, which does not coincide with coordinates from Chon and Böhringer. To better define the cluster centre, Dr. Siamak Dehghan produced Fig ii.29, which shows the isodensity map generated from 2972 galaxies within half a degree of the cluster’s reported centre, obtained from the SuperCOSMOS Sky Survey (Hambly et al., 2001c, b, a). The contour map was made using a grid of 150 kpc cells (at the redshift of the cluster) and then smoothed via a Gaussian kernel with standard deviation of 250 kpc. The density peak at $\alpha_{2000} = 357.756$ and $\delta_{2000} = -19.945$ is about 2 arcmin from the reported centre of the cluster. We consider these peak-density coordinates as the cluster centre, which still disagree with the coordinates provided by PSZ1.

The 168 MHz emission enveloping those galaxies at the optical centre of the cluster is likely a cluster halo, with the lack of significant 1.4 GHz NVSS emission implying a steep-spectrum source. We estimate the flux density of this diffuse emission by subtracting the extrapolated flux densities of the two blended sources, APMUKS(BJ) B234816.36-201016.8 and NVSS J235053-195715 (Obj. D and E in Fig. ii.28), using 1.4 GHz and 147.5 MHz flux density measurements from the NVSS and TGSS catalogues respectively (Condon et al., 1998; Intema et al., 2016). The spectral indices and extrapolated 168 MHz flux densities are presented in Table ii.4. The diffuse source is estimated to have a flux density of $S_{168} = 87 \pm 17$ mJy. From the lack of 1.4 GHz emission in the NVSS image above $3\sigma_{\text{rms}}$ we estimate an upper limit of $S_{1.4} \leq 4.3$ mJy resulting in an upper limit of $\alpha_{1.4}^{168} \leq -1.4 \pm 0.1$ for the spectral index. No significant emission is seen in the RASS broad band image, however due to the cluster’s redshift this is not surprising. Without supplementary archival Chandra or XMM-Newton data it is difficult to properly classify this emission as a halo. We consider this a newly detected candidate radio halo.

§ii.2.2.26. MACS J2243.3-0935

Cantwell et al. (2016) report the detection of a radio halo in the merging cluster MACS J2243.3-0935 (MCXC J2243.3-0935; PSZ1 G056.94-55.06), detected using the Karoo Array Telescope-7 telescope and GMRT. The cluster has a redshift of $z = 0.447$ (Ebeling et al., 2010), mass $M_{YZ,500} = 10.07^{+0.58}_{-0.60} \times 10^{14} M_\odot$ (PSZ1), and X-ray luminosity $L_{500} = 15.20 \times 10^{37}$ W (MCXC). Fig. ii.30 shows the the MWA contours overlaid on the RGB image. MACS J2243.3-0935 is near the edge of the EoR0 field and so the region within which it resides features heavy noise. Because of this, the detection is tentative, with the emission barely showing above $2\sigma_{\text{rms}}$. Fig. ii.30 shows the cluster with $2\sigma_{\text{rms}}$ contours to emphasise this.
Figure ii.30: MACS J2243.3-0935 with radio halo. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 60 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 10.2 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster with a radius of 1 Mpc.
Figure ii.31: Diffuse emission on the periphery of WHL J235151.0-085929 or centre of GMBCG J357.91841-08.97978. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 11.7 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the PSZ1 coordinates of WHL J235151.0-085929 with radius 1 Mpc. The dotted circle is centred on the cluster GMBCG J357.91841-08.97978 with the same 1 Mpc radius.

At this level we measure the 168 MHz flux density to be $S_{168} = 83 \pm 36$ mJy, with an LAS of $\sim2.8$ arcmin and a corresponding LLS of $\sim1$ Mpc. With the 610 MHz flux density measured by Cantwell et al. (2016) we obtain a spectral index of $\alpha_{610}^{168} = -1.6 \pm 0.4$. However, these results should be taken with caution due to the noise in this region of the EoR0 field.

§ii.2.2.27. WHL J235151.0-085929

WHL J235151.0-085929 (PSZ1 G082.31-67.01), a distant cluster with a redshift of $z = 0.3939$ (Wen et al., 2012) and mass $M_{YZ,500} = 5.90^{+0.78}_{-0.84} \times 10^{14}$ M$_\odot$ (PSZ1). Fig. ii.31 shows the cluster with an RGB (red, IR, blue) background and radio contours overlaid. Obj. A is a possible diffuse source on the cluster’s periphery. The cluster does not show significant X-ray emission in the RASS broad-band image. The location of the emission relative to the cluster centre and the lack of optical ID (see Fig. ii.31) are suggestive of a cluster relic. We note that source is point-like in the EoR0 field image, and that at this resolution—especially given the redshift of the cluster—there is an inherent uncertainty in whether the source
is extended or not. The NVSS image shows a source that is extended in the north-south direction, beyond that of the beam which is circular. The source does not appear in the TGSS ADR1 catalogue due to their higher 7σ_{rms} cutoff but is present in the NVSS catalogue, with 1.4 GHz flux density of \( S_{1.4} = 4.1 \pm 0.6 \) mJy (Condon et al., 1998). We use AEgéAN here to measure the flux density of the source to be \( S_{1.4}^{168} = 128 \pm 20 \) mJy. This, in conjunction with the 1.4 GHz measurement, is used to estimate a spectral index of \( \alpha_{1.4}^{168} = -1.62 \pm 0.10 \).

We do however note that the Gaussian Mixture Brightest Cluster Galaxy (GMBCG; Hao et al., 2010) catalogue reports a cluster at the centre of the emission: GMBCG J357.91841-08.97978, with a photometric redshift of \( z = 0.4 \). It is entirely likely that the emission resides within this cluster. If this is the case the steep spectral index and central location would imply a cluster halo. The two clusters, WHL J235151.0-085929 and GMBCG J357.91841-08.97978, have centres separated by \( \sim 2.7 \) arcmin which at \( z = 0.3939 \) is \( \sim 890 \) kpc. This separation in both angular distance and redshift would suggest either the clusters are interacting or that they are the same cluster. With this in mind we suggest that the emission is a candidate cluster halo, at a redshift of \( z = 0.3939 \), associated with the cluster GMBCG J357.91841-08.97978.

### §ii.2.3. On the scaling relations of cluster radio haloes

#### §ii.2.3.1. The \( P_{1.4}–L_X \) relation

There exists an empirical relation between the thermal and non-thermal emission of galaxy clusters traced by the synchrotron emission giving the radio halo 1.4 GHz power, \( P_{1.4} \) and the thermal Bremsstrahlung X-ray emission giving the cluster X-ray luminosity, \( L_X \). The \( P_{1.4}–L_X \) scaling relations have been studied and added too as each new halo detection or halo survey is released (e.g. GRHS: I; Venturi et al. 2007 and II; Venturi et al. 2008, EGRHS 7: I; Kale et al. 2013 and II; Kale et al. 2015, KAT-7 observations: Bernardi et al. 2016, ARDES: Shakouri et al. 2016) in an attempt to improve understanding about how the thermal X-ray emitting plasma interacts with the synchrotron electron population and how these relations might be caused by the clusters’ often dynamical natures.

For those haloes in our sample with measured 168 MHz flux densities and X-ray luminosities, we extrapolate using an assumed spectral index of \( \alpha = -1.3 \pm 0.2 \) (e.g. Cassano et al. 2013 use \(-1.3\) for haloes with no spectral index) to obtain the 1.4 GHz flux densities. We do not discriminate between ultra-steep spectrum and normal-spectrum radio haloes, as a number of the new detections presented here fall within the ultra-steep category when considering their spectral index limits. We then obtain the \( k \)-corrected 1.4 GHz radio power, \( P_{1.4} \), (see Hogg, \footnote{Adapted from \url{https://github.com/rsnemmen/nemmen/blob/master/nemmen/stats.py}} \footnote{Extended GMRT Radio Halo Survey}
Figure ii.32: The $P_{1.4}-L_X$ scaling relation updated with the halo detections in this paper. Error bars have been omitted for the sake of clarity. The black unfilled circles are haloes from the literature, drawing from the same sample as Shakouri et al. (2016) with the addition of the haloes detected in Triangulum Australis (Scaife et al., 2015), MACS J2243.3-0935 (Cantwell et al., 2016), ACT-CL J0256.5+0006 (Knowles et al., 2016), and PSZ1 G285.0-23.7 (Martinez Aviles et al., 2016). The green, filled circles are new halo detections from this paper, with assumed spectral indices of $\alpha = -1.3 \pm 0.2$. The dark-purple, filled circles are the same new halo detections but with the spectral index limits calculated here, thus they are upper limits to the 1.4 GHz radio halo power. For X-ray luminosities and radio power measurements without quoted uncertainties we assume a standard three per cent uncertainty to allow for BCES fitting (see text). The mauve shaded region represents a 95 per cent confidence interval associated with the solid black BCES orthogonal fit made to all the data. The powder-blue region is the same for the dotted BCES bisector fit presented by Cassano et al. (2013). The halo associated with the cluster CL 0217+70 has been included. Note that radio power is computed here assuming a flat $\Lambda$CDM cosmology, with $H_0 = 70\,\text{km}\,\text{s}^{-1}\,\text{Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_\Lambda = 0.7$, as compared to the rest of §ii which uses $H_0 = 68\,\text{km}\,\text{s}^{-1}\,\text{Mpc}^{-1}$. 
(2002; Hogg et al., 2002) via

$$P_{1.4} = \frac{4\pi D_L^2(z)}{(1 + z)^{1+\alpha}} S_{1.4} \quad [\text{W Hz}^{-1}], \quad \text{(ii.3)}$$

with the luminosity distance, $D_L(z)$, at the cluster’s redshift, with associated error, $\sigma_{P_{1.4}}$,

$$\sigma_{P_{1.4}} = \frac{4\pi D_L^2(z)}{(1 + z)^{1+\alpha}} \sqrt{[S_{1.4} \ln (1 + z) \sigma_\alpha]^2 + (\sigma_{S_{1.4}})^2} \quad [\text{W Hz}^{-1}] \quad \text{(ii.4)}$$

Further, for radio haloes in our sample with spectral index limits we calculate upper limits to the $P_{1.4}$ values. Fig. ii.32 shows the 64 current literature halo detections with $L_X$ measurements along with the newly detected halo in Abell 0141 and the newly detected candidate haloes in Abell 0141, Abell 2811, Abell S0084, and RXC J2351.0-1954. All but three (Triangulum Australis, MACS J2243.3-0935, and ACT-CL J0256.5+0006) of the previous literature detections are included by Shakouri et al. (2016) in their scaling relation plots. For Triangulum Australis we use $L_X, [0.1-2.4 \, \text{keV}] = (4.83 \pm 0.12) \times 10^{44} \, \text{erg s}^{-1}$ (Zhao et al., 2013). The cluster Abell 1213 has been removed from our sample as we do not consider this emission to be that of a cluster halo. The diffuse emission detected in Abell 1213 has an LLS of $\sim 250 \, \text{kpc}$ (LAS $\sim 4.3 \, \text{arcmin}$), and is asymmetric. It is more likely a radio phoenix within our classification scheme, or possibly a mini-halo. Further, as a point of difference from values presented by Shakouri et al. (2016), for Abell 0523 we use the X-ray luminosity estimated by Girardi et al. (2016) of $3.44 \times 10^{44} \, \text{erg s}^{-1}$ compared to $1.07 \times 10^{44} \, \text{erg s}^{-1}$ reported by Ebeling et al. (1998).

For $L_X$ and $P_{1.4}$ measurements without quoted uncertainties we attribute a standard three per cent error, which is approximately the mean value of the reported uncertainties, such that we can utilise the Bivariate Correlated Errors and intrinsic Scatter (BCES) linear regression method (Akritas and Bershady, 1996) to determine the best-fitting parameters to the data. We use the PYTHON code BCES\footnote{Available at https://github.com/rsnemmen/BCES}, a utilisation of which is shown by Nemmen et al. (2012). Table ii.5 summarises the best-fitting parameters for each of the BCES methods. Fig. ii.32 shows the best-fitting line (solid black) of the BCES orthogonal method, with the mauve, shaded region the 95 per cent confidence levels for that fit. The fit shown in Fig. ii.32 uses the assumed $\alpha = -1.3 \pm 0.2$ rather than the upper limits calculated. We also estimate the raw scatter, $\sigma_{\text{raw}}$, in the data via the error-weighted orthogonal distances to the best-fitting regression line via (e.g. Pratt et al., 2009; Cassano et al., 2013)

$$\sigma_{\text{raw}}^2 = \frac{(N/N - 2)}{\sum_{i=1}^{N} 1/\sigma_i^2} \sum_{i=1}^{N} \frac{1}{\sigma_i^2} (Y_i - aX_i - b), \quad \text{(ii.5)}$$

where $N$ is the sample size, $\sigma_i^2 = \sigma_{y_i}^2 + a^2 \sigma_{x_i}^2$ for uncertainties $\sigma_y$, $\sigma_x$ in $Y$, $X$, and fitting parameters $a$, $b$.  

Available at https://github.com/rsnemmen/BCES
We find that the equivalent BCES orthogonal fit from Cassano et al. (2013) is consistent within the uncertainties of the data, however the raw scatter for equivalent fits has increased with the increase in sample size. New haloes and halo candidates from this work lie where expected. The halo within Abell S0084 is hosted by the second least X-ray luminous cluster in the sample, surpassed only by CL 0217+70; its location on the $P_{1A}-L_X$ diagram expected for the cluster’s X-ray luminosity assuming the spectral index is close to $-1.3$. Such a low-luminosity, low-power detection was expected of the MWA due to its sensitivity to weak, steep-spectrum emission. However, we would also expect to find more ultra-steep spectrum halo candidates, given the frequency of 168 MHz used here. Only one halo in our sample clearly fits this definition: the candidate halo within GMBCG J357.91841-08.97978 with $\alpha_{1400}^{168} = -1.61 \pm 0.10$. This cluster, however, does not have a measured X-ray luminosity, nor significant emission seen in the soft-band RASS image, thus is not included in the present analysis.

There is a single halo that lies far beyond the rest of the sample, residing in the under-luminous cluster CL 0217+70, detected via its radio emission (Brown et al., 2011). The cluster is somewhat unique in its detection via radio emission, but also in that it features both a halo and a pair of relics. Its nature as under-luminous in the 0.1–2.4 keV X-ray band may be an effect of an uncertain redshift, though we have included the halo assuming the redshift is correct. Table ii.5 includes BCES best-fitting parameters for the four BCES methods, both including and excluding CL 0217+70. We see that the raw scatter ($\sigma_{\text{raw}}$) of the data is lower when excluding CL 0217+70, and that the overall fits tend to be steeper.

§ii.2.3.2. The $P_{1A}-M_{500}$ relation

We also update the known $P_{1A}-M_{500}$ scaling relation (e.g. Cassano et al. 2013, Shakouri et al. in prep.) similarly. We draw again from the same sample of haloes of Shakouri et al. (2016, in prep.) with the exception of the following clusters: Abell 1213, Abell 2218, as we do not consider these haloes; CL 0217+70, CL 1446+26, Abell 339, Abell 1550, due to lack of $M_{500}$ value; we do not use Abell 0851 as mass estimates through various methods vary from $4.4 \times 10^{14} \text{ M}_\odot$ (Martinet et al., 2016) to $12.5 \times 10^{14} \text{ M}_\odot$ (Hoekstra et al., 2015); and we do not use Abell 0800 as the only available mass is that given as part of the MCXC which uses X-ray luminosity as the mass proxy compared to the Compton parameter, $Y_{SZ}$, as used by PSZ1. For the remaining clusters, mass estimates are taken from PSZ1 except in the cases of MACS J0416.1-2403 (Umetsu et al., 2014) and Abell 0523 (Girardi et al., 2016). We also add the newly detected haloes in Abell S1121 and Abell 0141, and the candidate haloes in Abell 2811, Abell S0084, RXC J2351.0-1954, and WHL J235151.0-085929, as well as the recent detections in Triangulum Australis, MACS J2243.3-0935, ACT-CL J0256.5+0006, and PSZ1 G285.0-23.7.

Fig. ii.33 shows the updated scaling relation. We use the BCES method again to determine best-fitting parameters to the data. Table ii.5 summarises the best-fitting parameters for the four BCES methods for both the $P_{1A}-L_X$ and the $P_{1A}$--
Table ii.5: Best-fitting parameters from the BCES fitting with different methods, where $\log_{10}(P_{1.4}) = a \log_{10}(X) + b$ for $X = L_X, M_{500}$. The raw scatter in the data, $\sigma_{\text{raw}}$, is computed for each fitting method.

<table>
<thead>
<tr>
<th>Method</th>
<th>$a$</th>
<th>$b$</th>
<th>$\sigma_{\text{raw}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{1.4}-L_X$, excluding CL 0217+70</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BCES(X</td>
<td>Y)</td>
<td>2.61 ± 0.27</td>
<td>−92.60 ± 11.91</td>
</tr>
<tr>
<td>BCES(Y</td>
<td>X)</td>
<td>1.45 ± 0.16</td>
<td>−40.82 ± 7.24</td>
</tr>
<tr>
<td>Bisector</td>
<td>1.90 ± 0.11</td>
<td>−60.86 ± 5.13</td>
<td>0.38</td>
</tr>
<tr>
<td>Orthogonal</td>
<td>2.34 ± 0.21</td>
<td>−80.84 ± 9.33</td>
<td>0.45</td>
</tr>
<tr>
<td>$P_{1.4}-L_X$, including CL 0217+70</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BCES(X</td>
<td>Y)</td>
<td>2.47 ± 0.26</td>
<td>−86.68 ± 11.78</td>
</tr>
<tr>
<td>BCES(Y</td>
<td>X)</td>
<td>1.32 ± 0.19</td>
<td>−34.72 ± 8.38</td>
</tr>
<tr>
<td>Bisector</td>
<td>1.76 ± 0.16</td>
<td>−54.59 ± 7.21</td>
<td>0.41</td>
</tr>
<tr>
<td>Orthogonal</td>
<td>2.17 ± 0.24</td>
<td>−73.23 ± 10.60</td>
<td>0.47</td>
</tr>
<tr>
<td>$P_{1.4}-M_{500}$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BCES(X</td>
<td>Y)</td>
<td>5.31 ± 0.77</td>
<td>−54.55 ± 11.42</td>
</tr>
<tr>
<td>BCES(Y</td>
<td>X)</td>
<td>2.89 ± 0.28</td>
<td>−18.61 ± 4.17</td>
</tr>
<tr>
<td>Bisector</td>
<td>3.77 ± 0.30</td>
<td>−31.60 ± 4.38</td>
<td>0.47</td>
</tr>
<tr>
<td>Orthogonal</td>
<td>5.16 ± 0.74</td>
<td>−52.29 ± 10.99</td>
<td>0.59</td>
</tr>
</tbody>
</table>

$M_{500}$ relation. Fig. ii.33 shows the BCES orthogonal fit along with the equivalent BCES orthogonal fit by Cassano et al. (2013). We use a total of 64 haloes in this analysis, and Cassano et al. (2013) use 25. Despite this difference in sample size, we see identical best-fitting parameters for the BCES orthogonal method.

We use Fig. ii.34 as an illustration as to the importance of homogeneous measurements. Fig. ii.34 shows clusters that have masses measured via both the SZ effect and through their X-ray luminosity from the MCXC and PSZ1 catalogue. The MCXC (Piffaretti et al., 2011) estimates $M_{500}$ use the X-ray luminosity of the cluster as a proxy, extrapolating from relations between the two. Similarly, PSZ1 (Planck Collaboration et al., 2015a) estimates mass using the Compton $Y_{SZ}$ parameter. This illustrates clearly both a systematic discrepancy as well as random error between the types of measurements. The $M_{X,500}$ measurements are systematically higher than the $M_{YZ,500}$ measurements. There is also large discrepancies between measurements at large redshift, though this is to be expected as objects farther away are more difficult to measure accurately.

§ii.2.4. The detection rate of diffuse cluster emission within the EoR0 field

Here we examine the detection rate of radio haloes, relics, and phoenices within the EoR0 field and compare these to clusters in which no such emission is seen. For these comparisons we consider only those clusters within the MCXC and PSZ1
Figure ii.33: The $P_{1.4} - M_{500}$ scaling relation updated with the new halo detections in this paper. The fits are from this work (solid black line with mauve confidence interval) and Cassano et al. (2013; dotted black line with powder-blue confidence interval). The points are as in Fig. ii.32 except the green star indicates a halo with an exactly calculated spectral index. Note that, as with Fig. ii.32 radio power is computed assuming a flat $\Lambda$CDM cosmology, with $H_0 = 70\,\text{km s}^{-1}\text{Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_\Lambda = 0.7$, as compared to the rest of §ii which uses $H_0 = 68\,\text{km s}^{-1}\text{Mpc}^{-1}$.

catalogue, as a majority of ACO clusters do not have available masses, and a significant portion do not have redshifts. Fig. ii.35 shows cluster mass against redshift. Up until recently it has only been possible to detect radio haloes and relics in nearby clusters, except in the most massive and luminous examples (e.g., Abell 2744). This plot effectively demonstrates the power of the MWA to detect diffuse cluster emission in the redshift range 0.02–0.5, with uniformly distributed masses and redshifts over this range from catalogue-selected clusters. Fig. ii.35 also shows that with such sensitivity we are now probing the diffuse emission in nearby X-ray–emitting low-mass clusters.

The two major limiting factors in the detection of such emission are the resolution and sensitivity of the telescope. The MWA as a low-frequency telescope is limited in its resolution by the maximum baseline at 2873.3 m. The EoR0 field in particular has a beam size of $\sim 2.3$ arcmin, which, when considering only resolution, means that the viable detection range for distant haloes is $\text{LLS}_{500-1000\,\text{kpc}}(z) \leq 0.22–0.67$. Beyond these redshifts, any potential haloes if detected become point sources as they appear the same angular size as the synthesized beam. The second issue is sensitivity; the EoR0 field reaches a sensitivity of approximately 2.3 mJy beam$^{-1}$ in the best regions of the image. The lowest theoretical sensitivity of the Phase I MWA is approximately 1.7 mJy beam$^{-1}$ (Franzen et al., 2016).
Table ii.6: Clusters with diffuse emission and available mass measurements included in Fig. ii.35.

<table>
<thead>
<tr>
<th>Cluster</th>
<th>$M_{500}$ ($\times 10^{14} M_\odot$)</th>
<th>Type</th>
<th>New</th>
</tr>
</thead>
<tbody>
<tr>
<td>Abell 0013</td>
<td>2.79 $^a$</td>
<td>R</td>
<td>×</td>
</tr>
<tr>
<td>Abell 0085</td>
<td>4.90 $^a$</td>
<td>R</td>
<td>×</td>
</tr>
<tr>
<td>Abell 0133</td>
<td>3.08 $^a$</td>
<td>P</td>
<td>×</td>
</tr>
<tr>
<td>Abell 0141</td>
<td>4.48 $^a$</td>
<td>H</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 2556</td>
<td>2.47 $^b$</td>
<td>cP</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 2721</td>
<td>3.77 $^a$</td>
<td>cR</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 2744</td>
<td>9.56 $^a$</td>
<td>H,R</td>
<td>×</td>
</tr>
<tr>
<td>Abell 2751</td>
<td>1.26 $^b$</td>
<td>R</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 2798</td>
<td>1.31 $^b$</td>
<td>cR</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 2811</td>
<td>3.67 $^a$</td>
<td>H</td>
<td>✓</td>
</tr>
<tr>
<td>Abell 4038</td>
<td>2.03 $^b$</td>
<td>P</td>
<td>×</td>
</tr>
<tr>
<td>Abell S0084</td>
<td>2.36 $^b$</td>
<td>cH</td>
<td>✓</td>
</tr>
<tr>
<td>Abell S1121</td>
<td>7.05 $^a$</td>
<td>H</td>
<td>✓</td>
</tr>
<tr>
<td>RXC J2351.0-1934</td>
<td>5.60 $^a$</td>
<td>cH,cR,cR</td>
<td>✓</td>
</tr>
<tr>
<td>MACS J2243.3-0935</td>
<td>10.07 $^a$</td>
<td>H</td>
<td>×</td>
</tr>
<tr>
<td>GMBCG J357.91841-08.97978</td>
<td>5.90 $^a$</td>
<td>cH</td>
<td>✓</td>
</tr>
</tbody>
</table>

$^a$ $M_{YZ,500}$ (Planck Collaboration et al., 2015a)

$^b$ $M_{X,500}$ (Piffaretti et al., 2011), truncated to two decimal places.
Figure ii.34: The difference between $M_{X,500}$ (MCXC) and $M_{YZ,500}$ (PSZ1) measurements. This sample is for all clusters within the MCXC and PSZ1 catalogue that have both measurements. $M_{X,500}$ measurements utilise the cluster X-ray emission as a proxy for estimated mass, whereas $M_{YZ,500}$ uses the Sunyaev–Zel’dovich (SZ) effect as the mass proxy. The solid black line is simply a line indicating equal mass measurements.

However the sensitivity here is not the limiting factor in detecting high-redshift haloes. For the redshift range $z = 0.22–0.67$, a halo the size of the beam could theoretically be detected with 1.4 GHz power in the range of $P_{1.4}(z = 0.22–0.67) \geq 0.3–2 \times 10^{23}$ W Hz$^{-1}$. This entire range falls below the what is typically seen of cluster haloes (e.g. Cassano et al., 2013; Kale et al., 2015; Shakouri et al., 2016). The solid, black line in Fig. ii.35 shows the theoretical limit for detecting 1 Mpc radio haloes given the $P_{1.4}-M_{500}$ relation found in §ii.2.3.2 and assuming a spectral in index of $-1.3$. We see that haloes detected as part of this work lie above this limit, as expected, but note that relics are not bound by the same limit.

The somewhat uniform distribution of detections shown Fig. ii.35 is not surprising given the approximate limits above, and with the sensitivity and resolution of the EoR0 field, the entire redshift space covered by the Planck and MCXC catalogues are available for halo detection.

§ii.3. Conclusions about the EoR0 field

In this section we have presented diffuse cluster emission seen within the EoR0 field. We have presented 11 haloes, 9 relics, and 3 phoenices, of which 9 are new
Cluster redshift, $z$

Cluster mass, $M_{500} \times 10^{14} M_\odot$

Non-detection—PSZ1
Prev. det. cluster relic—PSZ1
Prev. det. radio phoenix—PSZ1
New cluster relic—PSZ1
New radio phoenix—PSZ1
New cluster halo—PSZ1

Non-detection—MCXC
Prev. det. cluster relic—MCXC
Prev. det. radio phoenix—MCXC
Prev. det. cluster halo—MCXC
New cluster relic—MCXC
New radio phoenix—MCXC
New cluster halo—MCXC

**Figure ii.35:** Cluster mass against redshift for clusters within the MCXC and PSZ1 catalogues. The filled points are those using the PSZ1 $M_{YZ,500}$ measurements and unfilled points are those using the MCXC $M_{500}$ measurements. Where clusters appear in both catalogues we use the PSZ1 $M_{YZ,500}$ measurements. The coloured lines indicate the limit at which a 1 Mpc halo can be detected given the $P_{1.4} - M_{500}$ scaling relation in §ii.2.3 assuming a sensitivity of 2.3 mJy beam$^{-1}$, beam size of 2.3 arcmin, and spectral indices $\{-1.1, -1.2, -1.3, -1.4, -1.5, -1.7, -1.8\}$, where a lower spectral index requires a lower mass cluster. No haloes are detected below this limit. Table ii.6 provides details of the clusters with detected diffuse emission included here. References for redshifts: Abell et al. (1989), Dalton et al. (1994), Alonso et al. (1999), Batuski et al. (1999), de Propris et al. (1999), Jones and Forman (1999), Struble and Rood (1999), Caretta et al. (2002), Zaritsky et al. (2006), Coziol et al. (2009), Wen et al. (2010), Piffaretti et al. (2011), Williamson et al. (2011), Chon and Böhringer (2012), Mahajan et al. (2012), Hicks et al. (2013), Pearson and Batuski (2013), Wen and Han (2013), Planck Collaboration et al. (2014), Bleem et al. (2015), Liu et al. (2015), and Planck Collaboration et al. (2015b).
haloes, 6 are new relics, and 1 is a new phoenix, or candidates of each. Along with these, we have presented 6 sources that may be either haloes, relics, phoenices, or relic AGN emission from ancient radio galaxies. Where possible we determine 168 MHz flux densities, estimate angular and linear sizes, and estimate spectral indices or limits. With these detections we examine the incidence rate of such emission, finding that the MWA is beginning to see emission without bias beyond what is present in the catalogues clusters are drawn from. Further, we update the $P_{1.4} - L_X$ and $P_{1.4} - M_{500}$ scaling relations of radio halo power with cluster X-ray luminosity and mass. We find nearly identical best-fitting parameters to the relations as previous works (i.e. Cassano et al. 2013) despite an increase in sample size.
§iii. Serendipity and follow-up observations

The primary goal of this work has been the search for diffuse cluster emission using MWA images in the form of the EoR0 field and GLEAM. During the course of this, interesting radio emission not considered a halo or relic has been found and examined. This section presents two such objects, as well as a follow-up of a tentative halo. First, a dying radio galaxy at the centre of the cluster Abell S1136, then diffuse emission resembling a cluster halo within Abell S1063, and finally a possible spiral galaxy hosting a radio-loud AGN with disturbed, double-lobed structure.

§iii.1. Diffuse emission within Abell S1136

§iii.1.1. A dying radio galaxy associated with ESO 470-G020

The AGN of a radio galaxy has a typical lifetime on the order of $\sim10^8$ yr (Cordey, 1986) and so there will be a stage in its lifetime where the core does not produce new electrons to power the jets. However, the radio plasma that makes up the lobes does not instantaneously vanish. The rate of energy loss of the electrons is proportional to $-E^2$, and so the highest-energy electrons lose energy more quickly. The result is the electron population of the old radio plasma has comparatively more low-energy electrons, giving the steep-spectrum often observed (Komissarov and Gubanov, 1994). Such dying sources are seldom seen, which is a result of both a lack of sensitivity with radio instruments as well as the short lifetime of this dying phase (Cordey, 1986; Giovannini et al., 1988). The first such detection was made by Cordey (1987) with a radio source, B2 0924+30, showing the expected characteristics of a dying radio galaxy associated with IC 2476. Currently, there are still only a small number of confirmed dying radio galaxies, and larger-scale searches have been performed with the hope of detecting more (e.g. Murgia et al., 2011).

Presented in §ii.2.2.23 was the diffuse emission associated with the cluster Abell S1136. We present the cluster once more in Fig. iii.1. The nature of this emission was not understood and the morphology of the source did not appear to represent either a relic or halo. Thus, we considered that the emission may be that of a dying radio galaxy—the old lobes of the central elliptical ESO 470-G020. It is common for BCGs and cD galaxies to host radio lobes, and perhaps ESO 470-G020 was no different. However, the lack of emission at 1.4 GHz suggests a steep spectral index, and since no core is detectable in the EoR0 field we suggest that, if a radio galaxy, it is not in a stage of normal activity.

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Figure iii.1: The centre of Abell S1136 showing elongated diffuse emission, as presented in §ii.2.2.23. The background is an RGB image with contours overlaid as follows: EoR0, white, beginning at 10 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; NVSS, red, beginning at 1.5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 14.4 mJy beam$^{-1}$ also increasing by a factor of 2.
Table iii.1: The measured flux densities for the diffuse source across the narrow GLEAM bands. The central frequency, $\nu_c$, is that given within the FITS header of the GLEAM images, and the local rms noise, $\sigma_{\text{rms}}$, is that calculated by BANE.

<table>
<thead>
<tr>
<th>Band</th>
<th>$\nu_c$ (MHz)</th>
<th>$S_\nu$ (mJy)</th>
<th>$\sigma_{\text{rms}}$ (mJy beam$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>118-126</td>
<td>122.2</td>
<td>985 ± 108</td>
<td>34.0</td>
</tr>
<tr>
<td>126-134</td>
<td>129.9</td>
<td>789 ± 96</td>
<td>35.0</td>
</tr>
<tr>
<td>139-147</td>
<td>142.7</td>
<td>697 ± 77</td>
<td>22.8</td>
</tr>
<tr>
<td>147-154</td>
<td>150.4</td>
<td>613 ± 88</td>
<td>21.5</td>
</tr>
<tr>
<td>154-162</td>
<td>158.1</td>
<td>524 ± 71</td>
<td>18.4</td>
</tr>
<tr>
<td>162-170</td>
<td>165.8</td>
<td>506 ± 70</td>
<td>17.0</td>
</tr>
<tr>
<td>170-177</td>
<td>173.4</td>
<td>548 ± 84</td>
<td>19.1</td>
</tr>
<tr>
<td>177-185</td>
<td>181.1</td>
<td>454 ± 74</td>
<td>17.5</td>
</tr>
<tr>
<td>185-193</td>
<td>188.8</td>
<td>428 ± 68</td>
<td>15.4</td>
</tr>
<tr>
<td>193-200</td>
<td>196.5</td>
<td>342 ± 61</td>
<td>16.7</td>
</tr>
<tr>
<td>200-208</td>
<td>204.2</td>
<td>371 ± 69</td>
<td>17.8</td>
</tr>
<tr>
<td>216-223</td>
<td>219.5</td>
<td>367 ± 85</td>
<td>16.5</td>
</tr>
<tr>
<td>223-231</td>
<td>227.2</td>
<td>318 ± 94</td>
<td>16.9</td>
</tr>
</tbody>
</table>

§iii.1.2. Follow-up analysis with GLEAM

As the emission within Abell S1136 is detected in all 20 GLEAM narrow bands, we make use of these to measure the spectral index of the entire diffuse region. As seen in Fig. ii.26, the diffuse emission at 168 MHz at the resolution of the MWA blends with the nearby double source, NVSS J233603-313431. Despite this, we make use of aegean to attempt to de-blend the diffuse region and NVSS J233603-313431. This is successful for a majority of the bands, especially at the higher frequencies. However, due to the lower resolution of the low-frequency bands we are unable to disentangle the sources with aegean. Table iii.1 shows the flux densities within each frequency band for the diffuse region. Bands not present are those that had the double and diffuse source fit as a single source, or those that decomposed the emission into three components, the third blending between the diffuse region and NVSS J233603-313431.

Fig. iii.2 shows the SED of the diffuse region within Abell S1136. The spectral index across the GLEAM bands is calculated to be $\alpha = -1.81 \pm 0.12$ which has the steepness expected from the lack of detectable 1.4 GHz or 843 MHz emission from NVSS and SUMSS. The SED here is assuming that contributions from point sources are negligible. This is an appropriate assumption given the lack of detection of point sources in the NVSS or SUMSS within the emission which suggests that any point sources, if present, must not contribute significantly to any flux. Any discrepancy due to embedded sources would be superseded by the uncertainty in the flux density measurements and the following spectral index calculation.
§iii.1.3. Follow-up observations of Abell S1136 at 2.1 GHz

On April 30, 2016, director’s discretionary time (DDT) was used to make an observation of the cluster Abell S1136 with the ATCA in the 6A configuration with the 16 cm band. We are able to get ~308 minutes of integration time on the diffuse source, though this is not enough time to allow rotation of the Earth to maximally fill the $uv$ plane. The 6A configuration has a largest baseline of 5938.8 m between the W4 and W392 stations. This large separation allows observations to view the compact cores of radio galaxies. Conversely, the shortest baseline is 627.6 m between the W4 and W45 stations and gives sensitivity to somewhat extended structures, up to approximately 1 arcmin. However, with only the 6A configuration we miss information on spatial scales sampled by the other configurations offered by the ATCA, especially missing out on the 30 metre minimum baseline that the ATCA is capable of. Since 2010, the ATCA has been operating with the Compact Array Broad-band Backend (CABB; Wilson et al., 2011) which allows the use of two intermediate frequency (IF) ranges of 2049 channels or 2048 MHz each. For 16 cm observations these two IFs are set to the same frequency range as it covers 95 per cent of the available bandwidth in that band.

The 16 cm band is centred on 2100 MHz and has an effective bandwidth of 1100–3100 MHz. This band gives the closest frequency to the EoR0 field of 168 MHz, but still offers a higher frequency than even the NVSS data, which can allow the exploration of the spectral index of, at the very least, any faint point sources.
§iii. The RFI flagging and calibration strategy for the initial four sub-bands of the primary and secondary calibrators and the source. At \texttt{uvsplit} each initial sub-band is further split into two sub-bands of 214 MHz each.

\textbf{Figure iii.3:} The RFI flagging and calibration strategy for the initial four sub-bands of the primary and secondary calibrators and the source. At \texttt{uvsplit} each initial sub-band is further split into two sub-bands of 214 MHz each.

sources within the diffuse emission seen in Abell S1136 and in particular the core. Despite the ever-increasing radio frequency interference (RFI) in the 16 cm band, observations were made without major RFI problems, with the exception of at least one 1000 pseudo-Jy spike of RFI during one of the pointings towards Abell S1136. Beyond that, the RFI contaminating the observations was expected within the 16 cm band.

§iii.1.3.1. Observing and calibrating

For most radio observations of astronomical sources, at least two calibration sources are required. These sources help to calibrate the amplitude of the flux density of the telescope response, the bandpass of the telescope, the polarisation leakages from the instrument, and the phase. For observations at 16 cm with the ATCA, the calibrator PKS B1934-638 is suitable for amplitude and bandpass calibration presuming it is up at the time of observation. At 1.4 GHz, PKS B1938-638 has a flux density of 14.9 Jy (Reynolds, 1994). The secondary calibrator, usually responsible for phase calibration, can be any source that does not require a large slew time of the telescope, that is reasonably strong, and that does not show extended structure at the observation frequency. For the observation of Abell S1136, the quasi-stellar source PKS B2313-340 was chosen as the secondary calibrator as it fit the aforementioned requirements. During the observation, the primary calibrator, PKS B1934-638 is visited first to calibrate the telescope for the observation, and is subsequently visited for a further 20 minutes to get data for calibration during data-processing. The secondary, PKS B2314-340, is observed in 2 minute intervals, for each 20 minute observation of the actual source, Abell S1136. The revisiting
of the secondary every 20 minutes allows the calibration of the phase throughout the observation.

After the observations, the data, including visibilities of the primary and secondary calibrators, and the source itself, are exported in the RPFITS format written by the correlator of the telescope. The reduction of these data are performed almost entirely within the MIRIAD data-reduction software (Sault et al., 1995). Task ATLOD acts as input, converting from RPFITS to MIRIAD data; UVFLAG is used here to flag end channels of the 2049 available due to bandpass rolloff from lack of sensitivity on the edges; UVSPLIT is used to split the data into individual datasets for the calibrators and source. In this process only the second spectral window (IF) is used, as IF1 and IF2 are identical, and IF2—in this case—produced data that were more well-behaved. Following this, the first-stage RFI flagging is done, performed on the entire 2048 MHz band, minus those edge channels that have already been flagged. There is further flagged done to end channels that show significant RFI, and we are finally left with a 1716 MHz band, which is subsequently split into four 429 MHz sub-bands.

The following calibration steps are outlined in Fig. iii.3. To begin, MFCAL corrects the bandpass shape of the flux calibrator by comparing the observed shape with the expected shape. GPCAL follows which calibrates the antenna response, and then we pass through a round of RFI flagging. The flagging is done with both the task PGFLAG, using an implementation of the SUMTHRESHOLD method (Offringa et al., 2012) in a manual and automated fashion, and the task BLFLAG removing contaminating visibilities manually. This sequence is repeated until the visibilities are free of any obvious RFI.

Once the primary calibrator is sufficiently flagged and calibrated, we copy the calibration tables to the secondary with GPCOPY and perform the same RFI flagging strategy. Following this, GPBOOT is used to rescale the flux density. These calibration tables are then copied to the source and antenna gains are averaged using GPAVER. Similar to the calibrators, initial RFI flagging is then done, and the sub-bands are then split in two, returning the final eight sub-bands of 214 MHz. As phase errors were present in preliminary images, we use UVAVER to remove visibilities corresponding to baseline-hourangle pairs that were showing such errors. A final found of RFI flagging is done before we move to the imaging process.

§iii.1.3.2. Imaging the data

The imaging process follows from the calibration. As the bandwidth is large (originally 2 GHz) we split this into eight sub-bands of 214 MHz. This number of sub-bands is chosen to determine where phase errors might occur over the entire bandwidth more easily. We find that a number of the bands feature errors due to phase issues, which are somewhat fixed by culling visibilities on certain baseline-hourangle pairs. Once we were satisfied that the remaining visibilities were free of the most problematic errors—likely from time-dependent RFI—the actual imaging
begins.

For each final sub-band, the imaging process is outlined in Fig. iii.4. We follow a standard imaging process, first using invert to go from visibility space to image space via Fourier transforms. In this instance, we use natural robust 0 weighting in the Briggs weighting scheme in an attempt to enhance any diffuse emission (Briggs, 1995). We follow this with various iterations of deconvolution via cleaning, involving clean and the multi-frequency equivalent, mfclean. These cleaning tasks use an adaptation of the Clark (1980) method, which itself is based on the method of Högbom (1974). The first clean stage is used to get a model to allow for self-calibration with the task selfcal, which uses sources within the field above a user-specified clip-level to perform both phase and amplitude calibration. This is performed twice, with the second round using a lower clip level. The second round of cleaning, which involves the second round of self-calibration, using the task mfclean with two iterations. The first uses a targeted clean around the most confusing source in the image. This happens to be a HT galaxy next to our source-of-interest. The extended structure in the HT galaxy’s tail is particularly confusing for the clean process, and the brightness of the source overall compounds this. The second iteration of mfclean performs a blanket clean over the inner portion of the image. This effectively cleans around all but the brightest sources. After the second round of self-calibration, we perform one more round of mfclean and finally use the task restor to combine the clean model, synthesized beam, and dirty map produced by the task invert to make a real image.

We produced a stacked image of the region centred on $\sim2.1$ GHz by first convolving the images to the lowest band’s resolution and using the task linmos to perform linear mosaicing. We present this image in Fig. iii.5 and iii.6. To complement this image, we also produce a similar stacked image made from tapered sub-band images. The imaging process for these is simple as it only involves one
Table iii.2: Sub-band properties for the ATCA observations of Abell S1136. The band is the frequency named by Miriad after uvsplit and the central frequency, $\nu_c$, is the frequency embedded in the FITS file. We use $\nu_c$ for calculations. The rms noise is calculated using BANE on cropped images of the central $\sim$1 degree of the field, and is the rms at the reference pixel of the image.

<table>
<thead>
<tr>
<th>Image</th>
<th>Central frequency (MHz)</th>
<th>Restoring beam ($'' \times ''$, $^\circ$)</th>
<th>$\sigma_{\text{rms}}$ (mJy beam$^{-1}$)</th>
<th>Core flux (mJy)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1413</td>
<td>1408.5</td>
<td>$19.31 \times 4.49$, $-24.3$</td>
<td>209.11</td>
<td>0.85 ± 0.21</td>
</tr>
<tr>
<td>1629</td>
<td>1672.0</td>
<td>$16.5 \times 3.78$, $-24.1$</td>
<td>240.96</td>
<td>1.00 ± 0.23</td>
</tr>
<tr>
<td>1845</td>
<td>1839.8</td>
<td>$13.6 \times 3.53$, $-23.2$</td>
<td>170.39</td>
<td>0.57 ± 0.15</td>
</tr>
<tr>
<td>2059</td>
<td>2040.5</td>
<td>$12.08 \times 3.13$, $-23.2$</td>
<td>131.72</td>
<td>0.45 ± 0.12</td>
</tr>
<tr>
<td>2274</td>
<td>2274.5</td>
<td>$10.28 \times 2.61$, $-22.2$</td>
<td>75.16</td>
<td>0.51 ± 0.08</td>
</tr>
<tr>
<td>2488</td>
<td>2495.0</td>
<td>$9.59 \times 2.45$, $-22.7$</td>
<td>69.52</td>
<td>-</td>
</tr>
<tr>
<td>2703</td>
<td>2726.6</td>
<td>$10.21 \times 2.46$, $-27.7$</td>
<td>57.91</td>
<td>-</td>
</tr>
<tr>
<td>2917</td>
<td>2917.6</td>
<td>$9.33 \times 2.25$, $-27.8$</td>
<td>42.37</td>
<td>-</td>
</tr>
<tr>
<td>Stacked</td>
<td>2114.0</td>
<td>$19.31 \times 4.49$, $-24.3$</td>
<td>116.67</td>
<td>-</td>
</tr>
<tr>
<td>Stacked $^a$</td>
<td>2097.9</td>
<td>$77.07 \times 20.25$, $-51.5$</td>
<td>5000</td>
<td>-</td>
</tr>
</tbody>
</table>

$^a$ Stacked after tapering sub-bands with a 30 arcmin Gaussian.

round of CLEAN. Tapering is done during the inversion from visibility space, where we apply a Gaussian taper of 30 arcmin by 30 arcmin when performing the Fast Fourier Transform (FFT) within the task INVERT. This tapering is done in an attempt to bring out any low-surface-brightness diffuse emission that is seen at low frequencies, where the diffuse emission may be seen for the same reason that more emission is seen within the EoR0 field image than in TGSS—high resolution images can resolve out diffuse flux from a radio map.

§iii.1.4. Results with the ATCA

After the imaging process, we are left with 8 sub-bands between 1.1 and 3.1 GHz. Table iii.2 summarises the sub-band images. In no band is the diffuse emission seen. In the stacked image shown in Fig. iii.6 we do not see even a hint of the emission, however it is clear that there are a number of intruding point sources. One of the motivations for the observation with the ATCA was to determine the spectral index of the proposed core of the emission, ESO 470-G020. We see the core above 4$\sigma_{\text{rms}}$ in 5 of the 8 sub-bands, and measure the integrated flux densities using the in-house PYTHON code. Fig. iii.7 shows the SED within these sub-bands for the core, and the spectral index is calculated to be $\alpha = -1.39 \pm 0.55$. The data are not well behaved and this is likely due to a combination of poor signal-to-noise for the core and perhaps subtle side-lobe artefacts from the nearby HT. We note that further source measuring in this region will produce similar results, and since the diffuse emission is so much brighter than these point sources attempting to subtract the three interloping sources would not increase the accuracy of the
current spectral index measurement within the GLEAM bands, and would require assumptions on the SEDs of each of the three point sources and the diffuse emission itself.

Fig. iii.6 shows the stacked and tapered ATCA images of the cluster. The top panel shows the final stacked image with no tapering, with a single contour of the EoR0 and TGSS images at 10 mJy beam$^{-1}$ (red and black). The bottom panel shows the tapered, stacked image, with contours showing both the TGSS (black) and the non-tapered, stacked ATCA image (red). There is no hint of diffuse emission in this tapered image, though due to side-lobe noise from the bright HT, this is not particularly surprising as any emission may be lost within this noise.

§iii.1.5. Discussion and conclusion on the nature of the emission within Abell S1136

The emission as seen at low radio frequencies and resolutions (e.g. across the GLEAM bands and within the EoR0 field) is suggestive of some sort of relic AGN
Figure iii.6: Top: The stacked radio image of Abell S1136 centred on 2.1 GHz. The single red contour is of the 168 MHz MWA data, and the single black contour is of the 147.5 MHz TGSS data; both contours at 10 mJy beam$^{-1}$. Bottom: The stacked, tapered radio image, with contours as in Fig. iii.5. The red ellipses in the bottom-left corner of each image are at the size of the synthesized beam of the respective image. The linear scale is at the redshift of the cluster.
Figure iii.7: The SED of ESO 470-G020 with flux densities from Table iii.2. The core is incredibly faint, and is barely detected in most bands. The three bands not used do not detect the core above $4\sigma_{\text{rms}}$. The shaded region represents the 95 percent confidence interval to the fit as in Fig. ii.32.

emission, with tentative lobe-like structure. The TGSS data confirms this, showing a peak at the emission where a possible core galaxy, ESO 470-G020 resides. Other peaks in the TGSS emission do not show optical hosts and are likely the old hotspots of the relic AGN emission. After performing follow-up observations of the cluster with the ATCA in the 16 cm band, we confirm the presence of a core with weak radio activity and a steep spectral index, likely in its last stages of life. The core is associated with the giant elliptical ESO 470-G020 as expected, and we see another two point sources that are embedded within the diffuse emission nearby, one associated with 2MASX J23361598-3135345 (north with respect to ESO 470-G020) and one previously undetected (south with respect to ESO 470-G020). The likeliest scenario for the origin of the emission is from the BCG of the cluster, ESO 470-G020, and relic AGN emission from a central galaxy is consistent with other findings of such dead radio galaxies (e.g. Murgia et al., 2011).
Figure iii.8: The RGB image of Abell S1063 presented in §ii.2.2.20 contours overlaid as follows: EoR0, white, beginning at 50 mJy beam$^{-1}$ increasing by a factor of $\sqrt{2}$; SUMSS, red, beginning at 5 mJy beam$^{-1}$ increasing by a factor of 2; TGSS, medium purple, beginning at 7.8 mJy beam$^{-1}$ also increasing by a factor of 2. The dashed circle is centred on the cluster and has a radius of 1 Mpc. The white box indicates the BCG of the cluster.

§iii.2. Diffuse emission within Abell S1063

The nature of the cluster (massive and X-ray luminous) would suggest a halo may be present, and the estimated spectral index of the emission agrees with this hypothesis. However, the morphology of the emission is more reflective of a HT galaxy with a blended point source possibly associated with the BCG, LCRS B224549.3-444744. The cluster has been observed with the ATCA in 2013 with the EW352 configuration (Project code C2837, PI M. Johnston-Hollitt) in a search of diffuse cluster emission from clusters in the South Pole Telescope survey (SPT: Song et al., 2012; Reichardt et al., 2013) though the data had not yielded unambiguous diffuse emission. We use these data in conjunction with observations in the 6A configuration (Project code C2585, PI R. Kale) obtained from the Australia Telescope Online Archive (ATOA) to fully explore the cluster’s emission in the frequency range 147.5–3100 MHz. Table iii.3 summarises the properties of the observations used in this work.
§iii.2.1. ATCA data of Abell S1063

The reduction of ATCA data follows standard procedures of CABB continuum data reduction with MIRIAD outlined in §iii.1.3.

In the data processing, Dr. Qian Zheng first flagged and removed RFI then further flagging the edge channels that are within the bandpass rolloff, as the filters on the correlator have an area of approximately 32 MHz on each side with lessened sensitivity. PKS B1934-638 was used as the bandpass and flux calibrator for both configurations, PKS B2326-477 was the phase calibrator for the EW352 configuration and MRC 2117-614 was the phase calibrator for the 6A configuration. The dataset was split into four sub-bands of 512 MHz width, approximately centred at 1332, 1844, 2356, and 2868 MHz.

At this point the data are passed on to the author of this work, and a similar imaging process is followed as outlined in §iii.1.3 (see Fig. iii.4). In the Briggs robust weighting scheme, natural weighting 0 is used in an attempt to enhance any low–surface-brightness, diffuse emission. The multi-frequency clean task mfclean is used for deconvolution using the Clark method. Each sub-band goes through two passes of amplitude and phase self-calibration using the task selfcal. The first pass utilises a higher clip level of 50 mJy beam$^{-1}$ for the lower three bands and 10 mJy beam$^{-1}$ for the highest. The second pass uses a lower clip value of 1 mJy beam$^{-1}$. A single pass of mfclean is used between each round of self-calibration, where each self-calibration and clean stage uses previously generated clean model as a prior. Finally the sub-bands are convolved to the synthesized beam of the lowest frequency band and stacked using the task LINMOS. In this case, it is used to increase the signal-to-noise ratio in the final, stacked 2100 MHz image. This stacked image has an rms noise of 21 µJy beam$^{-1}$ at the centre, increasing out towards the edges of the image. Table iii.4 summarises the sub-band images, on which we perform measurements. Fig. iii.9 shows the stacked sub-bands convolved to the resolution of the 1332 MHz sub-band centred on approximately 2100 MHz (top panel) and the stacked image after tapering with a 60 arcmin Gaussian beam during the FFT process (bottom panel).

§iii.2.2. Analysis of the central cluster region

The core of the cluster features four radio sources detected in the ATCA images: The BCG of the cluster, LCRS B224549.3-444744 (Obj. A in Fig. iii.9, the
Figure iii.9: Abell S1063. Top: ATCA stacked image of the 1100–3100 MHz band centred on 2100 MHz overlaid with contours as follows: EoR0, black, beginning at 40 mJy beam$^{-1}$; ATCA, red, beginning at 72 µJy beam$^{-1}$. The red ellipse in the top-right corner is the size of the synthesized beam. Bottom: Stacked, tapered ATCA image of the same band. The EoR0 contours are as in the bottom panel, with ATCA contours in red, beginning at 1.08 mJy beam$^{-1}$. The red ellipse in the bottom-left corner is the size of the synthesized beam. ATCA contours in both images are increasing with factors of 2 and the EoR0 contours increase with factors of $\sqrt{2}$. The linear scale is at the cluster’s redshift.
Table iii.4: Sub-band and image properties for the ATCA observations of Abell S1063. The rms noise is calculated using BANE and is for the centre of the image.

<table>
<thead>
<tr>
<th>Image</th>
<th>Centre frequency (MHz)</th>
<th>Restoring beam (″ × ″, ′′)</th>
<th>$\sigma_{\text{rms}}$ (μJy beam$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1332</td>
<td>1384</td>
<td>9.95 × 4.45, −3.1</td>
<td>50</td>
</tr>
<tr>
<td>1844</td>
<td>1873</td>
<td>7.57 × 3.89, 1.5</td>
<td>21</td>
</tr>
<tr>
<td>2356</td>
<td>2349</td>
<td>6.10 × 3.15, 0.0</td>
<td>22</td>
</tr>
<tr>
<td>2868</td>
<td>2811</td>
<td>5.13 × 2.74, −4.0</td>
<td>26</td>
</tr>
<tr>
<td>Stacked</td>
<td>2034</td>
<td>9.95 × 4.45, −3.1</td>
<td>18</td>
</tr>
<tr>
<td>Stacked $^a$</td>
<td>2251</td>
<td>122.9 × 40.1, −17.7</td>
<td>360</td>
</tr>
</tbody>
</table>

$^a$ Stacked after tapering sub-bands with a 60 arcmin Gaussian.

Figure iii.10: The central galaxies of Abell S1063. The background image is a three-colour image made using the HST F814W, F606W, and F435W bands corresponding to red, green, and blue respectively. The HST data is obtained from the Mikulski Archive for Space Telescopes (MAST) from project 14037, PI Lotz. The single white contour is at the 3$\sigma_{\text{rms}}$ level of the stacked ATCA image, and the linear scale is at the redshift of the cluster. The labels are as in the top panel of Fig. iii.9, though note that north is not directly up, which gives a rotation compared to Fig. iii.9. The blue arcs are lensed background galaxies. The spiral (B) shows no lensing in this image.
central elliptical of Fig. iii.10, is detected in each band, along with the source SUMSS J224845-443025 (Obj. C and D). From the SUMSS and TGSS images it would appear that Obj. D is in fact the core of a HT galaxy, with Obj C its tail. However, upon inspection of the higher resolution ATCA images, we see that the tail is a discrete extended source. This source does not have an optical ID, nor are there sources in NED listed at the peak of the radio emission. The source lies on edge of the X-ray emission from the cluster’s centre. For SUMSS J224845-443025 we use AEGEAN to measure the integrated flux density in each sub-band, yielding a spectral index of $\alpha^{2868}_{1332} = -1.11 \pm 0.19$, where flux density measurements have an uncertainty as in Eq. ii.1 but with a 10 per cent term as is typical of the ATCA instead of 5 per cent (plus calibration uncertainty) for the EoR0 field. Fig. iii.10 shows a close-up of the cluster centre, including LCRS B224549.3-444744 and Obj. B, which in this three-colour Hubble Space Telescope (HST) image is shown to be a spiral galaxy with radio emission. This spiral is likely the GALAXSC source, GALEX ASC J224841.77-443157.0, which is considered a lensed background galaxy (Gómez et al., 2012), however this spiral does not show lensing characteristics and likely this association with a lensed galaxy can be attributed to the image being used not having quite the same fidelity as the more recent HST images.

§iii.2.3. Conclusion on the nature of the emission within Abell S1063

The high resolution ATCA images confirm that there are embedded point sources within the emission seen at 168 MHz in the EoR0 field. These sources trace the emission seen in SUMSS and the TGSS, though the previous notion that SUMSS J224845-443025 was a HT galaxy is dispelled. While a diffuse cluster halo may be present, it is—with the current data—rendered undetectable. Given that cluster may have recently gone through a merger (Gómez et al., 2012) and its high X-ray luminosity (equivalent to the Bullet Cluster, 1E 0657-56; see e.g. Liang et al., 2000; Markevitch, 2006; Shimwell et al., 2014; Srinivasan, 2015) it was expected that Abell S1063 might host a halo.
§iii. A curious AGN host

While inspecting the cluster Abell 2685, a radio galaxy with curious morphology, akin to a rose, was observed nearby.

§iii.3. Disk galaxies hosting AGN

Disk galaxies with prominent dust are not typically found to host powerful AGN (see e.g. Abdo et al., 2009), however in rare circumstances have been observed (e.g. the host galaxy of Fornax A, NGC 1316; Dreyer, 1888; Burbidge and Burbidge, 1957). In particular, double-lobed radio sources associated with powerful AGN are seldom seen in such galaxies, and it is thought that the feeble amount of dust in typical ellipticals is what allows the jets to form. Disk galaxies—in particular, spirals—have been seen to produce small jets from a central black hole, classed as Seyfert AGN (Seyfert, 1943; Gallimore et al., 2006; Ulvestad et al., 1981) of various types. This small-scale emission does not typically extend much beyond the optical extent of the host galaxy, and the power is much lower than in normal double-lobed radio galaxies. It is likely the powerful AGN seen are the results of mergers that have created the elliptical galaxies (e.g. Hopkins et al., 2006; Chiaberge and Marconi, 2011). However, there are a small but growing number of spiral galaxies found to host large double-lobed AGN. In this section, we present a curious spiral host of large-scale double-lobed radio emission: ESO 472-G013.

§iii.3.2. The curious host: ESO 472-G013

The galaxy ESO 472-G013 is unambiguously classified as a spiral (SB: Lauberts 1982; S: Loveday 1996; SBbc: Paturel et al. 2003) in the literature, though this morphology is not inherently clear in the DSS2 images alone. ESO 472-G013 is detected as part of the 6-degree Field Galaxy Survey (6dFGS; Jones et al., 2004) and is reported to have a redshift of $z = 0.050718 \pm 0.000150$ (Jones et al., 2009). The galaxy hosts an AGN, with prominent emission from its core as well as a double-lobed structure. The northern lobe appears highly disturbed, which is unusual for a galaxy not part of a galaxy cluster or not within any significantly dense medium. The southern lobe appears much less grandiose in size as well as morphology, though likely this due to projection effects as the southern lobe may be angled away from the observer. Separated by $\sim 112$ arcsec ($\sim 111$ kpc) is ESO 472-G012, which is also a spiral galaxy (S: Lauberts 1982; Sbc: Paturel et al. 2003) and has a redshift of $z = 0.052193 \pm 0.000053$ (di Nella et al., 1996). ESO 472-G012 shows no peculiar characteristics for a spiral and hosts no detectable radio emission. We mention this companion here due to the close proximity to ESO 472-G013, and discuss in §iii.3.7 the possible interaction between the two spiral galaxies. Another spiral, AM 2356-245 lies 13.8 arcmin away, with a redshift of $z = 0.051422 \pm 0.000150$ (Jones et al., 2009) which shows a one-armed morphology. There are no observable clusters or group within the region at the redshift of ESO 472-G013.
§iii.3.3. Visible and ultraviolet wavelengths

Fig. iii.11 shows a three-colour DSS2 image with radio contours overlaid. ESO 472-G013 is clearly seen at the centre of the image with its companion ESO 471-G012. The spiral nature is not clear from the DSS2 image, instead an irregular morphology is more apparent; deferring classification to the aforementioned publications assuming authors had access to higher fidelity data. If the spiral classification is correct, we see that the lobes of the radio galaxy align approximately perpendicularly to the disk, consistent with previously detected double-lobed spirals. The close companion shows clear barred spiral structure in the DSS2 image, though itself does not feature significant radio emission.

ESO 472-G013 is detected in both the near- and far-ultraviolet (NUV and FUV) bands of the *Galaxy Evolution Explorer* (*GALEX*; Martin et al., 2005) All-sky Imaging Survey (AIS). Both ESO 472-G013 and ESO 472-G012 show significant emission in the bands bands, with ESO 472-G012 showing greater intensity in both. We obtain the NUV and FUV magnitudes for ESO 472-G013 from the *GALEX* AIS catalogue ¹: $\text{MAG}_{\text{NUV}} = 19.45 \pm 0.09$ and $\text{MAG}_{\text{FUV}} = 21.24 \pm 0.26$. We also obtain corresponding flux densities: $S_{\text{NUV}} = 60.4 \pm 5.1 \, \mu\text{Jy}$ and $S_{\text{FUV}} = 11.6 \pm 2.8 \, \mu\text{Jy}$.

¹http://galex.stsci.edu/GalexView/
§iii.3.4. At radio wavelengths

§iii.3.4.1. Radio flux density

The emission was first noticed within the EoR0 field, though we use the GLEAM survey to measure its low-frequency (and resolution) properties. We measure radio flux densities using the custom-built PYTHON code (see Appendix A), which simply sums pixel flux values and corrects for the beam area. An associated error is given as in Eq. ii.1, however for GLEAM at this declination uncertainty in the flux scaling is 8 per cent (Hurley-Walker et al., 2017). Fig. iii.12 shows the GLEAM 200 MHz image with GLEAM, NVSS, and TGSS contours overlaid. Note that despite an expected steeper spectral index for the lobes, the TGSS emission does not trace the entire lobe structure, likely due to lack of sensitivity to flux from extended sources.

We measure the flux density of the combined core and lobe emission at each of the 20 GLEAM narrow bands with the PYTHON code. Prior to this we estimate the noise statistics in each image using BANE. The rms noise of each of the narrow band GLEAM images varies, from 12–65 mJy beam$^{-1}$ for the highest- and lowest-frequency bands respectively. In measuring the flux densities, we use a $3\sigma_{\text{rms}}$ cutoff, where only pixels above this value are included as part of the source. Table iii.5
Table iii.5: The measured flux densities across the narrow GLEAM bands of the radio emission from ESO 472-G013. The central frequency, $\nu_c$, is that given within the FITS header of the GLEAM images, and $\sigma_{\text{rms}}$ for each band is calculated by BANE at the coordinates of ESO 472-G013.

<table>
<thead>
<tr>
<th>Band</th>
<th>$\nu_c$ (MHz)</th>
<th>$S_\nu$ (mJy)</th>
<th>$\sigma_{\text{rms}}$ (mJy beam$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>072-080</td>
<td>76.2</td>
<td>1815 ± 184</td>
<td>65.0</td>
</tr>
<tr>
<td>080-088</td>
<td>87.7</td>
<td>1569 ± 138</td>
<td>30.4</td>
</tr>
<tr>
<td>088-095</td>
<td>83.8</td>
<td>1629 ± 157</td>
<td>49.0</td>
</tr>
<tr>
<td>095-103</td>
<td>91.5</td>
<td>1317 ± 132</td>
<td>45.8</td>
</tr>
<tr>
<td>103-111</td>
<td>99.2</td>
<td>1183 ± 120</td>
<td>40.8</td>
</tr>
<tr>
<td>111-118</td>
<td>106.9</td>
<td>1277 ± 126</td>
<td>38.5</td>
</tr>
<tr>
<td>118-126</td>
<td>118.4</td>
<td>1235 ± 106</td>
<td>16.7</td>
</tr>
<tr>
<td>126-134</td>
<td>114.6</td>
<td>1187 ± 113</td>
<td>31.0</td>
</tr>
<tr>
<td>139-147</td>
<td>122.2</td>
<td>1140 ± 109</td>
<td>29.1</td>
</tr>
<tr>
<td>139-170</td>
<td>129.9</td>
<td>961 ± 93</td>
<td>26.0</td>
</tr>
<tr>
<td>147-154</td>
<td>142.7</td>
<td>955 ± 92</td>
<td>23.9</td>
</tr>
<tr>
<td>154-162</td>
<td>154.2</td>
<td>953 ± 81</td>
<td>11.0</td>
</tr>
<tr>
<td>162-170</td>
<td>150.4</td>
<td>858 ± 82</td>
<td>20.8</td>
</tr>
<tr>
<td>170-177</td>
<td>158.1</td>
<td>863 ± 83</td>
<td>20.2</td>
</tr>
<tr>
<td>177-185</td>
<td>165.8</td>
<td>812 ± 78</td>
<td>18.9</td>
</tr>
<tr>
<td>185-193</td>
<td>173.4</td>
<td>808 ± 77</td>
<td>17.8</td>
</tr>
<tr>
<td>193-200</td>
<td>200.3</td>
<td>832 ± 70</td>
<td>6.8</td>
</tr>
<tr>
<td>200-208</td>
<td>181.1</td>
<td>775 ± 75</td>
<td>18.0</td>
</tr>
<tr>
<td>208-216</td>
<td>188.8</td>
<td>734 ± 70</td>
<td>15.9</td>
</tr>
<tr>
<td>216-223</td>
<td>196.5</td>
<td>733 ± 70</td>
<td>15.1</td>
</tr>
<tr>
<td>223-231</td>
<td>204.2</td>
<td>745 ± 69</td>
<td>14.0</td>
</tr>
</tbody>
</table>
summarises the measured flux densities across the narrow GLEAM bands.

We check the NVSS catalogue (Condon et al., 1998) for flux densities of the emission. The NVSS catalogue breaks the emission into four components: NVSS J235925-242351 and NVSS J235916-242432 for the northern lobe; NVSS J235927-242707 for the southern lobe; and NVSS J235926-242530 for the core. The sum of flux densities from these sources is $201.9 \pm 6.9$ mJy, which we compare to the flux density as measured by the in-house code which gives $194 \pm 3$ mJy with a cutoff of $3\sigma_{\text{rms}}$. The values agree within their uncertainties and we use the lower measured value for the total emission to be consistent with our measured flux densities across the GLEAM bands. We do however use the NVSS catalogue measurement for the core: $87.5 \pm 3.1$ mJy. We also obtain from the literature the 8.4 GHz flux density of the core from the Combined Radio All-Sky Targeted Eight GHz Survey (CRATES; Healey et al., 2007), and the 147.5 MHz flux density of the core from the TGSS (Intema et al., 2016). Despite the coverage of the VLA Low-frequency Sky Survey (redux, VLSSr; Lane et al., 2014) we do not obtain a flux measurement at 74 MHz as the flux density scale of the VLSSr below 1 Jy differs sporadically up to approximately 30 per cent.

§iii.3.4.2. Spectral energy distribution from 72–8400 MHz

We make use of the GLEAM narrow bands and the fine sampling provided over the frequency range 72–231 MHz to estimate the average, integrated spectral index of ESO 472-G013. Due to the low resolution of the GLEAM images in comparison to other surveys such as NVSS and TGSS, we are only able to measure the average spectral index of the entire emission, rather than the core and jets separately. Fig. iii.13 shows the SED between 72–1400 MHz, with the 1.4 GHz measurement the sum of the lobes and core components, and the 72–231 MHz GLEAM measurements are of the entire emission. We fit the GLEAM measurements separately as well, which are fit well with a single power law. However, with the inclusion of the 1.4 GHz measurement we find that the simple power law is no longer valid. As the 1.4 GHz measurement is not below the fits of the GLEAM bands, we do not consider that the NVSS imaging has resolved out any of the diffuse emission of the lobes. Instead, we consider that the SED is more complex than a simple power law. The average spectral index is typical of most radio galaxies though the spectral index of the core is lower than average for spirals (e.g. $\langle \alpha \rangle = 0.74 \pm 0.12$; Gioia et al., 1982, though this is not for spirals with radio-loud AGN). We find that the core is separated out in the 8.4 GHz or 147.5 MHz measurements of CRATES and the TGSS, as well as the 1.4 GHz measurements of the NVSS. We fit these data to obtain the spectral index of the core of $\alpha_{\text{core}} = -0.555 \pm 0.003$. With this spectral index we calculate the 1.4 GHz power of the core to be $P_{1.4} = (5.21 \pm 0.19) \times 10^{23}$ W Hz$^{-1}$.

The top panel of Fig. iii.14 shows the spectral index map of the emission around ESO 472-G013, calculated across the individual narrow GLEAM bands. The bottom panel shows the corresponding spectral index uncertainty map. The spectral
Figure iii.13: Flux density against frequency for the radio emission associated with ESO 472-G013. We show the fit to the GLEAM emission alone (dotted line), as well as the same data with the addition of the 1.4 GHz NVSS point (solid line). This represents the emission from the core and lobes combined. The third fit is to the three measurements of the core only (dashed line). The shaded regions represent 95 per cent confidence intervals for the fits, as in Fig. ii.32. From this we see the GLEAM emission is dominated by the lobes, which have a steeper spectral index than the core.
Figure iii.14: Top: The spectral index map of the region around ESO 472-G013 across the 20 narrow GLEAM bands, from 72 to 231 MHz. The overlaid white, dotted contours are of the 1.4 GHz NVSS image, starting at 1.5 mJy beam$^{-1}$ and increasing with a factor of 2 for clarity, and a black, solid contour indicating the 3σrms level of the 200 MHz GLEAM image. Bottom: As in the top panel except the background is the spectral index uncertainty map.
Figure iii.15: 325 MHz rest-frame power against the largest-linear scale for radio galaxies. ESO 472-G013 is represented by an upward-pointing triangle, and other disk galaxies are downward-pointing triangles. The sample of FR-I and FR-II sources shown as circles was compiled by Laing et al. (1983). GRGs compiled by Saripalli et al. (2005) are shown as squares, GRGs reported by Schoenmakers et al. (2001; but see also Schoenmakers et al., 2000), and diamonds are those GRGs compiled in Schoenmakers et al. (2001; see references therein) reported prior to 1998. The cosmology used here is as in Hurley-Walker et al. (2015): a flat ΛCDM cosmology with $H_0 = 73 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.27$, and $\Omega_\Lambda = 0.73$.

index map is produced by first convolving and regridding GLEAM narrow-band images to the resolution and pixel size of the lowest frequency band (72–80 MHz). This is done using MIRIAD Sault et al. (1995) with tasks CONVOL and REGRID respectively. The FWHM and phase angle for CONVOL are chosen such that the final beam size for the resultant images matched that of the 72–80 MHz band and REGRID used 72–80 MHz band as a template. Due to the low resolution of the 72–80 MHz GLEAM band, the final spectral index map is not able to clearly show the core and lobes as distinct emission, rather blending it all together. Despite this Fig. iii.14 shows steepening towards the edges of the lobes, in the regions farthest from core. This is consistent with typical radio galaxies, where lobes tend towards steeper spectral indices than the cores. The uncertainties in the spectral index calculations increase towards the edges of the emission, and this apparent steepening does not fall outside of these uncertainties.
Table iii.6: Magnitudes and flux densities as measured by WISE across the four bands, W1–4.

<table>
<thead>
<tr>
<th>Band</th>
<th>λ (µm)</th>
<th>MAG (mag)</th>
<th>$S_\nu$ (mJy)</th>
<th>$\nu L_\nu$ ($\times 10^9$ L$_\odot$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>W1</td>
<td>3.4</td>
<td>11.407 ± 0.023</td>
<td>8.31 ± 0.22</td>
<td>-</td>
</tr>
<tr>
<td>W2</td>
<td>4.6</td>
<td>11.200 ± 0.021</td>
<td>5.61 ± 0.14</td>
<td>-</td>
</tr>
<tr>
<td>W3</td>
<td>12</td>
<td>8.634 ± 0.025</td>
<td>9.37 ± 0.26</td>
<td>3.42 ± 0.10</td>
</tr>
<tr>
<td>W4</td>
<td>22</td>
<td>6.876 ± 0.086</td>
<td>14.6 ± 1.2</td>
<td>2.90 ± 0.23</td>
</tr>
</tbody>
</table>

§iii.3.4.3. The P–D diagram

We use the spectral index calculated with the GLEAM bands, $\alpha = -0.91 ± 0.04$, to extrapolate to a 325 MHz rest-frame power of $P_{325} = (2.56 ± 0.09) \times 10^{24}$ W Hz$^{-1}$. Fig. iii.15 shows the 325 MHz power against largest-linear size of double-lobed radio sources, adapted from Schoenmakers et al. (2001). We add disk galaxies hosting large-scale radio lobes as in Hurley-Walker et al. (2015), which are shown as down-pointing triangles. We include ESO 472-G013 (up-pointing triangle) and find that it sits in the low-power, small-size quadrant of the plot. This location is consistent with previously detected disk galaxies hosting large-scale radio lobes which lie between $10^{24}–10^{26}$ W Hz$^{-1}$ and cover a range of linear sizes and redshifts.

§iii.3.5. At mid-infrared wavelengths

ESO 472-G013 is detected in the four bands of WISE. The bands W1, W2, W3, W4 correspond to 3.4, 4.6, 12, 22 µm respectively. We query the AllWISE catalogue (see Cutri et al., 2013) to obtain the W1–4 magnitudes and convert these to flux densities in Jy based on the relation

$$S_\nu = S_{\nu 0} 10^{-0.4MAG_{\nu}} \text{ [Jy]},$$

where $S_{\nu 0}$ is the frequency-dependent flux density associated with the so-called zero-magnitude, which corresponds to the Vega-calibrated WISE magnitudes, and MAG is the magnitude at a given frequency. A per-band correction is then applied which scales each band based on the in-band spectral index (see Wright et al., 2010; Cutri et al., 2013, though note that notation used here differs). Magnitude measurements are thus converted to flux densities and Table iii.6 summarises the magnitudes, calculated fluxes, and luminosities for selected bands.

§iii.3.6. Star-formation rates

There exists empirical relationships between infrared, radio, and ultraviolet luminosities of star-forming galaxies and their associated star-formation rates (see e.g.
Figure iii.16: The WISE colour-colour plot, taken from Yan et al. (2013) with minor aesthetic editing. We add the location of ESO 472-G013, indicated by a pink star, which finds itself within the intersection of Seyfert AGN and star-forming galaxies (purple and blue contours respectively).

Lequeux 1971, Kennicutt 1983a, Kennicutt 1983b, Condon 1992). In the case of radio, star-formation is related to the radio emission from SNRs and is usually only calculated for stars with masses above $\sim 5 \, M_\odot$ (see Condon, 1992, for a review). In the far- and mid-infrared, the emission arises due to re-radiation of light absorbed by interstellar dust, likely originating in the optical regime from young stars (Harwit and Pacini, 1975; Johnson et al., 2007), and the ultraviolet traces directly the emission from the same young stars (e.g. Meurer et al., 1995, 1999). SFR measurements between the three methods tend to show deviation, especially when not all radio emission can be attributed to star-formation as in the case of an AGN, where the AGN will cause an overestimate in the radio SFR due to the abundance of synchrotron radiation emitted following the rotation axis of the central black hole. Infrared and ultraviolet may suffer similar overestimates, but these will be much lower than an estimate of the SFR using the 1.4 GHz luminosity for radio-loud AGN.

To determine the SFR of ESO 472-G013, we first look at the infrared WISE images. It is important to note that corrections when converting to flux density from magnitudes are on the order of one part per thousand, and do not substantially affect the estimation of SFR, especially considering the uncertain nature of SFR estimation. Table iii.6 summarises the magnitudes and flux densities of each band. Yan et al. (2013) use colour-colour plots using the WISE bands to explore where different types of galaxies (e.g. star-forming, AGN) lie with respect to each other. Importantly, this gives a qualitative incentive to consider a galaxy as star-forming. We find that ESO 472-G013 has colours $W1 - W2 = 0.21 \pm 0.03$ and $W2 - W3 = 2.57 \pm 0.03$. Fig. iii.16 shows the location of ESO 472-G013 on the colour-colour diagram of Yan et al. (2013), sitting within the intersection of star-forming and Seyfert galaxies. Thus, we have an incentive to estimate the
SFR.

To determine the SFR using mid-infrared data, we use the relations presented by Jarrett et al. (2013) (their Equations 1 and 2), which utilise the W3 and W4 bands. These are

\[
SFR_{12} = 4.91(\pm 0.48) \times 10^{-10} \frac{L_{12}}{L_{\odot}} \quad [M_{\odot} \text{yr}^{-1}], \quad (\text{iii.2})
\]

\[
SFR_{22} = 7.50(\pm 0.08) \times 10^{-10} \frac{L_{22}}{L_{\odot}} \quad [M_{\odot} \text{yr}^{-1}], \quad (\text{iii.3})
\]

where the solar luminosity is \( L = 3.839 \times 10^{33} \text{ W} \). We find that \( SFR_{12} = 1.68 \pm 0.11 \ M_{\odot} \text{ yr}^{-1} \) and \( SFR_{22} = 2.17 \pm 0.18 \ M_{\odot} \text{ yr}^{-1} \). While there is disagreement between these two values, SFR estimations are inherently uncertain, and we consider that this reflects a range of possible values for the true SFR, giving \( 1.68(\pm 0.11) \leq SFR_{\text{MIR}} \leq 2.17(\pm 0.18) \ M_{\odot} \text{ yr}^{-1} \) for the mid-infrared SFR. The radio SFR is estimated from the 1.4 GHz flux density of the core only. We use

\[
SFR_{1.4} = \frac{L_{1.4}}{4 \times 10^{21} \text{ W Hz}^{-1}} \quad [M_{\odot} \text{yr}^{-1}], \quad (\text{iii.4})
\]

from Hopkins (1998) adapted from (Condon, 1992). From the NVSS catalogue, to core is measured to have a flux density of \( 87.5 \pm 3.1 \text{ mJy} \) (Condon et al., 1998) from which we calculate the 1.4 GHz power to be \( (5.23 \pm 0.19) \times 10^{23} \text{ W Hz}^{-1} \). With this we estimate the radio SFR of \( 131 \pm 5 \ M_{\odot} \text{ yr}^{-1} \). This is significantly higher than that calculated with the mid-infrared \textit{WISE} data though this will be due to the significant radio power contribution of the AGN. Thus \( SFR_{1.4} \) is an absolute upper limit to the SFR. Finally, we estimate the SFR from the near-ultraviolet band of the \textit{GALEX AIS}. This is done through the relation of Schiminovich et al. (2007) adapted from Salim et al. (2007)

\[
SFR_{\text{NUV}} = \frac{L_{\text{NUV}}}{9.26 \times 10^{20} \text{ W Hz}^{-1}} \quad [M_{\odot} \text{yr}^{-1}], \quad (\text{iii.5})
\]

where NUV is the near-ultraviolet band, 1750–2800 Å. With a NUV luminosity of \( (3.51 \pm 0.30) \times 10^{20} \text{ W Hz}^{-1} \), this yields \( SFR_{\text{NUV}} = 0.379 \pm 0.032 \ M_{\odot} \text{ yr}^{-1} \). This is lower than estimates from the \textit{WISE} data. However, this is not surprising, as we have not corrected for any attenuation of the NUV band due to dust. This can be corrected for if the attenuation factor is known (or can be calculated, e.g. Johnson et al., 2007). Considering the difference in the NUV and FUV flux densities (1.79 ± 0.28) we can see from Fig. 13 of Salim et al. (2007) that the attenuation factor is almost certainly > 1. The attenuation factor cannot be accurately calculated in this case so we consider \( SFR_{\text{NUV}} \) to be the absolute lower-limit to the true SFR. Thus, within absolute limits the SFR may lie within \( 0.379(\pm 0.032) \leq SFR \leq 131(\pm 5) \ M_{\odot} \text{ yr}^{-1} \). However, due to the power of the radio emission both of the core and the apparent lobes, we can certainly state that the radio power is grossly overestimating \( SFR_{1.4} \) due to the presence of a strong AGN. As we cannot determine the AGN contribution, a more reasonable estimate involves only \( SFR_{\text{NUV}} \) and \( SFR_{\text{MIR}} \): \( 0.379(\pm 0.032) \leq SFR \leq 2.17(\pm 0.18) \ M_{\odot} \text{ yr}^{-1} \).
§iii.3.7. Scenarios for the origin of the curious morphology

Based on the available radio, infrared, and optical data, we consider the following three scenarios for the observed morphology and emission from ESO 472-G013:

- an irregular galaxy with double-lobed structure
- an in-process merger between two galaxies
- a spiral galaxy with a double-lobed structure

In all scenarios, gravitational interaction between ESO 472-G013 and ESO 472-G012 may be resulting in the disturbed lobe structure seen, however in the case of an ongoing merger, this may not be necessary. The AGN is likely in its early stages given the spectral index of $\alpha = -0.555 \pm 0.003$ for the core region, and dust is almost certainly present due to the attenuation of the FUV band of GALEX.

In this scenario of an irregular galaxy with double-lobed structure, the irregularity may have been caused by a past merger between two galaxies, at least one of which a spiral. The merger may have triggered a radio-loud AGN, resulting in the radio emission and lobe-structure seen. The irregularity of the galaxy is clear in the DSS2 images, though to confirm this morphology, a higher-resolution follow-up with an optical telescope would be necessary. Irregular galaxies are known to host AGN, usually classed as radio-quiet Seyfert galaxies (Seyfert, 1943) of which spirals are also hosts. This classification is reflected in the WISE colours of Fig. iii.16, which suggest this is a composite Seyfert/star-forming galaxies. However, the radio power of the lobes is sufficient to consider the object as radio-loud (see e.g. Wilson and Colbert, 1995) and given the projected size of $\sim 400$ kpc at the redshift of ESO 472-G013 that the classification of Seyfert (or similar radio-quietness) is not correct.

Similar to the previous scenario, we instead consider that the merger is at an earlier stage, with the lobes again being generated by an newly formed AGN, which is consistent with the flat spectral index. In this scenario, the lobes might not be fully-formed, with the potential to increase in size along the lifetime of the AGN perhaps up to the canonical giant radio galaxy (GRG; see e.g. Saripalli et al., 2005) stage with an LLS $> 700$ kpc. This assumes that their projected LLS represents their true LLS. In this scenario is is likely that at least one of the original galaxies was a spiral given the dust present.

A spiral galaxy with double-lobed structure is a possibility, given the literature classifications of ESO 472-G013. In this scenario we are simply seeing a radio-loud spiral galaxy. The galaxy would be similar to those spirals detected by Ledlow et al. (1998); Hota et al. (2011); Bagchi et al. (2014); Mao et al. (2015); Singh et al. (2015), and Mulcahy et al. (2016). Such galaxies are found in under-dense environments, e.g. the outskirts of clusters or groups. ESO 472-G013 finds itself with a companion, ESO 472-G012, but also AM 2356-245 approximately 13.8 arcmin away. This environment does not suggest an over-dense region. To explore this scenario, higher-resolution optical imaging will need to be done to see not only the general spiral morphology, but also to determine the orientation of the
disk. To further complement such an observation, higher-resolution radio imaging, perhaps with the ATCA, might provide a better indication of the orientation of the jets, and the structure of the core.

§iii.3.8. Conclusion

The galaxy ESO 472-G013 is seen to have a radio-loud AGN at its core, producing large-scale (projected LLS $\sim 400$ kpc) jets which appear to align perpendicularly to the major axis of the galaxy. We show through established WISE colour-colour diagrams that the mid-infrared emission suggests a Seyfert AGN with current star-formation. The infrared data does not suggest the powerful AGN that is observed. We calculate SFR via WISE SFR relationships as well as NUV and 1.4 GHz. The ultraviolet SFR is a lower limit due to dust attenuation, the 1.4 GHz SFR is contaminated by AGN emission, and the MIR SFR is an upper-limit. The somewhat flat spectral index ($\alpha = -0.555 \pm 0.003$) of the core is suggestive of either new or restarted core activity, which may be implicative of a recent or ongoing merger consistent with an irregular morphology. We suggest that, to confirm the morphology of the host galaxy and the orientation of the jets, follow-up observations would be required.
§iv. Summary

During the course of this work, our primary goal was to investigate extended, diffuse emission associated with galaxy clusters within a 45 degree by 45 degree radio image centred on R. A. = 0°, decl. = −27°. The image has a central frequency of 168 MHz and a resolution of ∼2.3 arcmin with a sensitivity of up to ∼2.3 mJy beam−1. The types of emission most interesting to us were radio haloes, relics, and phoenices; emission from relativistic electrons in cluster magnetic fields, associated with the ICM rather than a particular galaxy within a cluster.

In doing so, we have identified, classified and measured 168 MHz radio properties, where possible, of a number of diffuse radio sources in the field including 11 haloes, 9 relics, and 3 phoenices. A subset of these are new discoveries and add to the slowly growing sample of such emission. We update the known $P_{1.4}$–$L_X$ and $P_{1.4}$–$M$ relations between radio halo power and cluster X-ray luminosity and mass to find that an increase in sample size greater than a factor of two has yielded consistent fitting parameters to the relations. We see that the detection limit, derived from the $P_{1.4}$–$M$ relation, of radio haloes with the EoR0 field is upheld, and we find that the MWA is able to push into higher-redshift, lower-mass clusters. However we note that the MWA is still limited by its resolution, which is a function of its current longest baseline of ∼3 km, and we still require high-resolution follow-up on a number of ambiguous and otherwise hard to classify steep-spectrum emission that has been detected as part of this work.

As part of follow-up work, we made use of DDT to image the cluster Abell S1136 with the ATCA at 2.1 GHz in the hopes of detecting core emission from a long-dead radio galaxy associated with ESO 470-G020—the BCG of the cluster. We detected the steep-spectrum, remnant lobes at 168 MHz and within the TGSS images at 147.5 MHz, and provided follow-up spectral analysis with GLEAM, providing a spectral index of $\alpha_{231}^{72} = -1.81 \pm 0.12$ averaged over the entire emission. In the ATCA image we detect a faint core and measure a spectral index of $\alpha_{2274}^{1413} = -1.39 \pm 0.55$ which has a large uncertainty due to the low-brightness of the emission. We also find a number of faint point sources embedded as well, though do not provide spectral indices due to their low signal-to-noise ratios.

The cluster Abell S1063 was analysed with archival ATCA data, within which we hoped to find a massive diffuse halo but only radio galaxies were clearly detected in the ATCA images, which had sensitivity to structures up to 21 arcmin. The rms noise in the stacked ATCA image at 2.1 GHz was 18 µJy. We had expected to see a halo in this cluster due to the morphology of the blended sources at 168 MHz but also due to the cluster’s massive and X-ray luminous nature.

Finally, ESO 472-G013, a disk galaxy hosting large-scale radio lobes, is investigated after being detected within the EoR0 field. We measure a spectral index across the narrow GLEAM bands of $\alpha_{72}^{231} = -0.91 \pm 0.04$ for the lobes and core.
combined. We note that the core alone has a spectral index, from higher-frequency, higher-resolution imaging, of $\alpha_{\text{core}} = -0.555 \pm 0.003$. In comparison with $WISE$ colour–colour plots we consider that ESO 472-G013 is likely star-forming, and estimate its star-formation rate via its $WISE$ MIR, $GALEX$ NUV, and 1.4 GHz properties. We see that the 1.4 GHz SFR is overestimated due to the presence of a radio-loud AGN. We compare ESO 472-G013 to other disk galaxies hosting large-scale radio lobes and other radio galaxies within the the context of their 325 MHz power and LLS measurements, finding that ESO 472-G013 lies within the space occupied by similar disk galaxies. Lastly, we briefly consider the origins of the morphology and AGN activity of ESO 472-G013, considering a number of scenarios that might have led to its current state.
Bibliography


Bibliography


§A. Source-finding and measuring with Witchwood

In what follows we describe source-finding software used during the course of this work. The software does not do anything new, and was written as a pet-project by the author of this work. We describe it here because there is no documentation for it elsewhere, and it was used in the data analysis presented in all sections. The code is hosted at https://github.com/Sunmish/Witchwood.

During the course of this work it became clear the measuring flux densities of radio sources would be a necessary thing over and over again. Source-finding software exists that will take an input image, return sources above some threshold (typically some multiple of an input rms), and calculate the integrated flux density of each source. One such example, AEGEAN does this to great effect, going as far as fitting elliptical Gaussians to disentangle blended point sources. Despite its usefulness, AEGEAN is designed first and foremost for point-source–finding, whereas for this work we require software that simply measures the flux density of an extended source, without considering it as a point source (i.e. we consider the source to be larger than the beam and often of irregular morphology). In this section, we describe a simple source-finding and measuring routine named WITCHWOOD that simply finds pixel groups above a given threshold assumed to be discrete sources, and measures their integrated flux densities as well as calculating their largest angular scales.

This does not add anything beyond what is seen in other source-finding programs, rather it simply does what we needed to it do for most of our sources. WITCHWOOD is written in PYTHON and makes heavy use of the community-developed package, ASTROPY, as well as NUMPY. It is intended to be used from with other PYTHON scripts or from the PYTHON or IPYTHON console, hence works as a normal function. The main user-functions are measure_forest and measure_tree. The reader is encouraged to ignore the tortured metaphor. The first function performs the main source-finding on an image, returning a catalogue and an optional output FITS file that shows the detected sources and their numbers, as well as an optional annotation file for SAO’s DS9 or Karma’s Kvis which both simply show the source number of each source. Fig. A.1 shows example FITS image with source counts, as well as the original image with the annotation file overlaid.

The second function performs the source-finding, returning the catalogue, and then finds the closest source to input coordinates. Values are returned as PYTHON variables and optionally printed to the console in a readable format shown in Fig. A.2.

\footnote{For blended sources we use AEGEAN and assume our source can be represented as a point.}
Figure A.1: Example of WITCHWOOD source-finding on an EoR0 field image of the cluster Abell 0013. Left: Sources as detected by WITCHWOOD with an rms of 12 mJy beam$^{-1}$ with a cutoff of 3$\sigma_{\text{rms}}$. The colourscale is set to the source numbers. Right: The radio image with sources marked as in the left panel.

Figure A.2: Example output of WITCHWOOD during single-source–finding. The image was of Abell 0013, and the input coordinates were of the cluster centre. The nearest source is the relic slightly to the east. LAS has been optionally turned on for this measurement. Setting the output to anything but “None” will write out the example FITS file in Fig. A.1. Note that the integrated flux density has not been scaled as per §ii.1.3.2.
§A.1. The floodfill algorithm

WITCHWOOD works by making use of the floodfill algorithm. The floodfill algorithm is used in many applications (and in fact, many source-finding applications) and works by spreading from some initial point. That is, if we have a 3 by 3 array and start in the centre, we would check each surrounding cell and for any surrounding cells that meet some condition we would add that cell and do the same check with the cells surrounding that one. This continues until no border cells pass the condition. Within the context of WITCHWOOD, we make a pass of the input array and any time a pixel is detected above the input threshold, we look at the surrounding pixels to see if they too are above this threshold. If so, they are added to that source. This process can be time- and process-consuming, so we have a reference array which is simply used to check if we have looked at a pixel previously. This avoids double (and triple and quadruple, et cetera) checking. This continues over the entire input array, and sources—when found and added to—are written to dictionaries for later keeping.

§A.2. Calculating the flux density and other measurements

§A.2.1. Flux density

The primary purpose of WITCHWOOD was never source-finding, rather we needed an easy way of measuring flux densities of sources whose positions we already knew. The measurement of most importance is that of the integrated flux density and its associated error. WITCHWOOD is designed to work with radio images with pixel values in units of Jy beam$^{-1}$, thus to make a measurement of the integrated flux density we simply sum the pixel values that comprise our source and correct for the beam. The floodfill algorithm defines which pixels will be used. The integrated flux density is then

$$S_\nu = \sum_n S_n \times \left[ \frac{|c_1c_2|4 \ln 2}{\pi B_{\text{maj}}B_{\text{min}}} \right] \text{[Jy]},$$  \hspace{1cm} (A.1)

where the sum is over the $N$ pixels comprising the source, $c_1$ and $c_2$ are the pixel dimensions, $B_{\text{maj}}$ and $B_{\text{min}}$ are the major and minor axes of the beam FWHM, and the factor of $\ln 2$ accounts for the integral over the Gaussian surface of the beam. The associated uncertainty is

$$\sigma_{S_\nu} = \sigma_{\text{rms}} \sqrt{N_{\text{beam}}} \text{ [Jy]},$$  \hspace{1cm} (A.2)

where $\sigma_{\text{rms}}$ is the user-supplied rms for the map and $N_{\text{beam}}$ is the number of beams crossing the source. We assume the rms does not vary significantly over the source. These flux density measurements are similar to those done by the software DUCHAMP (Whiting, 2012).
§A.2.2. Other quantities

A useful secondary application of WITCHWOOD is the calculation of the largest angular scale (LAS) of any sources found. During the source-finding, any pixels that are the boundary of a detection are written to a separate dictionary tied to the associated source. During the flux density calculation step, we also compare the separations of all boundary pixels with one another. This is a reasonably long task as we need to check $N^{3/2}$ separations for $N$ pixels. The greatest of these is considered the LAS.

Finally, we define source positions in two ways in the same way as DUCHAMP. The first is by the brightest pixel of a source. For a point source this would be its centre, but for extended sources this is not necessarily the case. The second position is the flux-weighted coordinates. These are defined to be

$$\begin{align*}
x_w &= \frac{\sum_{n}^{N} x_n S_n}{\sum_{n}^{N} S_n}, \\
y_w &= \frac{\sum_{n}^{N} y_n S_n}{\sum_{n}^{N} S_n},
\end{align*}$$

for pixel coordinates $x$ and $y$ which are later converted to world coordinates in degrees by use of ASTROPY.